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COMPARISON OF MEASURED AND CALCULATED
FLOW PROPERTIES AFTER THE ROTATING CASCADES OF
A THREE-STAGE AXIAL-FLOW COMPRESSOR

by

Salvatore Frank Gallo

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THESIS

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COMPARISON OF MEASURED AND CALCULATED
FLOW PROPERTIES AFTER THE ROTATING CASCADES OF A
THREE-STAGE AXIAL-FLOW COMPRESSOR

by

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ABSTRACT

This work was undertaken to check the feasibility of obtaining the velocity profiles downstream of the rotors of turbomachines by measuring only the radial distributions of total temperature, total pressure, and absolute flow angle and using these data to calculate the flow velocities by the non-isentropic radial equilibrium equation such that the measured flow rate is matched. Curvature effects are ignored in this analysis.

The velocities calculated by this method are compared with those obtained by measurements with flow probes and hot-wire anemometers.

The tests were conducted on a 3-stage axial flow compressor of the Turbo-Propulsion Laboratory at the Naval Postgraduate School. Measurements were made over the entire operating range of the compressor at a fixed rotor speed of about 1200 rpm.

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TABLE OF SYMBOLS

Symbols

B_k	Gross weight flow blockage factor
c_p	Specific heat at constant pressure for air (0.24 Btu/lbm-°R)
g	Gravitational constant (32.17 lbm-ft/lbf-sec ²)
H	Stagnation enthalpy (Btu/lbm)
J	Conversion factor (778 ft-lbf/Btu)
M_v	Mach number of absolute velocity
M_w	Mach number of relative velocity
P	Static pressure (psfa)
P_t	Total pressure (psfa)
q	Velocity head - $\frac{1}{2} \rho V^2$ (psf)
r	Radius (ft)
R	Radius (in.)(symbol used in figures only)
R	Gas constant for air (53.35 ft-lbf/lbm-°R)
S	Stagnation entropy (Btu/lbm-°R)
T	Static temperature (°R)
T_t	Total temperature (°R)
U	Peripheral velocity (ft/sec)
V	Absolute velocity (ft/sec)
W	Relative velocity (ft/sec)
W	Mass flow rate (lbm/sec)
z	Axial direction

Greek Letters

α	Absolute flow angle (degrees)
β	Relative flow angle (degrees)
γ	Ratio of specific heats (1.4 for air)
ρ	Mass density (slugs/ft ³)
ϕ	Axial velocity ratio
$\bar{\phi}$	Average axial velocity ratio
ψ	Pressure coefficient

Subscripts

a	Axial direction
o	Outer (used in conjunction with radius)
r	Radial direction
T	Tip (used in conjunction with peripheral velocity)
u	Peripheral direction
0	Inlet screen position
1	Inlet survey plane
2	Inlet guide vane

SECTION 1

INTRODUCTION

The experimental analysis of performance of turbomachinery requires detailed and accurate measurement of the flow properties within the passages of the machine under investigation.

Even at the present state of the art it is necessary to make a number of simplifying assumptions for the design of turbomachines. A limited amount of basic design data is available which may not apply directly to a particular type of machine. It is necessary, therefore, to check the accuracy of the design method by testing actual machines. For axial type turbomachines it is of great interest to know the flow profiles after the different stages since this information indicates whether the flow deflections, losses, and velocity distributions on which the design was based have been realized. Comparison of assumed and actual flow properties will make it possible to correct or improve the design procedure with the result that the performance of later machines can be predicted with greater accuracy.

The measuring of the flow properties between the rows of blades of axial turbomachines is connected with considerable difficulties. It is necessary to use small probes to avoid disturbing the flow; and some of the more accurate probes, such as Pitot-static probes, cannot be arranged because of small axial blade clearances. Flow angles, total pressures, and total temperatures can be measured with relative ease and sufficiently small probes. To establish the velocity profiles, however, it is necessary to know the static pressure and the static temperature. The measuring of these quantities between the rows of turbomachines can usually be carried out only with probes that have been calibrated for different

Mach number, Reynolds number, proximity of walls, and flow angles. For these reasons the accuracy of such measurements is low, and the experimental procedure is quite difficult.

The purpose of this study is to determine whether it is possible to use the first-mentioned measurements together with certain theoretical flow relations to obtain the flow profiles with a sufficient degree of accuracy. These conditions are checked on a three-stage axial compressor of large size where the axial clearances between the rows of blades make it possible to measure the velocities directly with calibrated flow probes and hot-wire instruments. This compressor will henceforth be called the O.N.R. compressor since the Naval Postgraduate School received this machine from the Office of Naval Research, Department of the Navy.

The author gratefully acknowledges the guidance and counsel of Professor M. H. Vavra of the Department of Aeronautics of the Naval Postgraduate School. Professor Vavra not only guided this research project but also gave the author an appreciation of what it means to be an engineer.

The author also wishes to express his appreciation to the Office of Naval Research which made the compressor used in this study available to the Naval Postgraduate School.

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SECTION 2

BASIS FOR THE ANALYSIS

For any flow condition there are two principal equations of conservation which must be satisfied, namely, the equation of motion and the equation of continuity.

The following simplifying assumptions are made for the present treatment:

1. The fluid is assumed to be a perfect gas.
2. The general flow equations are applied to compute fluid properties between blade rows where blade forces are nonexistent.
3. The flow is assumed to be steady.
4. The flow is assumed to be axisymmetric. By this assumption, all partial derivatives with respect to the peripheral coordinate are taken to be equal to zero. Basically, this is the equivalent of saying that the three dimensional flow through a blade row can be represented by the circumferential average of the flow conditions at each radial position.
5. The flow is assumed to be adiabatic.
6. The shearing stresses at the annulus boundaries are ignored in the equation of motion, but their effects are reflected by the use of measured data.
7. The specific heat of the gas is assumed to be constant.

With these simplifying assumptions, the equation of motion as defined by Vavra (1) and the equation of continuity, respectively, are

$$\nabla H = T \nabla S + \vec{V} \times (\nabla \times \vec{V}) \quad (1)$$

$$\nabla \cdot (\rho \vec{\nabla}) = 0 \quad (2)$$

Since this study deals with the radial variations of fluid properties, it suffices to use the radial components of Eq. 1. In consistent engineering units,

$$J_g C_p \frac{\partial T_t}{\partial r} = J_g T \frac{\partial S}{\partial r} + V_u \frac{\partial V_u}{\partial r} + \frac{V_u^2}{r} + V_a \frac{\partial V_a}{\partial r} - V_a \frac{\partial V_r}{\partial z} \quad (3)$$

A further simplifying assumption is made inasmuch as the radial accelerations due to streamline curvature are ignored, thus eliminating the last term in Eq. 3. This assumption is valid for lightly loaded machines where the curvatures of the meridional flow path are small as described by Harrison (2) and Giamati and Finger (3). Since both conditions are met by the O.N.R. compressor, the error introduced by this assumption will be small.

In consistent engineering units the equation of continuity can be expressed by

$$\dot{W} = 2\pi g \int_{r_{hub}}^{r_{tip}} \rho V_a r dr \quad (\text{lbm/sec}) \quad (4)$$

The integration of Eq. 4 within the boundary layer of the annulus walls requires extensive data in the boundary layer. These data were not available in this study due to the physical dimensions of the probes which were used to obtain the surveys. The introduction of a gross weight flow blockage factor in the equation simulates the effect of the boundary layer by increasing slightly the axial velocity components to meet the required continuity condition. With the weight flow blockage factor B_k , Eq. 4 becomes

$$\dot{W} = 2\pi g B_k \int_{r_{hub}}^{r_{tip}} \rho V_a r dr \quad (\text{lbm/sec}) \quad (5)$$

Equations 3 and 5 require iterative solutions to satisfy both equations. In addition, the non-linearities in Eq. 3 require numerical solutions; hence, the use of a high speed computer is almost a necessity to carry out the procedure.

Equation 3 was multiplied by dr , and integration yields

$$\int_{r_i}^r J_g C_p \frac{\partial T_t}{\partial r} dr = \int_{r_i}^r J_g T \frac{\partial S}{\partial r} dr + \int_{r_i}^r V_u \frac{\partial V_u}{\partial r} dr + \int_{r_i}^r \frac{V_u^2}{r} dr + \int_{r_i}^r V_a \frac{\partial V_a}{\partial r} dr \quad (6)$$

Stations r and r_i are two closely adjoining radial stations.

Some of the terms in Eq. 6 may be integrated directly, but the integrals containing entropy changes and the one involving V_u^2/r must be determined numerically.

Across any blade row the difference in entropy at a given stream-line may be expressed by

$$J\left(\frac{S}{R}\right)_2 - J\left(\frac{S}{R}\right)_1 = \ln \left[\frac{(T_{t2}/T_{t1})^{\frac{\gamma}{\gamma-1}}}{(P_{t2}/P_{t1})} \right] \quad (7)$$

The symbol S represents the stagnation entropy. Subscript 2 refers to the downstream position and subscript 1 to the upstream position. The entropy gradient across the blade row on two closely adjoining stream-lines may now be calculated. For descriptive purposes two such stream-lines will be subscripted by i and j .

Subtracting the axial entropy change across the blade row on stream-line i from that on j yields

$$J\left(\frac{S}{R}\right)_{2j} - J\left(\frac{S}{R}\right)_{1j} - J\left(\frac{S}{R}\right)_{2i} + J\left(\frac{S}{R}\right)_{1i} = \ln \left[\frac{(T_{t2j}/T_{t1j})^{\frac{\gamma}{\gamma-1}}}{(P_{t2j}/P_{t1j})} \right] - \ln \left[\frac{(T_{t2i}/T_{t1i})^{\frac{\gamma}{\gamma-1}}}{(P_{t2i}/P_{t1i})} \right] \quad (8)$$

The numerical value of the entropy gradient in the radial direction may now be simplified by assuming that position 1 is far upstream where no radial entropy gradient exists and where radial gradients of total temperature and total pressure are zero. Therefore, $T_{t_{1i}}$ equals $T_{t_{1j}}$, and $P_{t_{1i}}$ equals $P_{t_{1j}}$. Then Eq. 8 simplifies to

$$S_{2j} - S_{2i} = \frac{R}{J} \ln \left[\frac{(T_{t_{2j}}/T_{t_{2i}})^{\frac{\gamma}{\gamma-1}}}{(P_{t_{2j}}/P_{t_{2i}})} \right] \quad (9)$$

The integration of the term in Eq. 6 that contains the entropy gradient $\partial S / \partial r$ is then

$$\int_{r_i}^r J_g T \frac{\partial S}{\partial r} dr = \frac{1}{2} \frac{R}{J} \ln \left[\frac{(T_t/T_{ti})^{\frac{\gamma}{\gamma-1}}}{(P_t/P_{ti})} \right] J_g (T + T_i) \quad (10)$$

The static temperature appearing in Eq. 10 may be expressed by the stagnation temperature T_t and the absolute velocity V , or by

$$T = T_t - \frac{\gamma-1}{2} \frac{V^2}{\gamma g R} \quad (11)$$

With Eq. 11, Eq. 10 becomes

$$\int_{r_i}^r J_g T \frac{\partial S}{\partial r} dr = \frac{1}{2} \ln \left[\frac{(T_t/T_{ti})^{\frac{\gamma}{\gamma-1}}}{(P_t/P_{ti})} \right] \left[g R (T_t + T_{ti}) - \frac{\gamma-1}{2\gamma} (V^2 + V_i^2) \right] \quad (12)$$

The non-linear term in Eq. 6 containing V_u^2/r can be evaluated numerically by

$$\int_{r_i}^r \frac{V_u^2}{r} dr = \frac{\left(\frac{V_u^2}{r} + \frac{V_{u_i}^2}{r_i} \right)}{2} (r - r_i) \quad (13)$$

For simplification, let

$$F = \ln \left[\frac{(T_t/T_{t,i})^{\frac{\gamma}{\gamma-1}}}{(P_t/P_{t,i})} \right] \quad (14)$$

Since V_a at an arbitrary radius is to be determined, V and V_u in Eq. 6 are expressed by V_a and α , or

$$\begin{aligned} V_u^2 &= V_a^2 \tan^2 \alpha \\ V^2 &= V_a^2 (1 + \tan^2 \alpha) \end{aligned} \quad (15)$$

Equation 6 may now be solved for V_a at an arbitrary radius r ,

$$\begin{aligned} V_a^2 &= \left[\frac{1}{1 - F \frac{\gamma-1}{2\gamma} + \tan^2 \alpha (2 - \frac{\gamma}{\gamma-1} - F \frac{\gamma-1}{2\gamma})} \right] \\ &\quad \left[2gR \frac{\gamma}{\gamma-1} (T_t - T_{t,i}) - FgR(T + T_{t,i}) + \right. \\ &\quad \left. V_{a,i}^2 (F \frac{\gamma-1}{2\gamma} + 1) + V_{a,i}^2 \tan^2 \alpha_i (F \frac{\gamma-1}{2\gamma} + 2 - \frac{\gamma}{\gamma-1}) \right] \end{aligned} \quad (16)$$

With measured values of total temperature, total pressure and flow angle as a function of radius, Eq. 16 could be solved at all radial positions if the reference axial velocity $V_{a,i}$ were known.

In Eq. 5 the density is a function of velocity. For a perfect gas

$$\rho = \frac{P}{RT} \quad (17)$$

From isentropic relationships

$$\left(\frac{P_t}{P} \right) = \left(\frac{T_t}{T} \right)^{\frac{\gamma}{\gamma-1}} \quad (18)$$

Combining eqs. 17 and 18 with the static temperature of Eq. 11

$$\rho = \frac{P_t}{RT_t} \left(1 - \frac{\gamma-1}{2\gamma} \frac{V^2}{RgT_t} \right)^{\frac{1}{\gamma-1}} \quad (19)$$

This quantity introduced into Eq. 5 establishes the flow rate for the assumed velocity V_{a_i} . If it does not agree with the measured flow rate, a new reference axial velocity V_{a_i} is assumed to obtain an improved solution of Eq. 16; and the process is repeated until agreement between the measured and calculated mass flow rates is reached.

Since Eq. 16 contains differences instead of differentials, it is evident that small increments in radius are necessary to insure accuracy in the final results.

The described method of velocity determination is similar to that presented in Ref. 3 for the design and off-design analysis of axial flow compressors.

SECTION 3

COMPUTER TECHNIQUE FOR SOLUTION

A computer program for the calculation of the radial flow properties downstream of a rotor row was prepared for the IBM-360-67 computer in Fortran IV language.

The program is specifically set up for the O.N.R. three-stage axial compressor of the Naval Postgraduate School described in Section 4, but slight modifications make it applicable to radial surveys downstream of arbitrary axial rotor rows of either turbines or compressors for the assumptions stated in Section 2.

3.1 Non-Isentropic Radial Equilibrium Equation

The computer program has been set up for data from a maximum of fifty radial stations, not necessarily extending to the hub and to the tip radii, although accuracy would be reduced if data were not measured close to the hub and the tip of the blading. Values of total pressure, total temperature, and absolute flow angle are introduced as a function of radius. Other input values are measured flow rate, initial reference value of axial velocity, assumed blockage factor, desired accuracy in flow rate matching, and rotor speed.

The introduced data which are measured at discrete radii are first expressed with fourth order polynomials as a function of radius. The polynomial fit for the data was obtained by the method of least squares. Due to the smooth change of the data, the polynomial fit was extremely accurate throughout the radial span for all the parameters. An example of the accuracy of the curve fit is given in Table B-2 where the symbol X signifies radius; F2, the input data for different radii; Y, the values

of the parameter obtained from the polynomial; and DELY, the difference between the measured data and those from the polynomial. The subprogram used for the polynomial curve fitting is available in the Naval Postgraduate School subroutine library and is presented in Appendix B.

A maximum of one hundred points may be specified at which the equilibrium equation is to be solved. For brevity, the non-isentropic radial equilibrium equation shall be referred to as the NISRE equation in the remainder of this presentation. The radial positions of the points are obtained by dividing the radius from hub to tip into equal increments. Values of total pressure, total temperature and absolute angle of flow are then obtained from the polynomials at these specified radial positions. The measured mass flow rate is calculated from measured conditions in the inlet to the compressor.

The subprogram dealing with the NISRE equation then solves for the axial velocity and density profile from blade hub to blade tip. The profiles thus obtained are used in the continuity equation which is integrated by the trapezoidal method. The initial axial velocity at the reference position is then changed arbitrarily, and a second solution is generated. The third and subsequent values of the reference axial velocity are calculated with the Newton-Raphson iteration technique. This process continues until the desired accuracy in mass flow rate is obtained.

With the axial velocity profile thus determined, all remaining fluid properties may be calculated. These properties are printed out in dimensional and non-dimensional form. Examples of the print out of the solutions are presented in Tables B-3 and B-4.

3.2 Determination of Velocity Profiles with Flow Probes

The measured values of total pressure, static pressure, absolute flow angle, total temperature and rotor speed are used to obtain the axial velocity profile. The fluid properties at different radial stations are calculated and printed out in a format similar to that of the NISRE equation (See Tables B-5 and B-6.).

3.3 Determination of Velocity Profiles with the Hot-Wire Anemometer

The hot-wire anemometer survey was made at the same positions as the flow probe and total temperature surveys. To place the hot-wire as nearly perpendicular as possible to the flow, the absolute flow angle at each radial position was obtained from a five-hole probe. The hot-wire output was set to a reference value at the mean square radius of the annulus, and all values were measured with respect to this setting. The velocity determined by the flow probe at the mean square radius was used as the reference velocity for the hot-wire anemometer. The root mean square radius was used as reference radius since the wall interference effects on the flow probe are small at this location.

Tables B-7 and B-8 give sample outputs of the flow properties at different radii calculated from the measured data. It should be noted that the static pressures and static temperatures are the values obtained from the analysis. The measured static pressures are not used in these calculations.

SECTION 4

O.N.R. THREE-STAGE AXIAL-FLOW COMPRESSOR

The compressor installation is shown in Fig. 1. A detailed description of the test installation is given by Bowen et al. (4). Marshall (5) describes the test set up at the Naval Postgraduate School.

The compressor is suitable for a large variety of research experiments. Each one of the rotor and stator blade rows may be removed. Although stagger angles are adjustable, they were not varied during the present experiments. All three rotor blade cascades were set at a stagger angle of 43.8 degrees, with all stator blade stagger angles at 39.8 degrees.

The casing of the compressor was designed to give maximum accessibility for measuring instruments. Six rectangular instrument ports are located in the upper half of the casing. These ports accommodate a special instrument carriage permitting detailed surveys in radial and peripheral directions (Fig. 2). Three of the instrument ports are suitable for stator outlet surveys over a peripheral arc of 15 degrees, and the other three are suitable for rotor outlet surveys over the same arc. Only rotor outlet surveys were made during this study.

The casing has numerous radial survey ports. Several of these were used downstream of each rotor.

The compressor is electrically driven and operates at two fixed speeds of either about 900 rpm or 1200 rpm.

The inlet duct (Fig. 3) consists of a screen, an entrance bellmouth and a length of straight pipe with a honeycomb flow straightener ahead of the inlet guide vanes.

The compressor discharge (upper foreground of Fig. 1) is fitted with an electrically operated throttle valve whose positions are indicated by a counter.

SECTION 5

INSTRUMENTATION

The compressor inlet duct allows vertical and horizontal surveys to be made across the inlet as well as at 60 degrees from the vertical direction by unbolting and rotating the inlet duct. A 3/32 inch diameter Prandtl-type Pitot-static probe was mounted for vertical survey (Fig. 4) with readout on a Meriam Instrument Company Model-750 Micromanometer (Fig. 5). A 1/4 inch diameter hot-wire anemometer probe was mounted for horizontal survey. The hot-wire probe was constructed at the Naval Postgraduate School and provides for quick changing of tips in the event of wire breakage (Fig. 6). A supply of tips was kept readily available during the inlet surveys, and tip replacement was effected on several occasions while the compressor was in operation. Hot-wire data were read on a Security Associates Applied Sciences Model 200 Constant Temperature Anemometer. Details of the flow rate measurement are given in Section 6.

Wet and dry bulb Mercury glass thermometers were mounted on the inlet screen.

A 1/4 inch diameter Prandtl-type Pitot-static probe was installed between two of the inlet supports ahead of the guide vanes (foreground of Fig. 7) with readout on the same micromanometer as the inlet duct Pitot-static probe. This was made possible by the use of two scanner valves (Fig. 8). In addition, a 1/8 inch diameter Kiel probe with a total type thermocouple was mounted in the same meridional plane through one of the radial access ports. This total temperature probe is shown in the foreground of Fig. 7. The reference junction of the thermocouple

was placed in an ice bath. The output of the thermocouple was read on a Leeds and Northrup Potentiometer (Fig. 9).

Radial surveys were conducted downstream of each of the three rotor blade rows. Total and static pressure measurements were obtained with a United Sensor Corporation DA120 five hole probe (serial number 535) although the pitch angle was assumed to be zero. The five hole probe was mounted in the special carriage mentioned in Section 4 with readout on a water manometer board (Fig. 10). Flow direction was obtained by balancing pressure on the static ports. Total pressure and the difference between total pressure and static pressure were measured with the same manometer board. Total temperature measurements at different radii were obtained by use of a thermocouple mounted in a 1/4 inch diameter Kiel probe which was placed in one of the radial access holes. The reference junction for this thermocouple was also placed in an ice bath, and the aforementioned potentiometer was used for the readout by the use of the double-pole double-throw knife switch shown in the background of Fig. 9. Hot-wire anemometer data at different radii were measured after each of the three rotor blade rows by means of a 1/4 inch diameter hot-wire probe. Figure 11 shows the installation of the total temperature probe and the hot-wire anemometer probe used for the radial surveys. The hot-wire anemometer readout instrument is shown in Fig. 9.

Compressor speed was measured with a flux cutter mounted on the compressor drive shaft whose impulses were read on a Monsanto Model 100A Counter-timer.

SECTION 6

FLOW RATE CALIBRATION

The purpose of the flow calibrations was to obtain a factor which, when multiplied by the velocity ahead of the inlet guide vanes, gives the volume flow rate through the compressor.

Marshall (5) found a flow rate calibration factor for the O.N.R. compressor by means of horizontal and vertical surveys of the inlet with the existing Pitot-static probe. This calibration factor was to be checked by a more accurate survey with a hot-wire anemometer.

Since Marshall showed that the velocity profiles in the vertical and horizontal planes were similar, it was decided to conduct a survey in the horizontal plane only.

Since hot-wire instruments give only the ratio of the actual velocity to some reference velocity, initial hot-wire instrument setting was made at the inlet duct centerline where the velocity obtained from readings of the Prandtl type Pitot-static probe was used as the reference velocity. At the inlet duct centerline the Pitot-static probe is 18 inches from the duct wall; hence, wall effects are minimized. The hot-wire instrument was set at 90 per cent of full readout range at the centerline, and surveys were made at radial increments of 3 inches to a radius of 15 inches and of 0.2 inches to a point 0.2 inches from the duct wall. The design of the hot-wire probe prevented measurements closer to the wall. Frequent checks were made at the duct centerline to ascertain that the centerline setting of 90 per cent had not drifted. Such instrument drifts were noticed only on rare occasions. If drift occurred, it was always less than 2 per cent of full scale, and the hot-wire instrument

was then reset to 90 per cent. Surveys of this type were conducted on both sides of the centerline. Total pressure and velocity head readings were also taken at the duct centerline and ahead of the inlet guide vanes with the fixed Pitot-static pressure probe connected to a water micromanometer. Wet and dry bulb temperatures were recorded from the Mercury thermometers on the inlet screen. The temperature in the test cell was recorded also for the purpose of correcting water column heights.

The following symbols are used for the recorded data:

q_{1r}	-velocity head at the centerline of the inlet duct (in. H_2O)
$P_{t_{1r}}$	-total pressure at the centerline of the inlet duct (in. H_2O)
q_{2r}	-velocity head ahead of the inlet guide vanes (in. H_2O)
$P_{t_{2r}}$	-total pressure ahead of the inlet guide vanes (in. H_2O)
TOR	-temperature at the inlet screen ($^{\circ}F$)
BAR	-barometric pressure (in. Hg.)
TBAR	-temperature of the Mercury column ($^{\circ}F$)
TW	-temperature of the water column ($^{\circ}F$)
VRR	-hot-wire anemometer readings, right of centerline looking downstream (dimensionless)
VRL	-hot-wire anemometer reading, left of centerline looking downstream (dimensionless)

The specific gravity of the Mercury in the barometer was corrected for temperature by

$$GHGRM = 13.63905 - 0.0013630303 TBAR \quad (20)$$

The specific gravity of the water column was corrected for temperature by

$$GWRM = 0.99837633 + 1.0605756 TW \times 10^{-4} - 1.593186 TW^2 \times 10^{-6} \quad (21)$$

These specific gravity relations were obtained from tabulated data of Ref. 6.

With these corrections, pressures were converted to absolute values, or

$$PAMB = BAR (0.4891585) GHGRM \frac{144}{13.54} \quad (\text{psfa}) \quad (22)$$

where the constant 0.4891585 is the conversion factor from inches of Hg. to pounds per square inch for a specific gravity of Mercury of 13.54. Then

$$P_{t_1} = P_{t_{1R}} (GWRM) \frac{62.42732}{12} + PAMB \quad (\text{psfa}) \quad (23)$$

The constant 62.42732 is the conversion factor from feet of water to pounds per square foot for a specific gravity of water of 1.0.

$$q_1 = q_{1R} (GWRM) \frac{62.42732}{12} \quad (\text{psf}) \quad (24)$$

The static pressure P_1 was then calculated by

$$P_1 = P_{t_1} - q_1 \quad (\text{psfa}) \quad (25)$$

Because of the low velocities of about 70 feet per second in the inlet duct, and ahead of the compressor inlet guide vanes, compressibility effects were ignored, and the temperature TOR at the inlet screen was used as the static temperature.

$$T_o = TOR + 459.7 \quad (^\circ R) \quad (26)$$

Considering the air entering the compressor as a perfect gas having a gas constant R of 53.35 (ft-lb)/(lbm-°R), the mass density is

$$\rho_1 = \frac{P_1}{gRT_0} \quad (\text{slug/ft}^3) \quad (27)$$

For each run the density was taken as the average obtained from all readings.

The velocity at the inlet duct centerline was then calculated by

$$V_1 = \sqrt{\frac{2g_1}{\rho_1}} \quad (\text{ft/sec}) \quad (28)$$

This velocity was used as the reference velocity for the hot-wire anemometer setting. Then, the average velocity V at an arbitrary radius is taken as

$$V = \left(\frac{VRL}{2} \frac{VRR}{2} \right) \frac{V_1}{0.9} \quad (\text{ft/sec}) \quad (29)$$

The constant 0.9 must be introduced since the hot-wire anemometer was set at 90 per cent of full scale readout of the instrument at the centerline in case velocities higher than those at the centerline would occur.

The volume flow rate was calculated by

$$\begin{aligned} \text{VOLFL} = & 3.1416 V_1 \left(\frac{r_2}{2} \right)^2 + 3.1416 \sum_{i=2}^{n-1} \left\{ V_i \left[\left(\frac{r_i + r_{i+1}}{2} \right)^2 - \right. \right. \\ & \left. \left. \left(\frac{r_i + r_{i-1}}{2} \right)^2 \right] \right\} + 3.1416 V_n \left[\left(r_{n+1} \right)^2 - \left(\frac{r_n + r_{n-1}}{2} \right)^2 \right] \quad (\text{ft}^3/\text{sec}) \quad (30) \end{aligned}$$

The subscript 1 in the summation refers to the inlet duct centerline. The subscript n pertains to the reading 0.2 inches from the duct wall, and the subscript n+1 is for the conditions at the duct wall.

The velocity V_2 ahead of the inlet guide vanes was obtained in a similar manner, using the temperature measured at the inlet screen as the static temperature since the difference between total and static temperature is less than 0.4°F at the highest velocity of 70 feet per second.

The calibration constant for each run was obtained from

$$CCC = \frac{VOLFL}{V_2} \quad (\text{ft}^3/\text{sec per ft/sec}) \quad (31)$$

This constant was found to be $4.4050 \text{ ft}^3/\text{sec per ft/sec}$ velocity obtained ahead of the inlet guide vanes. The maximum relative deviation of CCC for all surveys was 0.3 per cent.

This data reduction was carried out on the IBM-360-67 computer. The program is explained in Appendix A which also gives a sample of the computer output.

SECTION 7

RADIAL SURVEYS

Radial surveys were conducted downstream of each row of rotor blades of the O.N.R. compressor. Radial distributions of total pressure, velocity head, total temperature, absolute flow angle, and hot-wire velocity ratio were obtained at various flow rates.

Flow rate was varied by means of the discharge throttle valve. After setting the throttle valve to a new position, data were taken only after waiting for about 20 minutes to stabilize the temperature in the test cell. The test cell has a front door through which air is normally admitted to the compressor from the atmosphere. The air is discharged back into the atmosphere through a door located opposite to the front door and aft of the compressor. However, experience showed that gusts in the atmosphere produced erratic measurements particularly with the hot-wire instrumentation. By closing the front door it was found that the flow oscillations could be minimized, but the above-mentioned waiting period was necessary for the air to reach a new equilibrium temperature in the test cell. Steady temperature conditions were checked by the mercury thermometer at the inlet screen and the total temperature Kiel probe ahead of the inlet guide vanes.

Periodic readings of the total pressure, velocity head and total temperature ahead of the inlet guide vanes were recorded during each run for the determination of the flow rates. Conditions at the inlet screen and ahead of the inlet guide vanes were found to be very stable for all flow rates irrespective of throttle settings and atmospheric conditions.

The previously described traversing instruments for the radial

surveys were mounted downstream of each one of the rotors. Initially, a peripheral survey was made with the flow probe at various radii to check whether the flow conditions were uniform in the peripheral direction. Generally, this was found to be true downstream of each row of rotor blades at flow rates above full stall.

For most of the radial survey runs a hot-wire instrument setting of 90 per cent was used at a reference radius of 14.5 inches, or very close to the root mean square radius of the annulus. To properly position the hot-wire with respect to flow direction, initial angle setting of the probe was made with the flow angles obtained from the flow probe. This setting was then refined by turning the hot-wire into the direction which gave maximum output. Almost without exception, the hot-wire angle position thus found was identical with the angle measured by the flow probe. The instrument setting of 90 per cent at the radius of 14.5 inches was periodically checked for drift. Drift was encountered only occasionally and was always less than 2 per cent. If drift was noticed, the hot-wire instrument was reset to 90 per cent of full scale at the reference radius.

The total temperature Kiel probe was set at the angle which was obtained from the flow probe at the particular radius.

For each run, radial survey readings of total temperature, total pressure, velocity head, absolute flow angle, and hot-wire anemometer velocity ratio were taken from the blade tip radius of 18 inches to a distance of 0.2 inches from the hub which has a radius of 10.8 inches. Although readings closer to the hub would have been desirable, the design of the flow probe prevented readings at distances less than 0.2 inches from the hub.

Data were taken at radial increments of 0.5 inches for the majority of the runs. Initially, the increment in radius was chosen as 0.2 inches. However, because of the smooth variation of the flow conditions in the annulus, this increment could be increased to 0.5 inches without loss of accuracy.

Various flow rates were set by means of the discharge throttle valve. The throttle valve position is indicated by means of a digital counter. The counter is calibrated from 0 to 1360 (closed to open). Radial surveys downstream of each rotor row were taken at counter readings of 1000, 900, 800, 700, 600, 500, and 435. Below a counter reading of 435, low rumbling noises and vibrations were observed as well as significant read-out fluctuations, indicating that major portions of the blading were stalled. Peripheral surveys with the flow probe at a counter setting below 435 showed significant flow variations with respect to the peripheral direction. These conditions existed between the hub and approximately mid-blade height. In addition, extreme variation in the hot-wire anemometer reading was noticed also in this region. In some cases, the hot-wire oscillations approached 30 per cent of the instrument read-out. Because of this condition no surveys were made at throttle settings below 435 counts. At a throttle setting of 435 counts, slight fluctuations in the hot-wire anemometer readings were noticed between the hub radius of 10.8 inches and a radius of 12 inches, whereas the flow probe readings were steady in this portion of the annulus.

No flow profiles are presented for readings of the throttle valve counter above 1000, although four such surveys were undertaken. They do not show appreciable differences since the flow rate increases only by about 2 per cent for counter readings between 1000 and 1360.

SECTION 8

DISCUSSION OF RESULTS

8.1 General

For the present study the O.N.R. compressor was run for 68 hours, of which 28 hours were required for the flow rate calibrations.

The tests were conducted with the so-called free-vortex blading of the compressor installed. The rotor blades of all three rotor rows were set at the design stagger angles of 43.8 degrees with respect to the axial direction. All stator blades had stagger angles of 39.8 degrees. The runs were made at the high rotor speed of about 1190 rpm.

8.2 Flow Rate Calibration

The flow rate calibrations were undertaken to verify the calibration factor found by Marshall (5). The fluctuating readings due to atmospheric conditions experienced by Marshall were eliminated by closing the door in front of the compressor inlet duct. It is interesting to note that during the radial surveys downstream of the third rotor, the door to the atmosphere was opened. Even though the atmospheric conditions were calm, fluctuations of up to 10 per cent were noticed in the hot-wire readings. The fluctuations stopped when the door was closed.

Velocity measurements in the inlet duct were made from the centerline to a radius of 17.8 inches. It was not possible to measure the velocities closer than 0.2 inches from the wall. Since the inlet pipe has a diameter of 36 inches, the hot-wire probe had to be supported from both walls to eliminate vibration. Therefore, the probe had to be attached at right angles to the support structure (Fig. 6). The

probe thickness of 1/4 inch and the fillet at the attachment point prevented measurements closer than 0.2 inches from the wall. Velocity measurements to the wall would have been desirable for a more accurate calculation of volume flow rate. In the calculation of volume flow rate, the velocity measured at a radius of 17.8 inches was assumed to be that at the wall also.

8.3 Presentation of Data

The axial velocity profiles obtained from the NISRE solution and from the flow probe and hot-wire measurements are presented in Figs. 12 through 32 in dimensionless form. These quantities were made dimensionless by dividing the velocities by the rotor tip speed. The parameter Φ thus obtained is convenient for two reasons. First, assuming that a mean axial velocity \bar{V}_a exists in the flow annulus, the volume flow rate can be expressed by

$$VF = \bar{V}_a \frac{651.4}{144} \quad (\text{ft}^3/\text{sec}) \quad (32)$$

and the rotor tip speed is

$$U_T = \omega \frac{18}{12} \quad (\text{ft} / \text{sec}) \quad (33)$$

where ω is the angular velocity of the rotor in radians per second.

Thus

$$\bar{\Phi} = \frac{VF}{\omega} \left(\frac{12}{18} \right) \left(\frac{144}{651.4} \right) = \frac{VF}{\omega} (0.1474) \quad (34)$$

Therefore, $\bar{\Phi}$ is a flow coefficient relating volume flow rate to rotor speed. A numerical average of the values of Φ obtained from the radial distribution of axial velocities at a given flow rate gives an average value of $\bar{\Phi}$ which is a measure of the volume flow rate at

a particular throttle setting and rotor speed. Second, the flow coefficient is a convenient parameter for comparing the velocities obtained by the NISRE solution and those measured with the flow probe and the hot-wire anemometer because changes in rotor speed have no influence on Φ .

The total pressures measured with the flow probe downstream of each of the rotors at various flow rates are presented in Figs 33 through 35. These pressures are shown in dimensionless form by the parameter

$$\psi = \frac{P_t - P_a}{\rho_a U_r^2} \quad (35)$$

where the subscript "a" refers to the atmospheric conditions.

The work input of a blading element in an axial-flow compressor can be expressed by the so-called Euler turbine equation. The rise in total temperature from station (1) ahead of to station (2) after the blading is

$$\Delta T_t = \frac{\omega}{C_p g J} (r_2 V_{u_2} - r_1 V_{u_1}) \quad (^\circ R) \quad (36)$$

For a frictionless process of an incompressible fluid, the theoretical rise in total pressure $(\Delta P_t)^*$ then becomes

$$(\Delta P_t)^* = \rho \omega (r_2 V_{u_2} - r_1 V_{u_1}) \quad (\text{psf}) \quad (37)$$

With losses, the pressure rise ΔP_t is

$$\Delta P_t = \eta (\Delta P_t)^* = \rho \omega \eta (r_2 V_{u_2} - r_1 V_{u_1}) \quad (\text{psf}) \quad (38)$$

where η is the stage efficiency. Rewritten

$$\Delta P_t = \rho U_r^2 \eta \left(\frac{U_2}{U_r} \frac{V_{u_2}}{U_r} - \frac{U_1}{U_r} \frac{V_{u_1}}{U_r} \right) \equiv \rho U_r^2 \Psi$$

The so-called pressure coefficient Ψ is therefore a function of the flow angles and the losses only and is independent of the density of the flow and the rotor speed, as long as the influences of Reynolds number and Mach number can be ignored. The aforementioned parameter ψ is suitable for comparing the radial distributions of the total and static pressures measured after the rotors because the influences of varying densities and rotor speeds are eliminated.

Since the present study was not concerned with determining blade losses, no measurements of total pressure were made upstream of the rotors while the radial surveys were conducted downstream of them. Since the surveys after the rotors were conducted on different days, it was not possible to maintain exactly the same value of the average flow coefficient $\bar{\phi}$; hence, the values of ψ presented for the total pressure cannot be used to establish the quantity Ψ defined earlier.

The static pressures calculated by the NISRE method, those measured by the flow probe, and the ones calculated by using the velocity measured by the hot-wire anemometer were made dimensionless by the same method. The dimensionless parameter thus obtained is convenient for comparing the static pressures determined by these different methods because changes of atmospheric pressure, density, and tip speed do not influence the data.

Figures 36 through 56 show the measured values of the absolute flow angles α obtained for all runs.

8.4 Accuracy of the NISRE Method

Figures 12 through 32 show very good agreement between the velocity profiles calculated by the NISRE method and those measured by the flow probe and hot-wire anemometer. The agreement is good downstream of all rotors through the range of flow rates, with the possible exception of

Fig. 24. This figure shows axial velocity profiles obtained after the second stage rotor at a flow rate of 22.85 lbm/sec corresponding to a discharge throttle valve counter setting of 500. This run was repeated to check the results; but for both runs they were almost identical. The calculated velocities differ from the measured ones by as much as 7.5 per cent at radius ratios R/R_0 of 0.67 and 0.9. No obvious explanation could be found for this deviation from the otherwise close agreement between the calculated and measured data.

Figures 57 through 77 show the comparison of the static pressures obtained from the three methods. This is not an independent comparison since these pressures are dependent on the velocities also. With the flow probe, the static pressures were measured directly, but for the NISRE calculation and hot-wire measurement, the static pressures were calculated by using Eqs. 11, 17, and 19. However, good agreement has been obtained with the three methods.

8.5 Blockage Factor

The value of the gross weight flow blockage factor to be used with the NISRE method has a large influence on the results. Reference 2 suggests a blockage factor of 0.98 for the first stage and 0.96 for all subsequent stages.

Blockage factors of 0.96 for the second and third stage rotors gave the results of Figs. 19 through 32. Blockage factors of 0.98 were first tried for the calculations of the velocity profiles for the first stage rotor but gave velocities well below those measured by the flow probe and the hot-wire anemometer. The effect of the area blockage by the wall boundary layers was then increased by changing the blockage factor to 0.97

and finally to 0.96. This increase in area blockage did not materially change the shape of the calculated profiles but increased the magnitudes of the velocities. Blockage factors of 0.96 for the first rotor gave the best correlation between the axial velocities calculated by the NISRE method and those measured. Figures 12 through 18 show the axial velocity profiles after the first rotor for this value. It is believed that the requirement for a smaller blockage factor after the first rotor is caused by the boundary layer build-up along the walls of the inlet duct which has a length of six feet.

8.6 Compressor Design Point

As stated in subsection 8.1, the tests were conducted with the so-called free-vortex blading of the compressor. At their design point, such bladings are supposed to produce flow patterns where the product of the radius r and the peripheral component V_u of the absolute velocity remain constant in the radial direction after each row of blades. If entropy gradients are ignored, free-vortex flows have constant total pressure P_t , constant total temperature T_t , and constant axial velocity components V_a between the rows of blades. However, if entropy gradients occur even though total temperatures do not change in the radial direction, the axial velocity components of the absolute velocity are not constant. Equation 3, without the term involving meridional streamline curvature, can be expressed also by

$$J_g C_p \frac{\partial T_t}{\partial r} = J_g T \frac{\partial s}{\partial r} + \frac{V}{r} \frac{\partial (r V_u)}{\partial r} + V_a \frac{\partial V_a}{\partial r}$$

Hence, if the product rV_u were constant in the radial direction, the term containing V_u would be zero. If the total temperature were also constant in the radial direction, the only terms remaining are those involving entropy and axial velocity component. This indicates that with the aforementioned assumptions, the variations of the axial velocity components are a function of the entropy gradients and the static temperatures.

From the presented data it can be noticed that neither constant velocities V_a nor constant total pressures P_t were reached with the installed blading, irrespective of flow rate. In Ref. 3, the design stagger angle of the stator blades is given as 29.8 degrees. Hence, since a value of 39.8 degrees was used for the present tests, it is likely that radial changes in V_a and P_t were due to this condition.

All the axial velocity profiles calculated by the NISRE method show regions of increased axial velocities at radius ratios R/R_0 of about 0.67 and 0.90. At which of these two stations the maximum velocity occurs depends on the flow rate. As flow rate decreases, the region of highest velocity moves from the inner to the outer part of the annulus. The measured velocity profiles show the same trend but are generally flatter. The crossover point, where the maximum velocity at both regions has about the same magnitude, occurs at a flow rate of about 26.5 lbm/sec, as shown in Figs. 12, 14, 15, 22, and 29. To this flow rate corresponds a flow coefficient $\overline{\Phi}$ of about 0.44, which is the average of the flow coefficients obtained from the calculated and measured axial velocity profiles presented in the abovementioned figures. Except for the regions near the hub and the tip, the axial velocity is nearly constant at this flow rate. Further evidence that the design criteria of a free-vortex

flow were most nearly met at a $\overline{\Phi}$ of 0.44 is given in Figs. 33 through 35, where it is shown that total pressure is nearly constant except for the hub and tip regions. However, this uniformity is not so well realized after the second and third stage rotor. For this discussion it is of interest to note that Ref. 4 gives a design value of $\overline{\Phi}$ of 0.45 for the free-vortex blading at rotor and stator stagger angles of 43.8 and 29.8 degrees respectively.

Reduced total pressures and low axial velocities occur in the regions near the hub and near the outer casing downstream of all rotor rows. They are caused by end and tip clearance losses, by the wall boundary layers, and by the effect of the rotating hub. These conditions produce large entropy gradients at the inner and outer radii of the annulus for the reason shown in the explanation of Eq. 3 in this subsection. Their effect near the hub extends from radius ratios of 0.6 at the hub to about 0.64 for the first rotor, 0.66 for the second rotor, and 0.69 for the third rotor. Near the outer casing, they influence the velocity distributions at radius ratios of about 0.91 after the first rotor and about 0.94 after the second and third rotor. The regions which are affected by the hub and tip losses become larger as the fluid proceeds downstream since the losses accumulate from stage to stage and further deteriorate the flow profiles.

The velocities at the outer casing are difficult to measure. Since the probes extended into the flow annulus from the outer casing, radial position changes of the probes of the order of 0.01 inches at the outer radius caused changes in the measured data of up to 40 per cent. It is believed that these discrepancies were caused by small errors in the probe

position indication. The probes retract into the radial access holes, and small changes in radial position cause the access holes to block the measuring holes of the probes.

SECTION 9

CONCLUSIONS AND RECOMMENDATIONS

The accurate determination of the radial distribution of absolute velocity in magnitude and direction is important for the evaluation of the performance of turbomachines. If these distributions were known, the velocity triangles would be completely determined. Knowledge of the velocity triangles allows direct comparison between the applied design criteria and the actual results for a turbomachine.

The accurate predictions of these velocity triangles is of particular importance in the design of multi-stage axial-flow machines. With the exception of the first stage, the inlet conditions of a given stage are the discharge conditions of the preceding stage. If a stage has inlet conditions different from those for which it was designed, its performance is likely to be marginal and could produce discharge conditions that deviate even more from the design values. The result is that the machine will not be able to handle the desired enthalpy change at the expected level of efficiency. The radial distributions of losses and flow deflections in a row of blades are a function of inlet conditions as well as the design of the blades. A blade element designed for a certain range of flow incidence angles, but operating outside of this range, may either stall or not develop the required blade forces, depending on whether the incidence angle is too large or too small. Optimum design of multi-stage axial-flow machines therefore requires that the discharge conditions of any stage match the design inlet conditions of the following stage.

Since designs of turbomachines are based on the results of experimental

work and the experience of the designer, checking the results of new designs is important for two reasons: first, to evaluate the performance of a new design, and second, to improve the design procedures for future machines.

The NISRE method represents a fairly accurate and simple method for determining the velocity profile downstream of an axial-flow rotor. The data which are required can be obtained by small and accurate probes in the vaneless space between blade rows with small axial clearance. The method as presented in this study is limited by the fact that the effect of meridional streamline curvature is ignored. For designs where the curvatures of the meridional streamlines are appreciable, the computing process could be improved in the manner carried out by Harrison (2).

Further experimentation seems necessary to accurately predict the gross weight flow blockage factors, particularly with machines having many stages. The blockage factors used for the velocity profiles after the first rotor were determined by arbitrary variation until accurate matching with the measured profiles were obtained. By changing the length of the inlet duct of the O.N.R. compressor the effect of boundary layer growth on blockage factors could be investigated.

The hot-wire anemometer was not used for an analysis of the unsteady flow in the passages downstream of the rotors. The presented average velocities were read on an instrument which heavily damps the signal and cannot follow the high frequency response of the hot-wire anemometer which is up to 50 kilohertz. However, some oscilloscope traces were photographed downstream of the second rotor. Sample pictures of these oscillograms, with the hot-wire probe at a radius of 13 inches, are presented in Fig. 78. The oscillogram marked (a) was made with the throttle

valve open, and the oscillogram marked (g) was made at a throttle valve counter setting of 425. The measured flow rates are indicated in the figures. The time for successive blades to pass by the hot-wire is 1.675 milliseconds, corresponding to a frequency of about 0.6 kilohertz which is well within the frequency response of the hot-wire anemometer. Therefore, the hot-wire probe will be able to measure the flow conditions in the wakes between neighboring blades.

The low signal amplitudes in Fig. 78, which are marked by arrows, were found to have the time interval of 1.675 milliseconds. Hence, they are caused by blade wakes. The trace of the hot-wire output moves from left to right on the oscillograms. Hence, the wakes start on the concave side of the blade profiles and end on the convex side of the profiles. Therefore, the flow profiles from left to right between the indicated wakes start from the pressure side of one blade and extend to the suction side of the neighboring blade.

An interesting phenomenon occurs in the oscilloscope traces at a flow rate of 19.26 lbm/sec which is evident from the oscillogram marked (g). An additional trace of lesser intensity but greater amplitude is superimposed on the aforementioned wake pattern. This pattern is periodic in nature and seems to be an indication of the propagating stall discussed by Iura and Rannie (7).

If the resolution of the oscilloscope traces could be improved or if the hot-wire signal were recorded on magnetic tape and transferred to a strip chart recorder, the wake pattern of the flow profiles could be analyzed in greater detail to detect incipient stall conditions. Using instrumentation of this type, it seems feasible to apply the momentum theorem to determine the losses associated with either different blade

shapes or various stagger angles of a given set of blades. The O.N.R. compressor is suitable for such studies since it is possible to vary rotor stagger angles and to install different types of blades. Such a study would require accurate calibrations of the hot-wire probes to enable measurements of velocity in absolute values rather than as ratios with a known velocity. A test rig is now being designed at the Naval Postgraduate School for such calibrations.

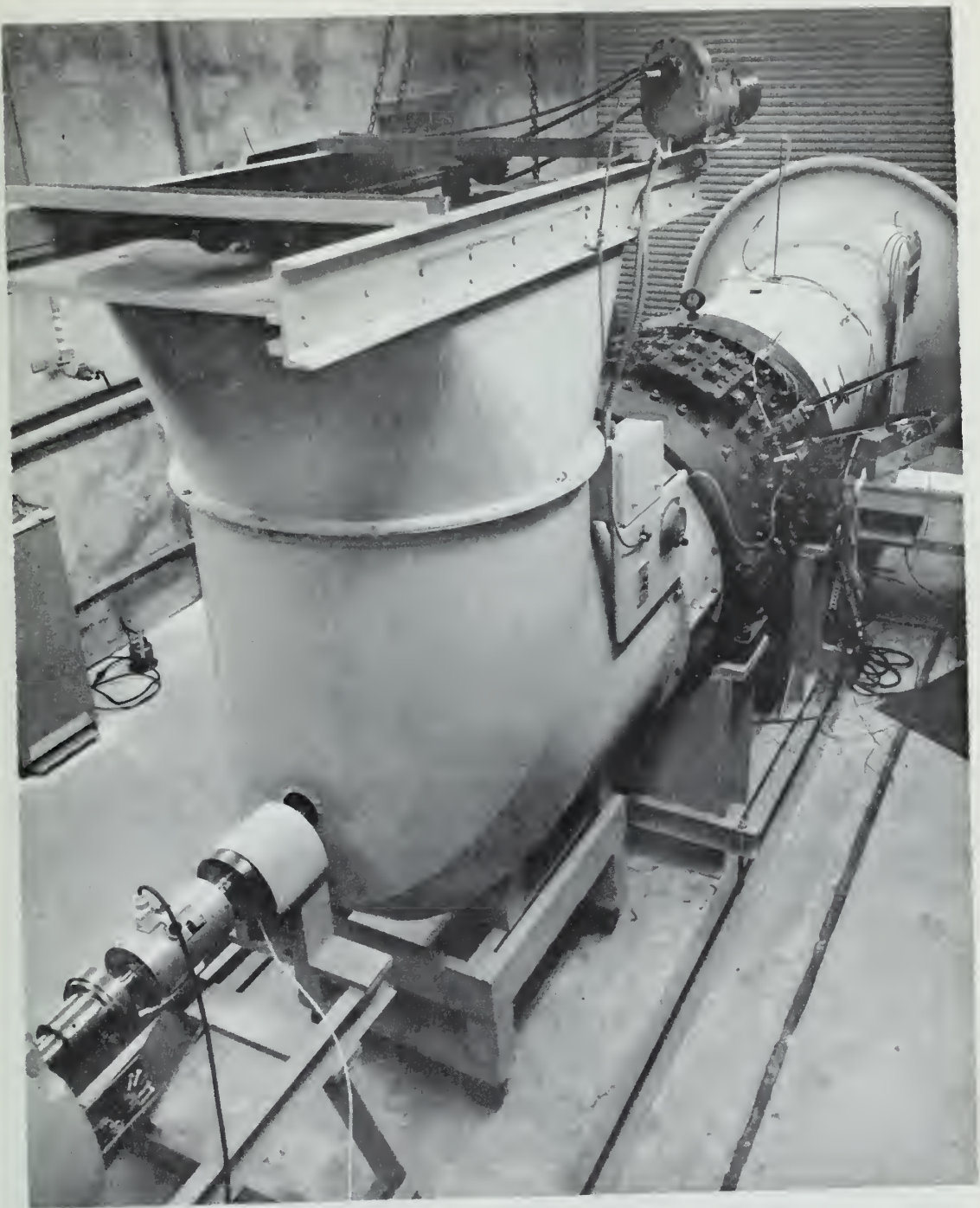


FIGURE 1
COMPRESSOR INSTALLATION

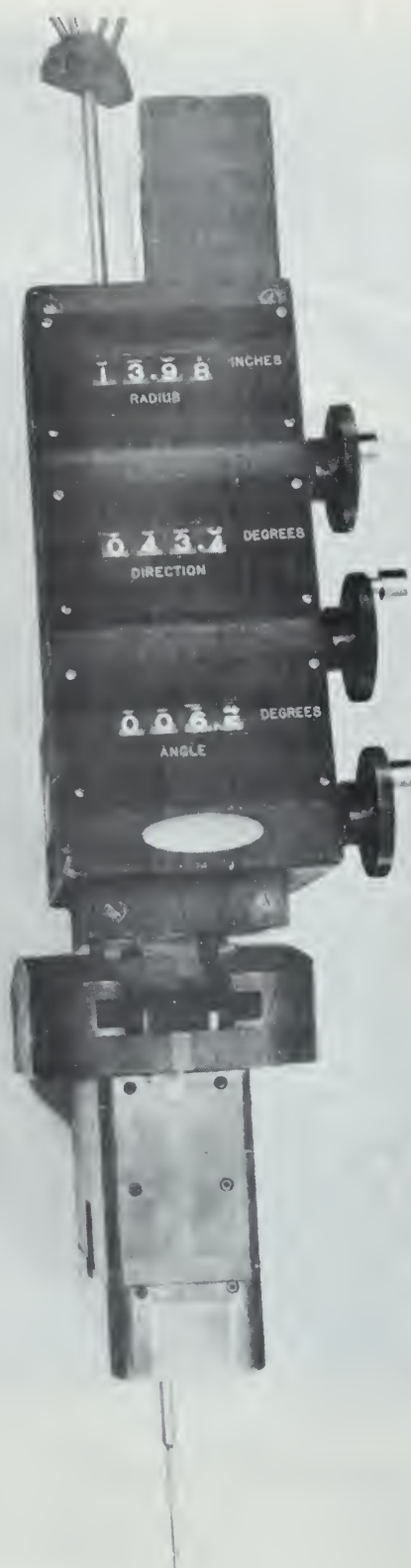


FIGURE 2
DETAIL OF FLOW PROBE CARRIAGE



FIGURE 3
COMPRESSOR INLET DUCT



FIGURE 4
COMPRESSOR INLET WITH INSTALLED FLOW RATE SURVEY INSTRUMENTS

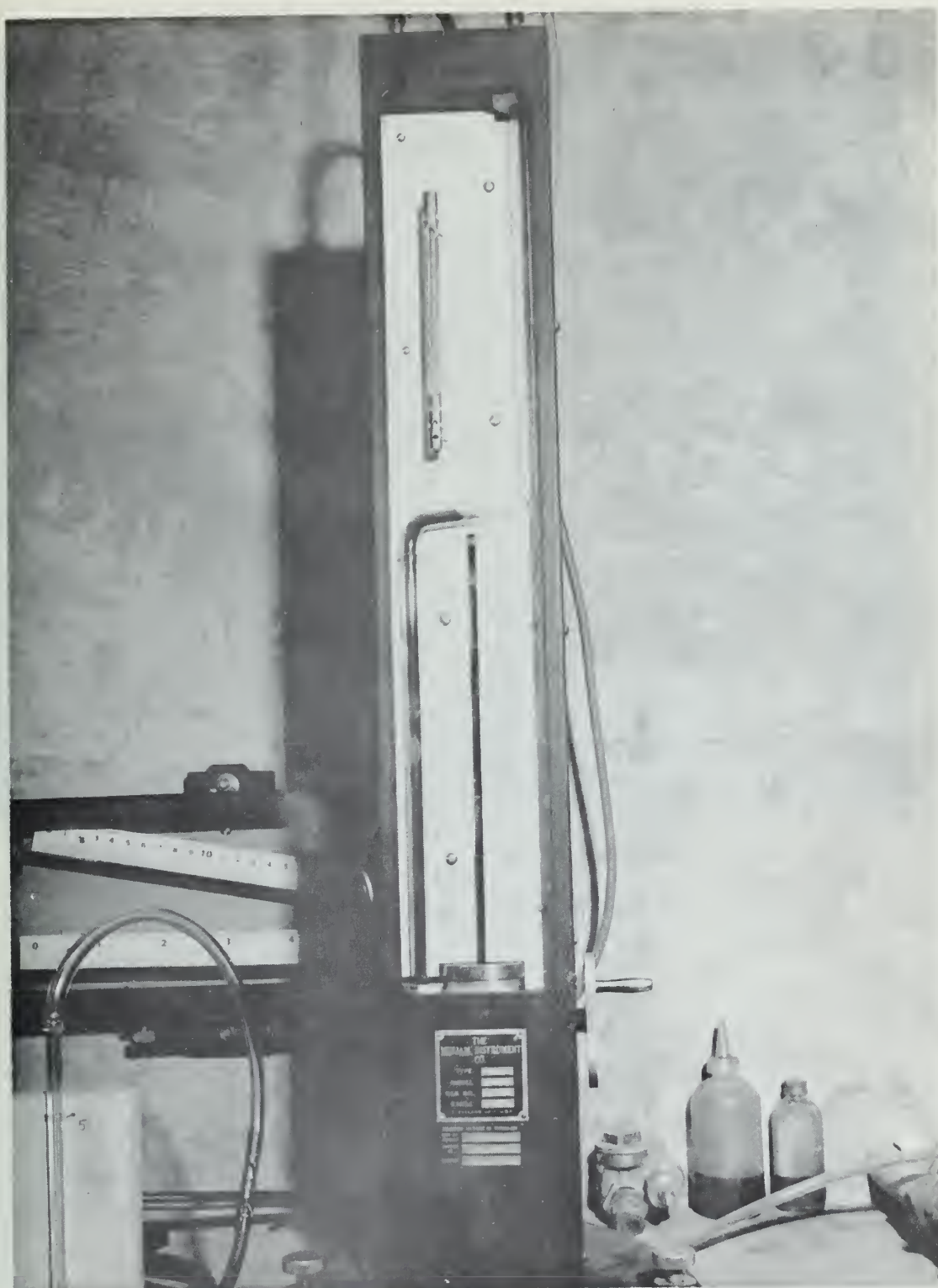


FIGURE 5
MICROMANOMETER

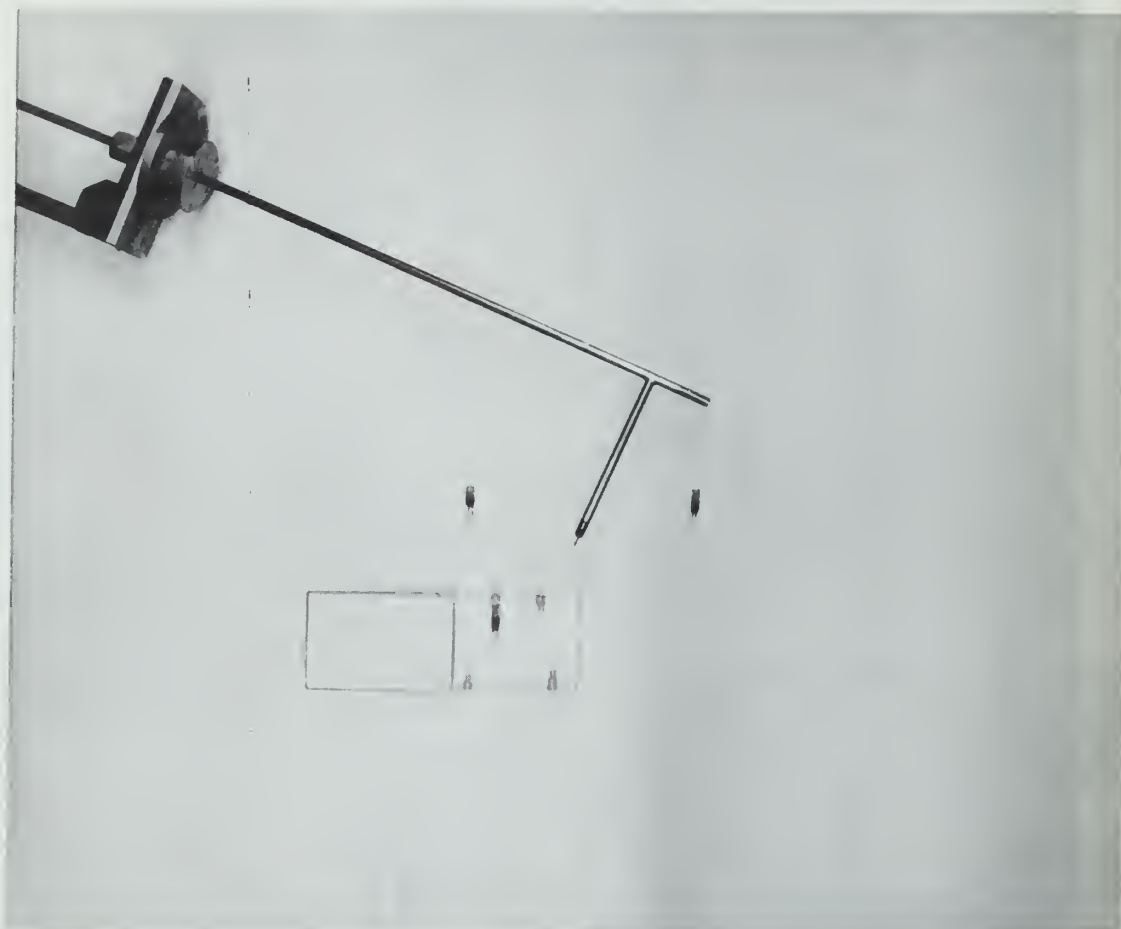


FIGURE 6
DETAIL OF INLET HOT-WIRE ANEMOMETER PROBE



FIGURE 1
 A. 100% OF THE TURBINE, 100% OF THE TURBINE, AND TURBINE
 100% OF THE TURBINE, 100% OF THE TURBINE, 100% OF THE TURBINE



FIGURE 8
PRESSURE SCANNER VALVES AND CONTROLLERS

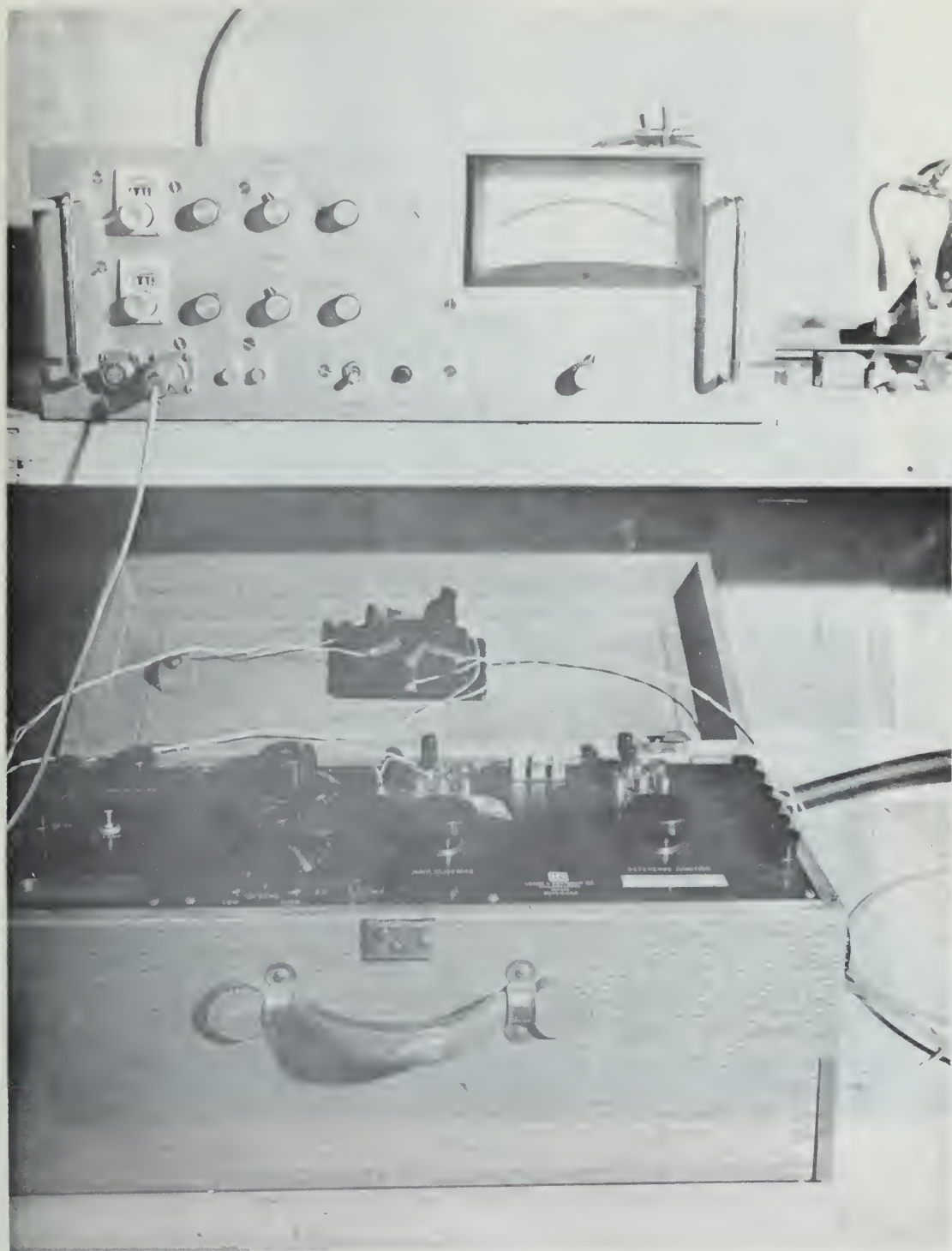


FIGURE 9
HOT-WIRE ANEMOMETER INSTRUMENT READOUT
AND THERMOCOUPLE READOUT

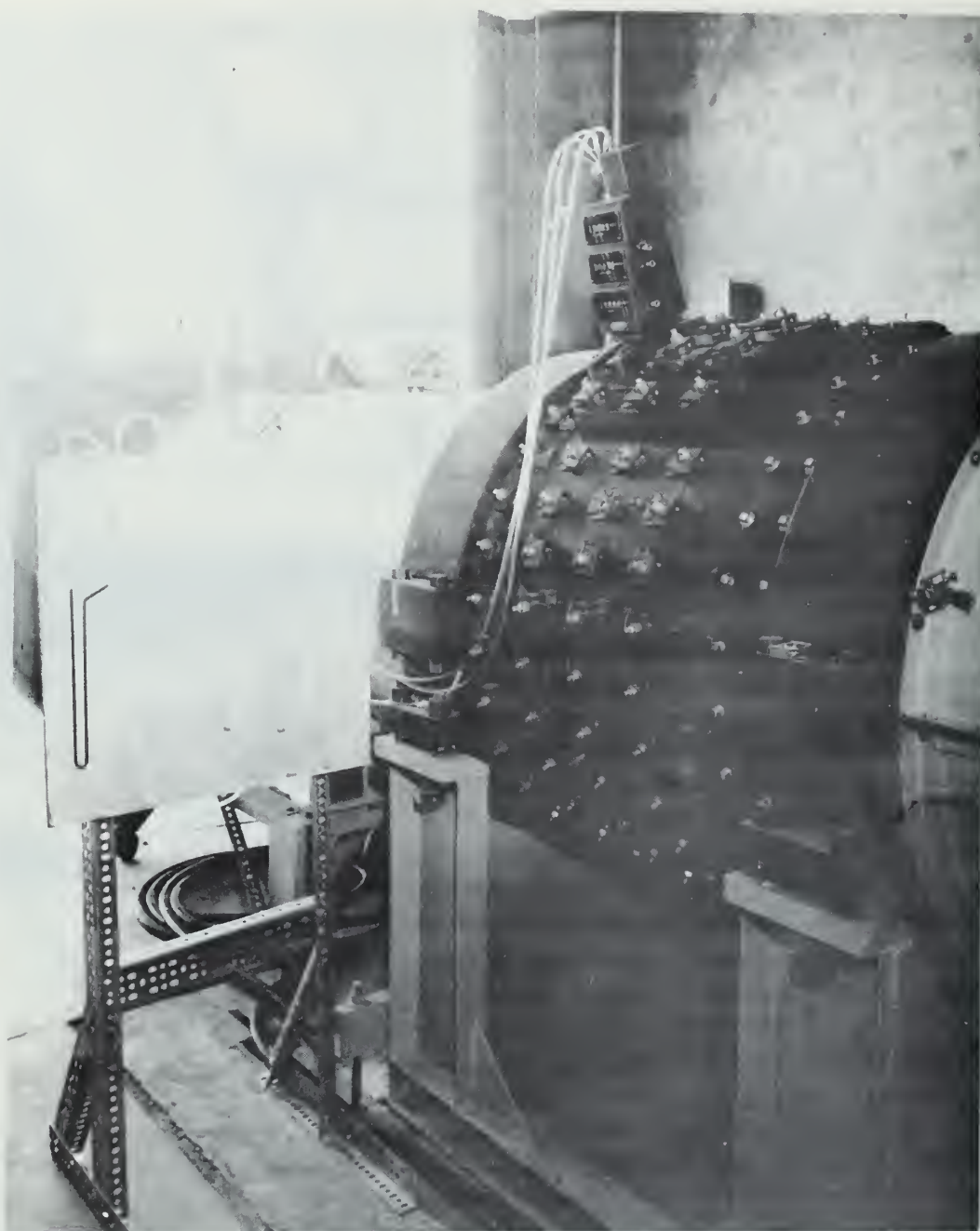


FIGURE 10
VIEW OF COMPRESSOR SHOWING FLOW PROBE CARRIAGE
INSTALLED AND ASSOCIATED MANOMETER BOARD

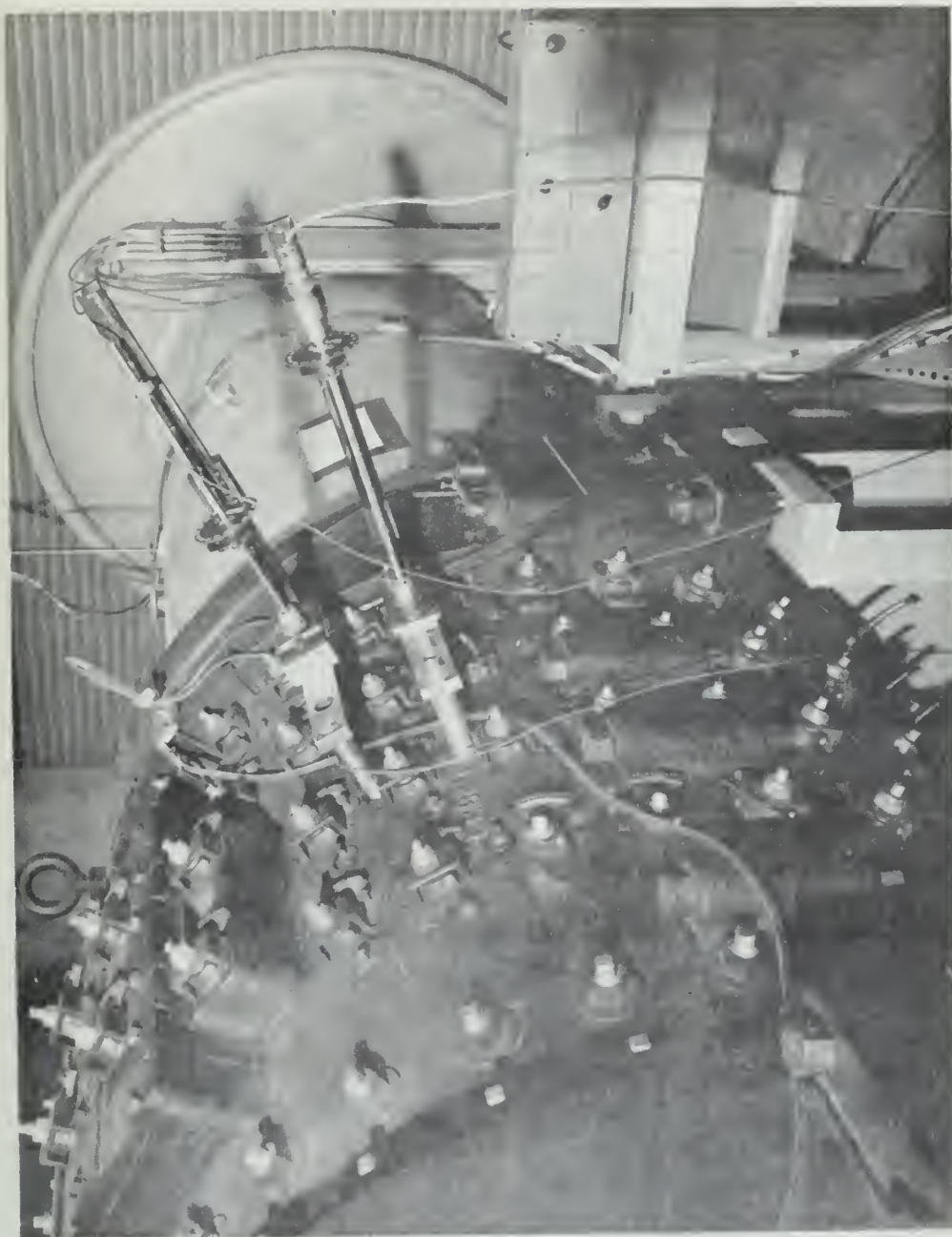
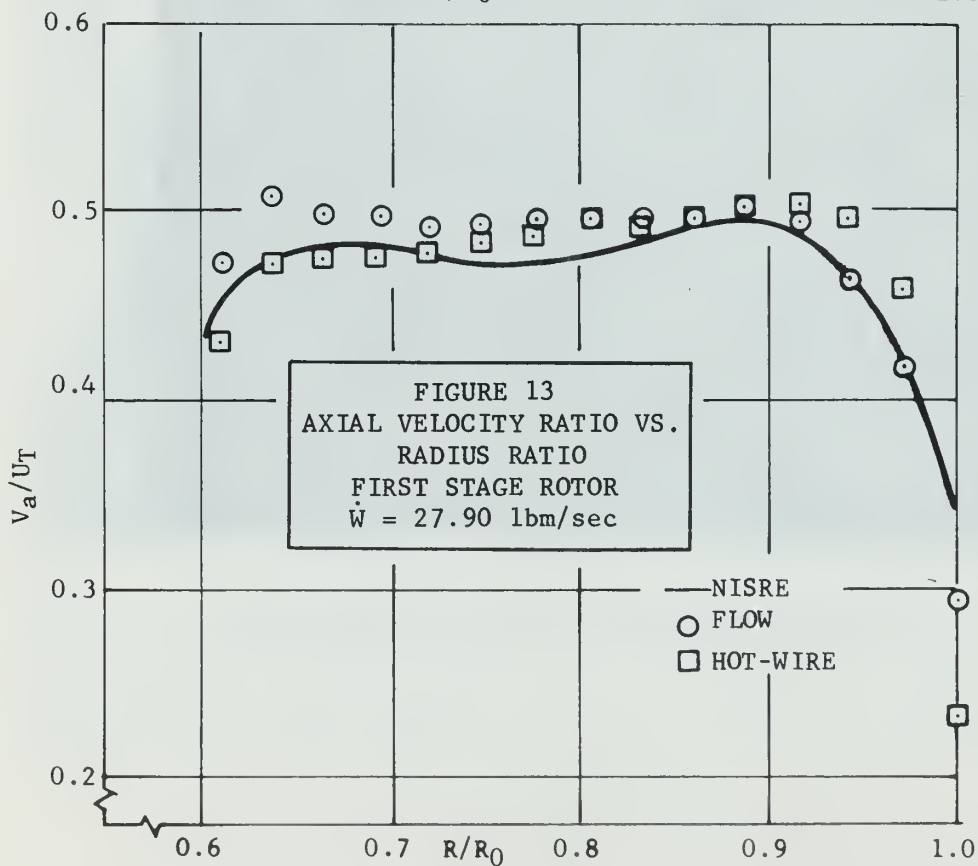
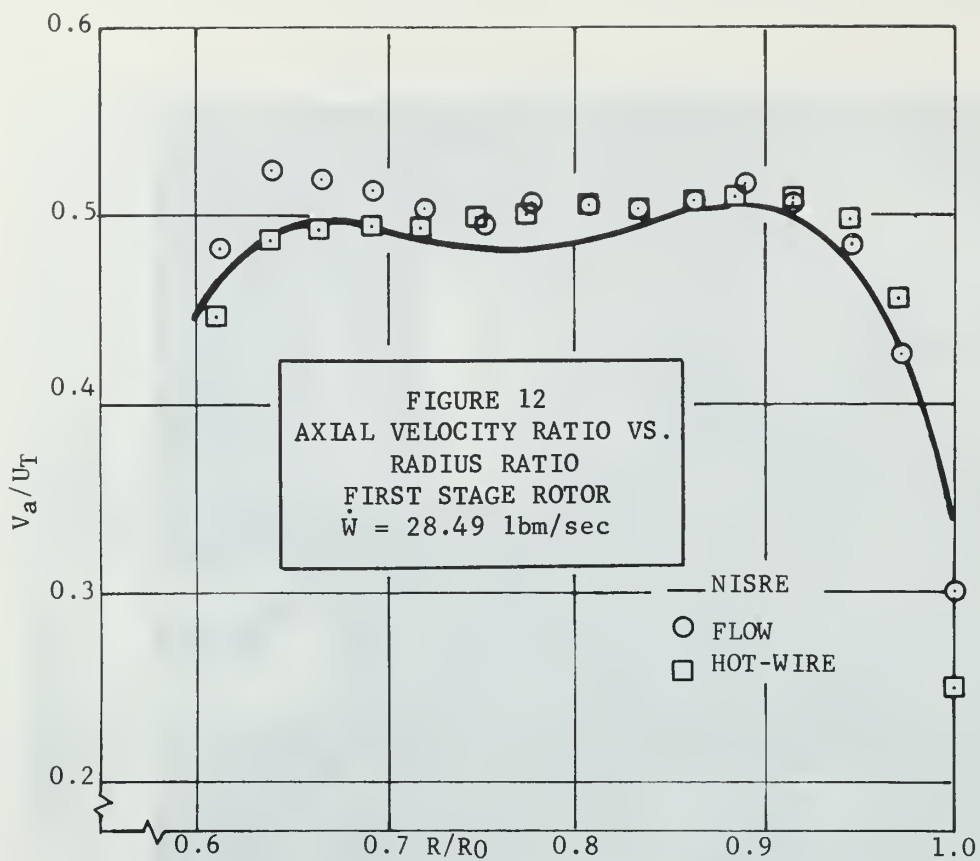
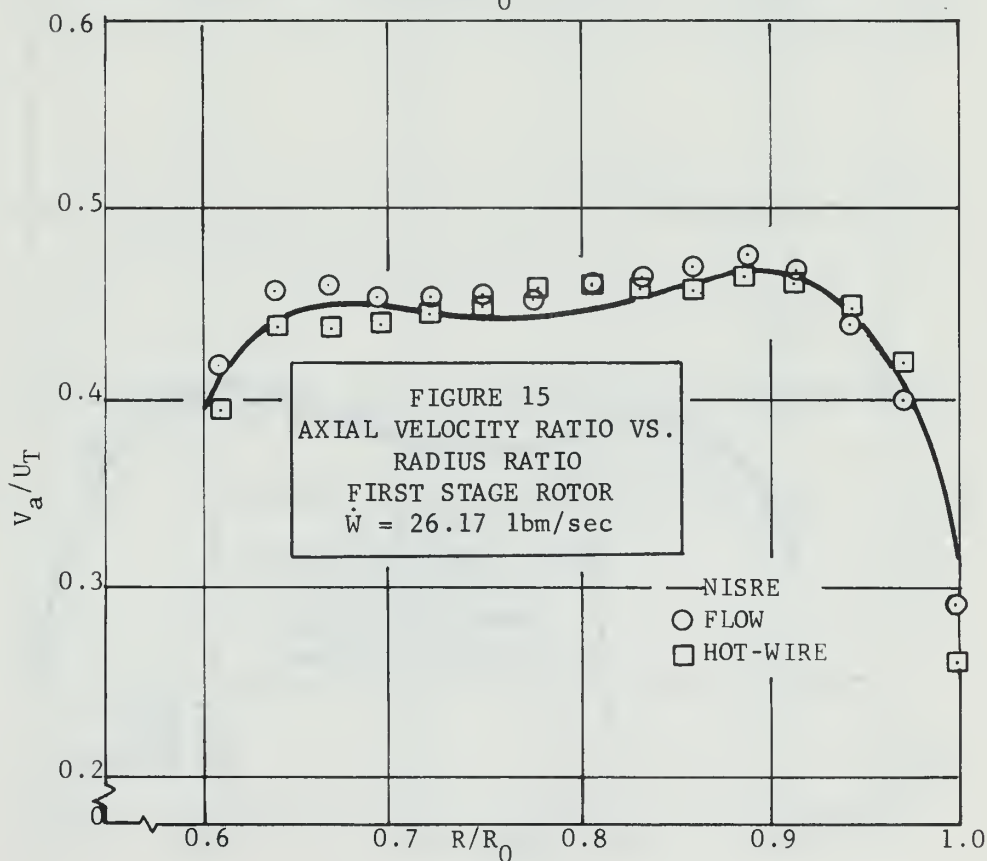
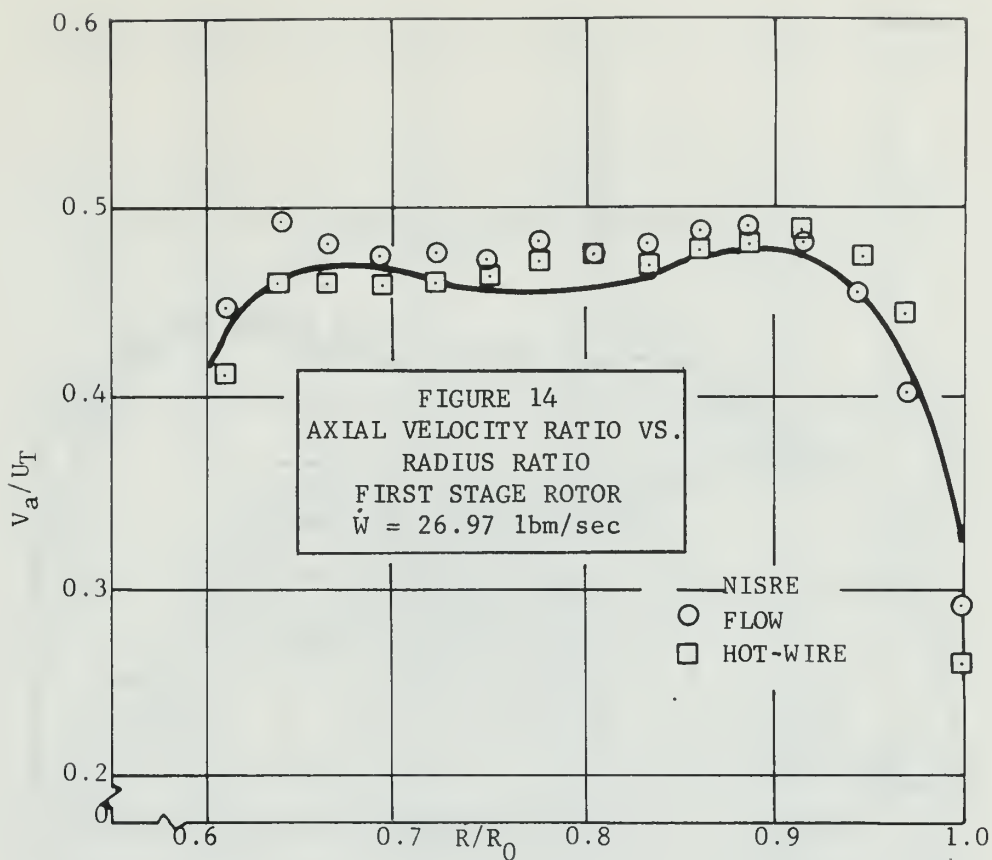
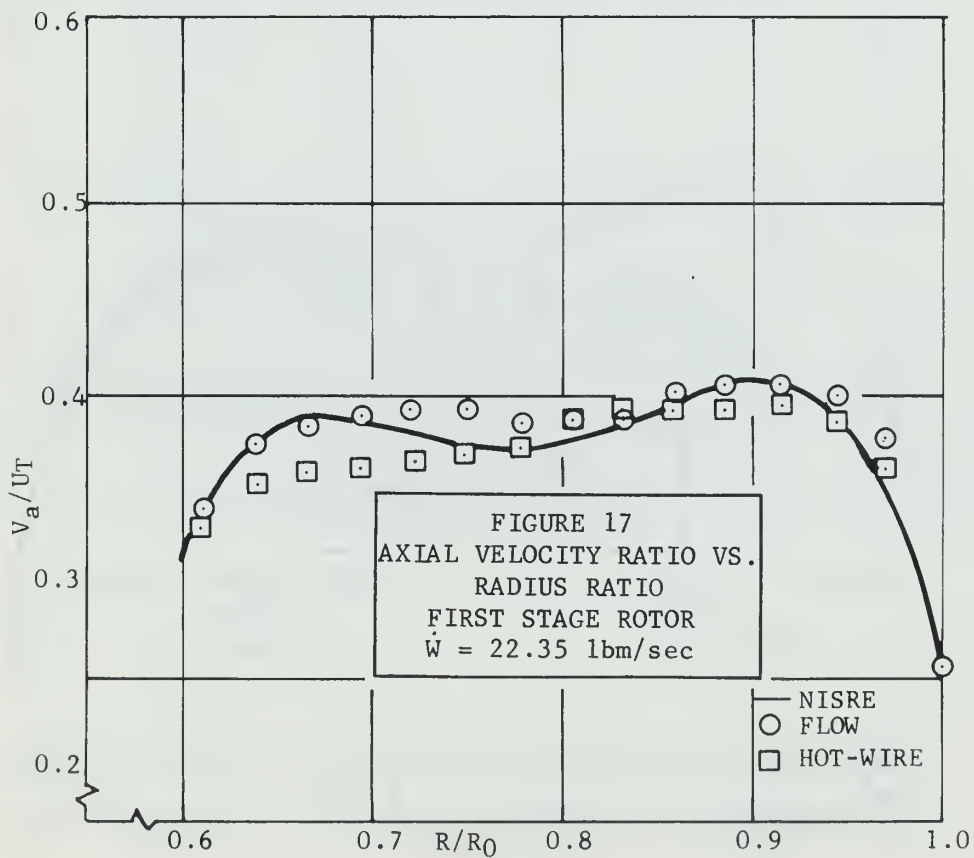
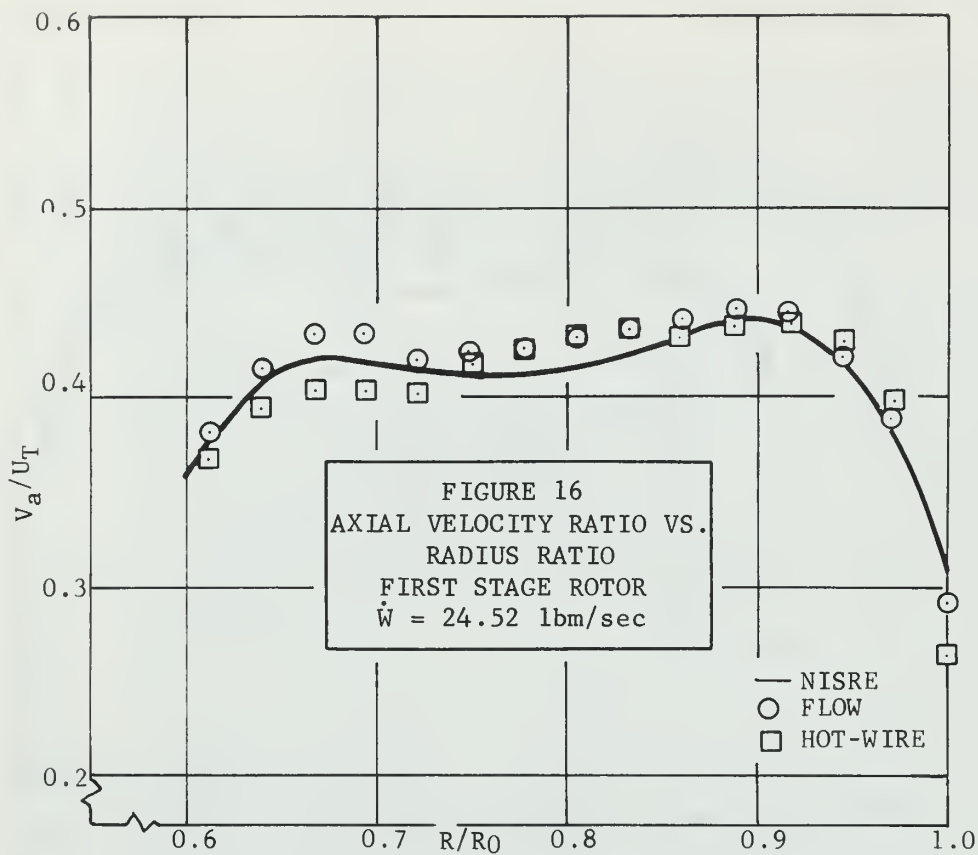
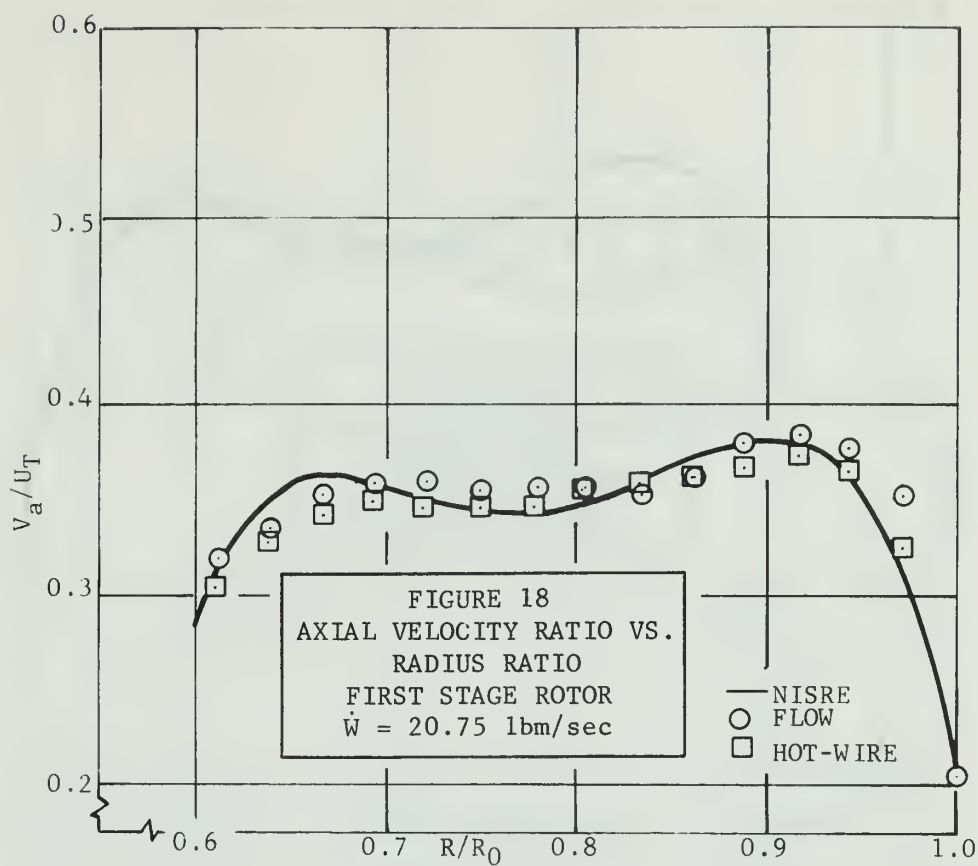


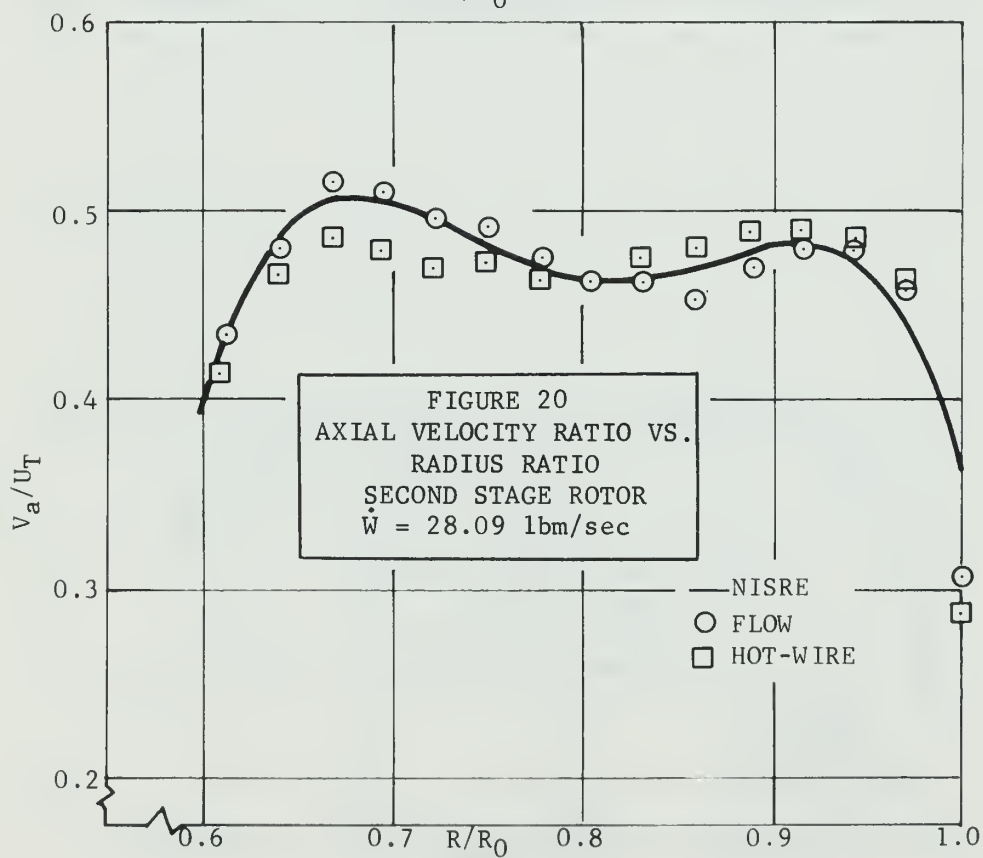
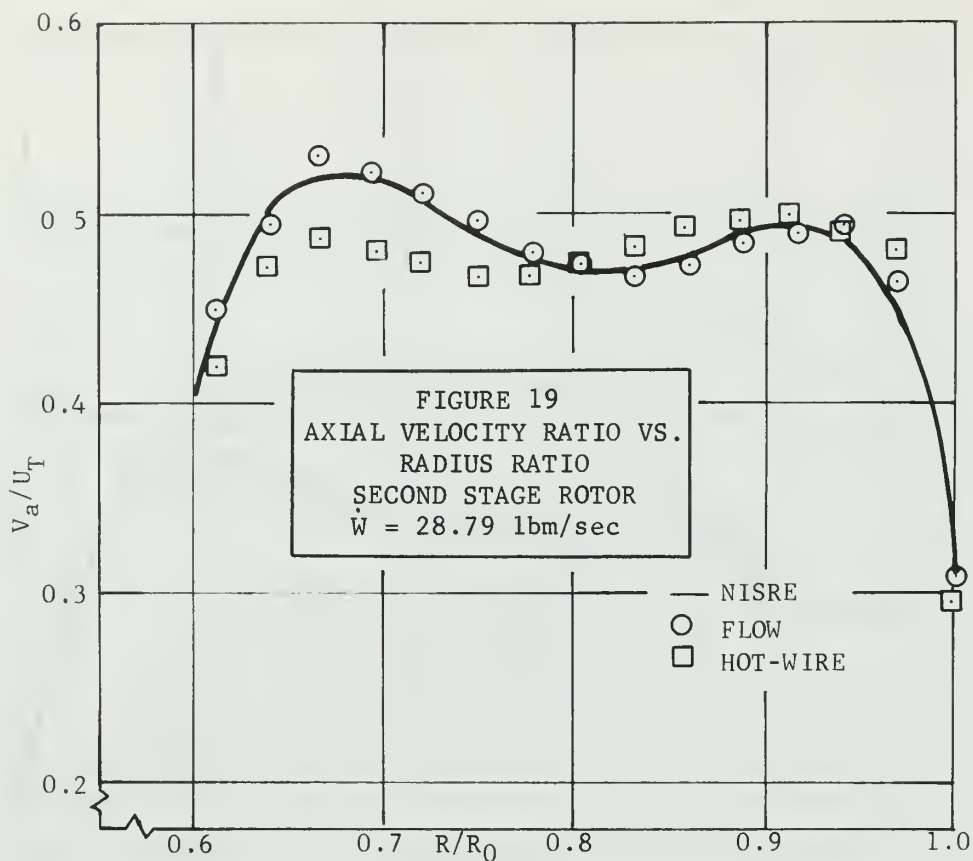
FIGURE 11
VIEW OF COMPRESSOR SHOWING HOT-WIRE ANEMOMETER
AND TOTAL TEMPERATURE PROBES INSTALLED

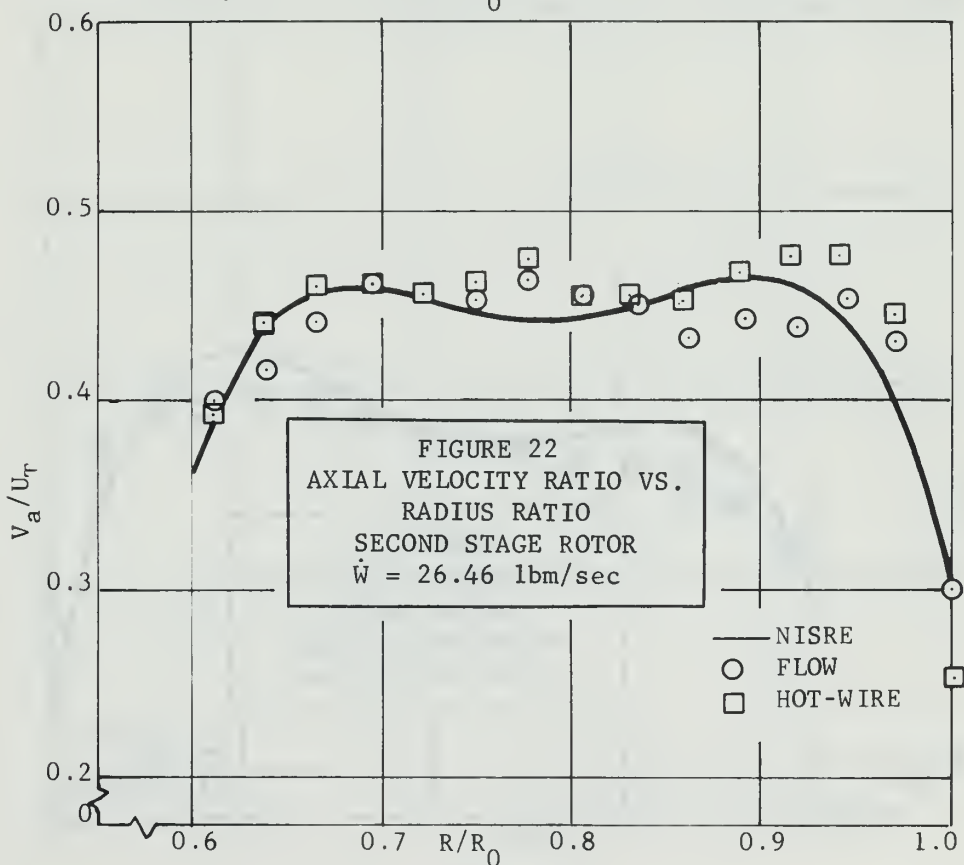
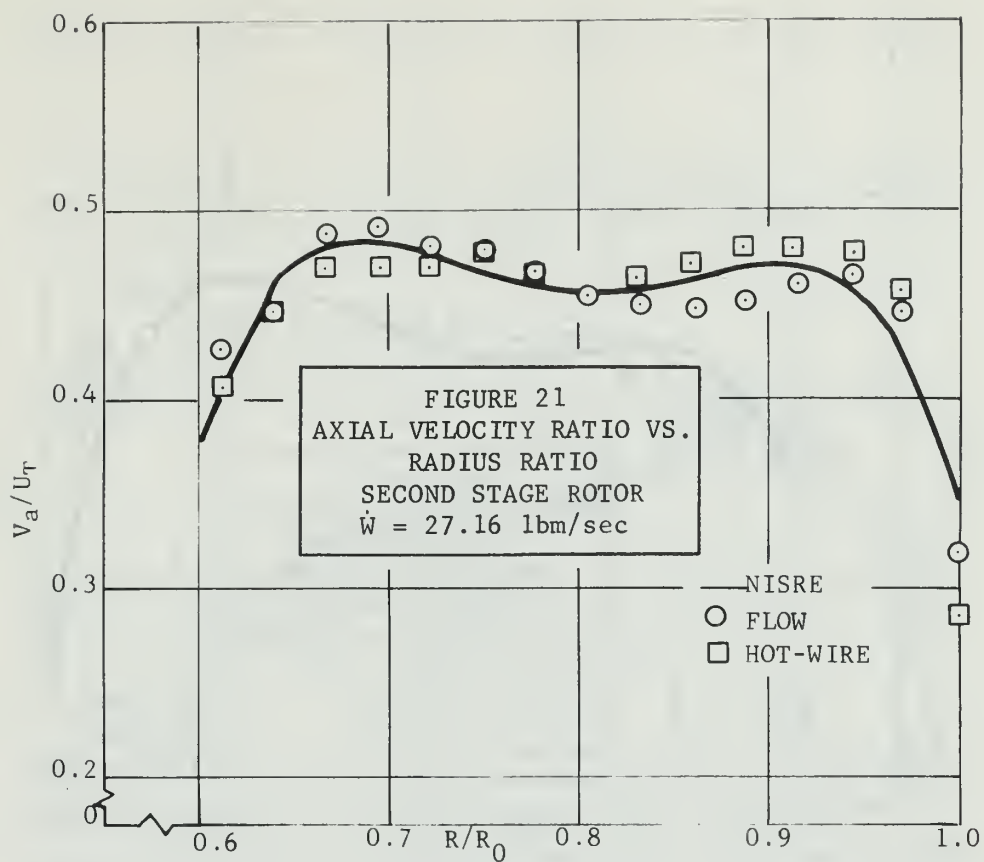


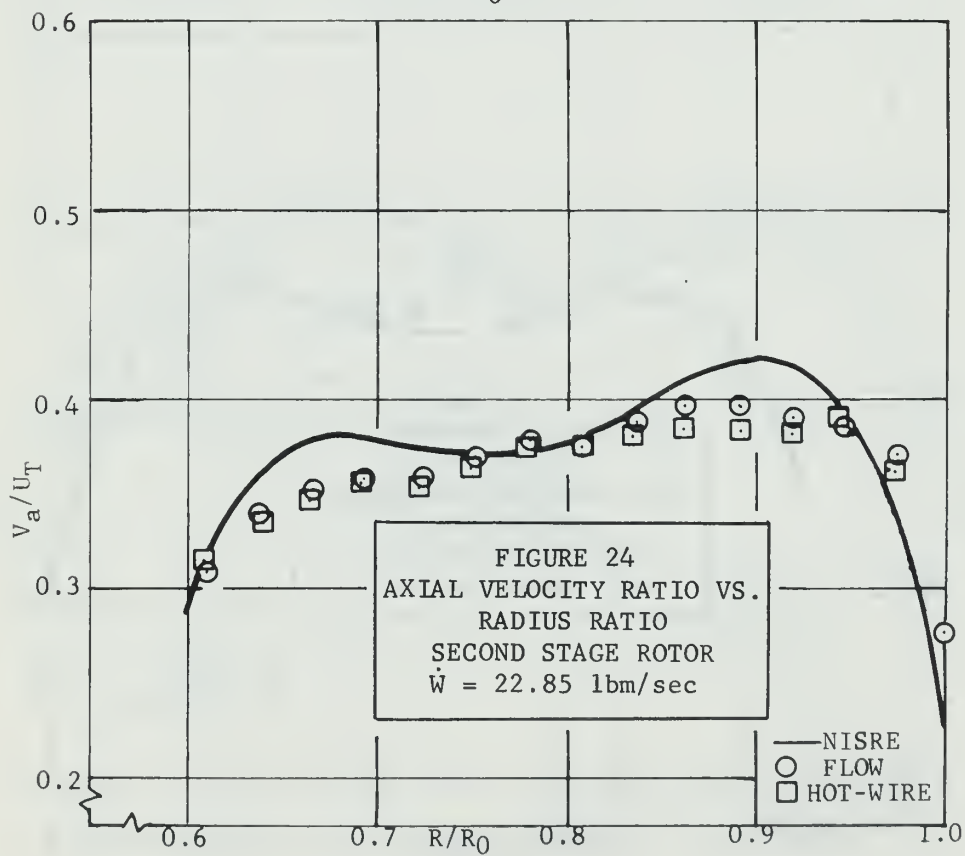
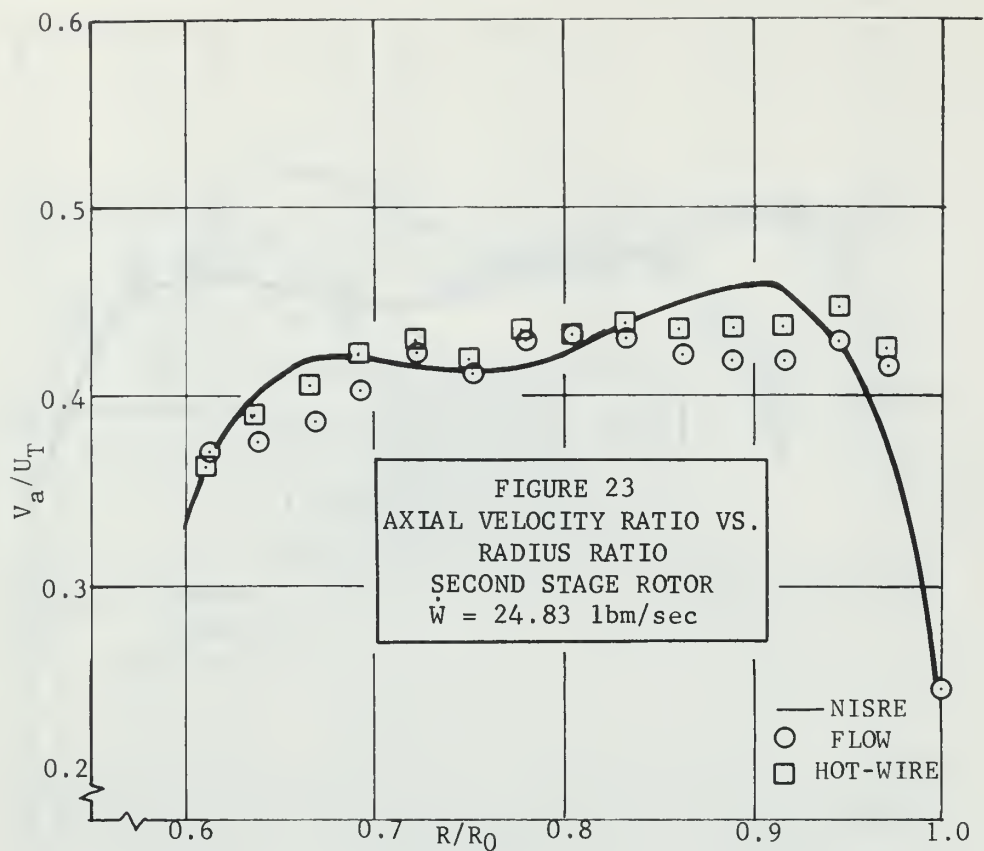


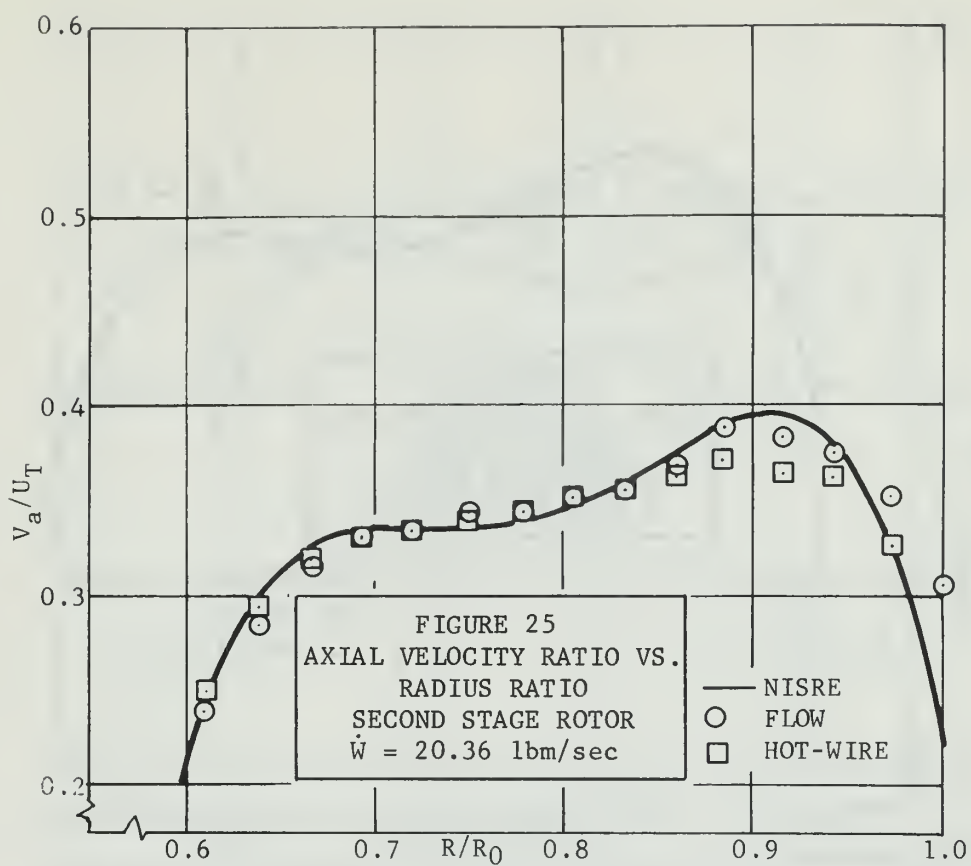


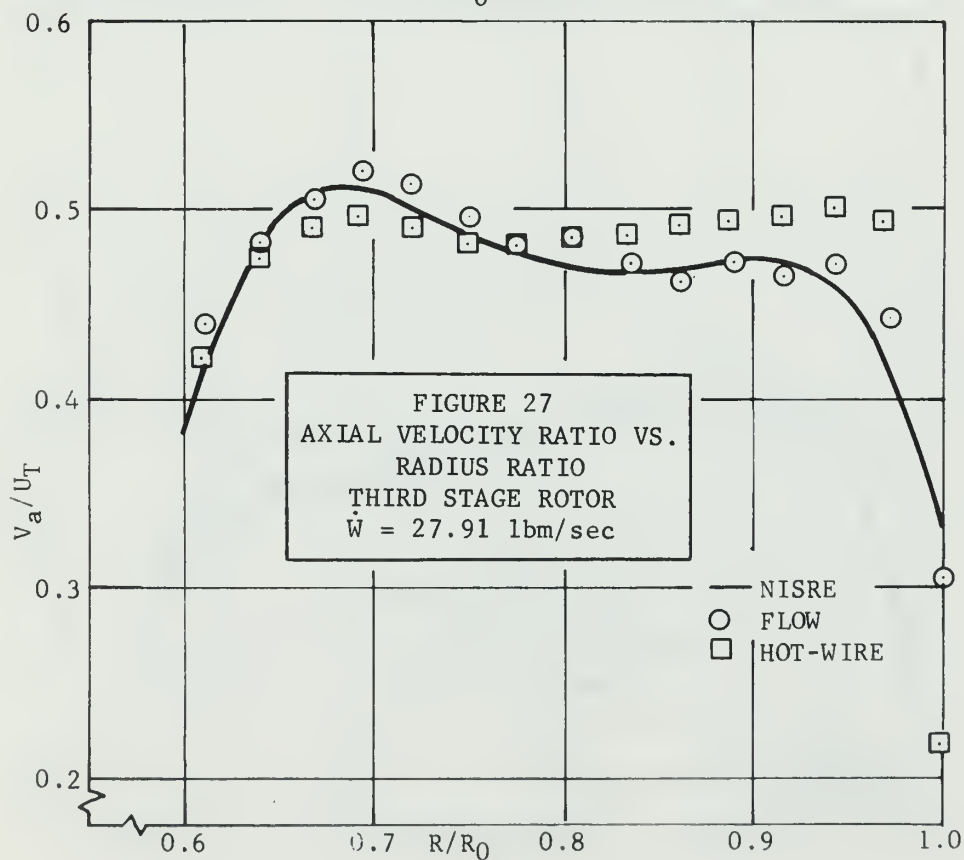
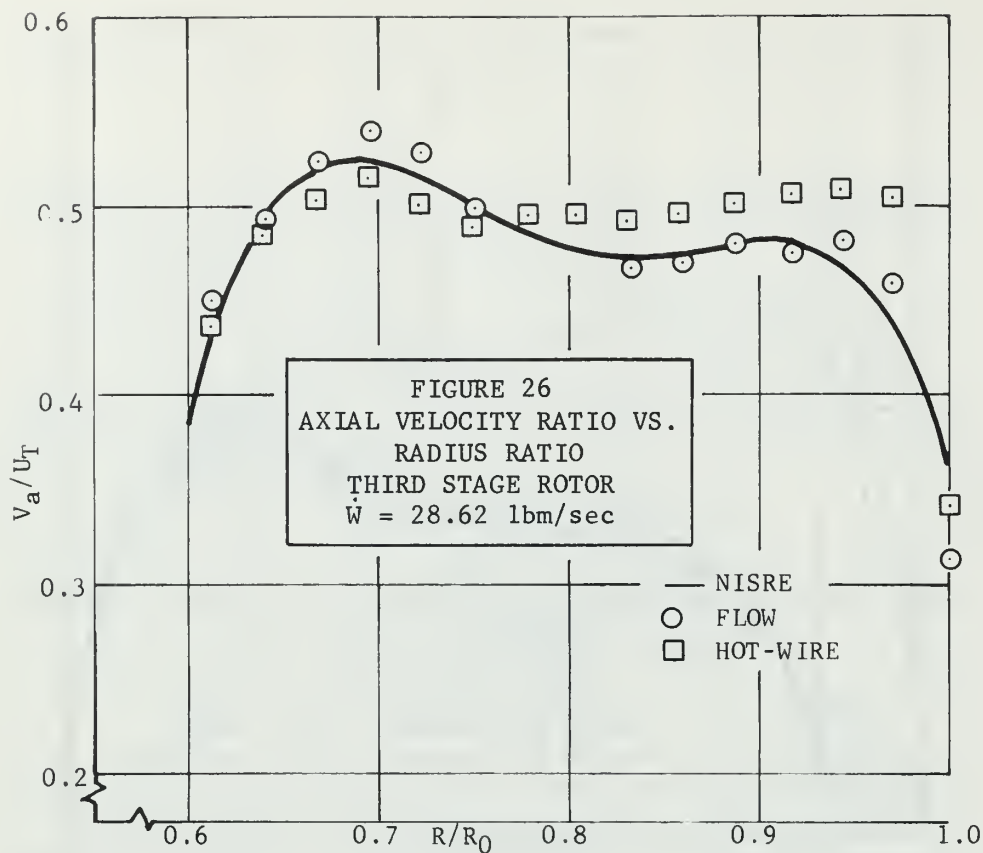


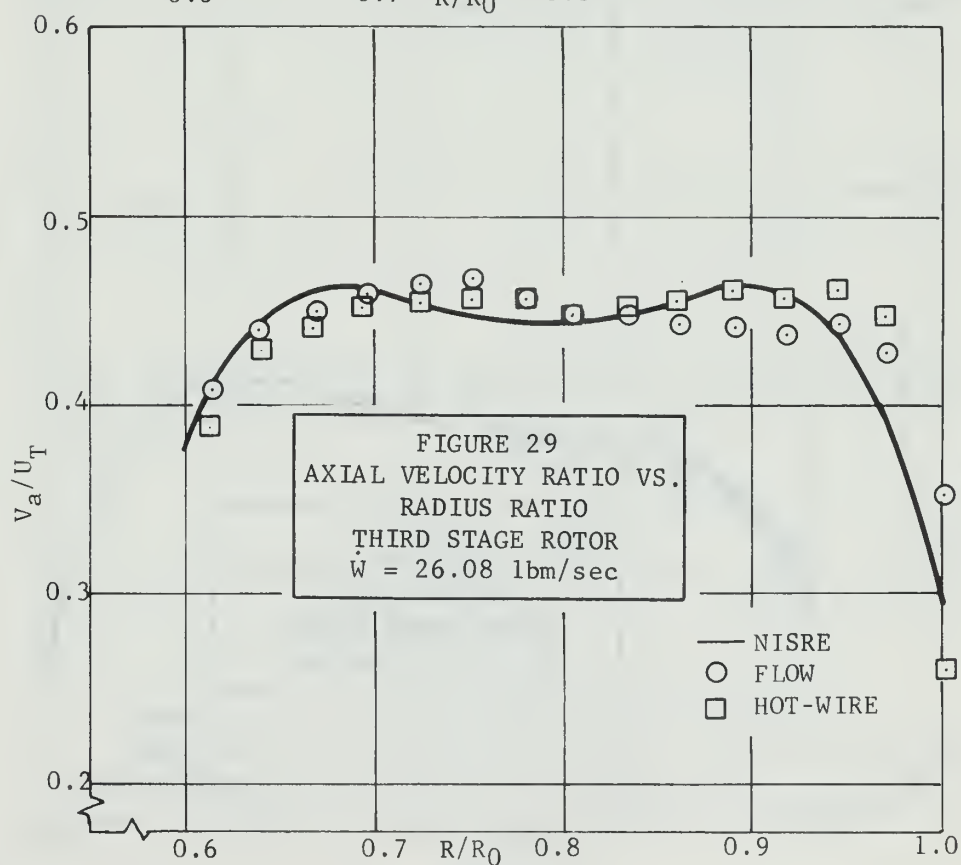
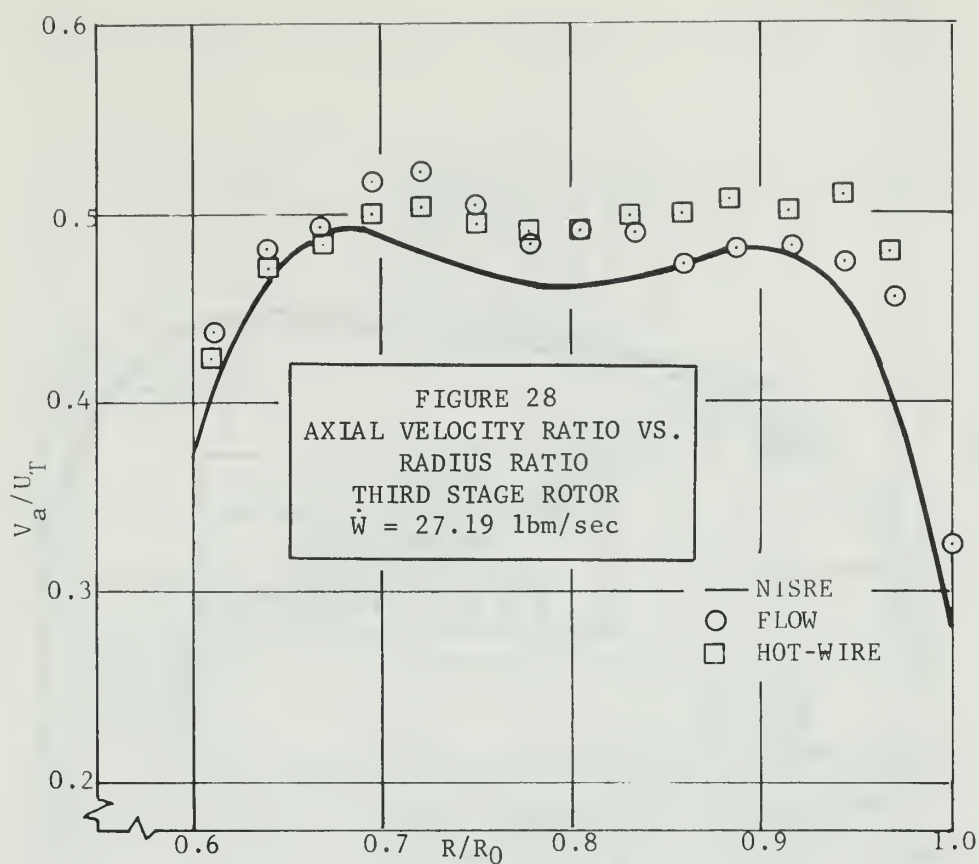


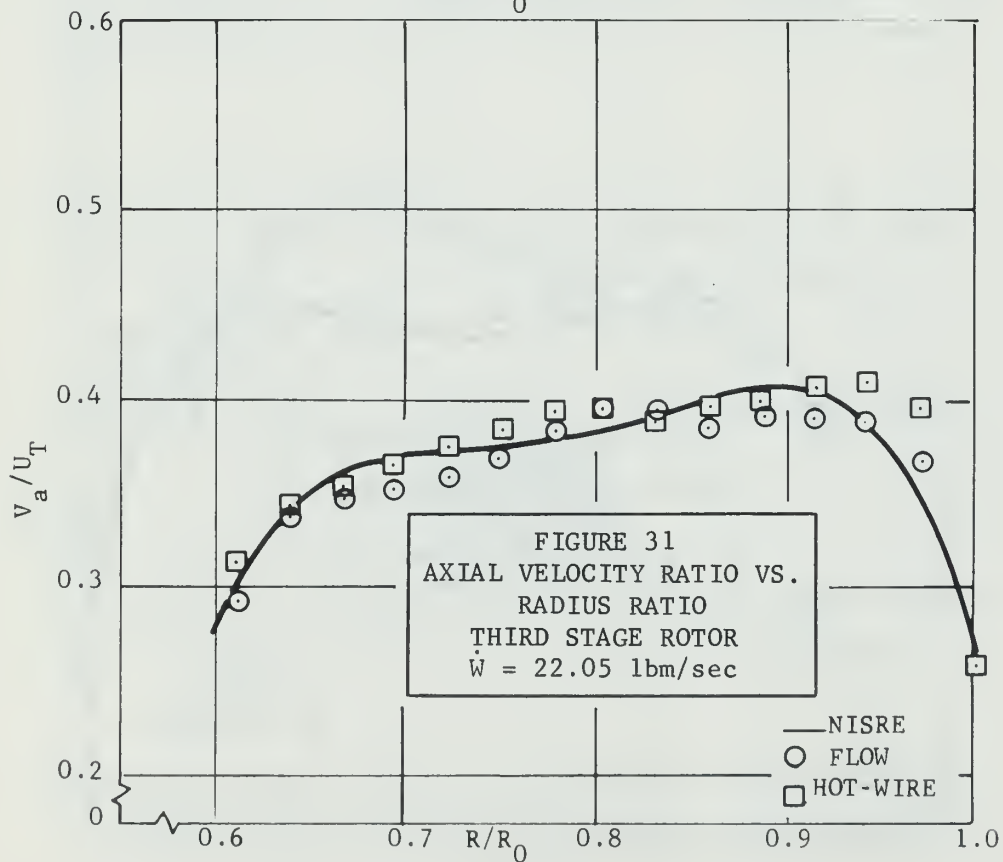
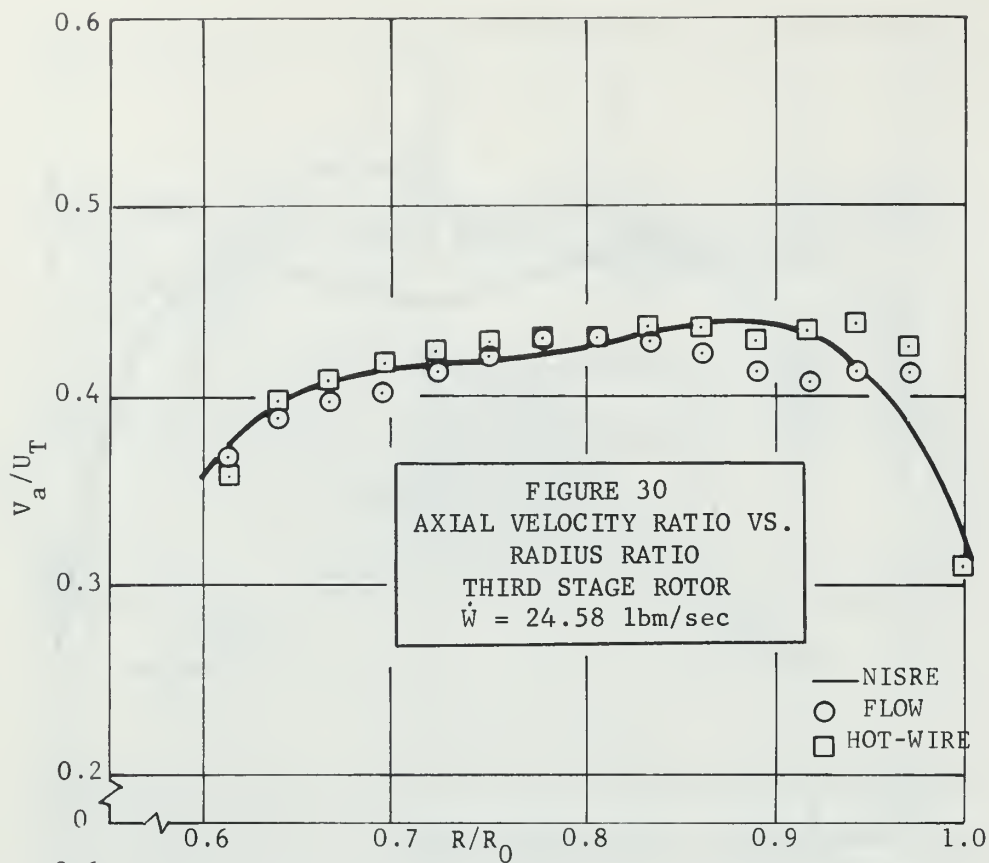


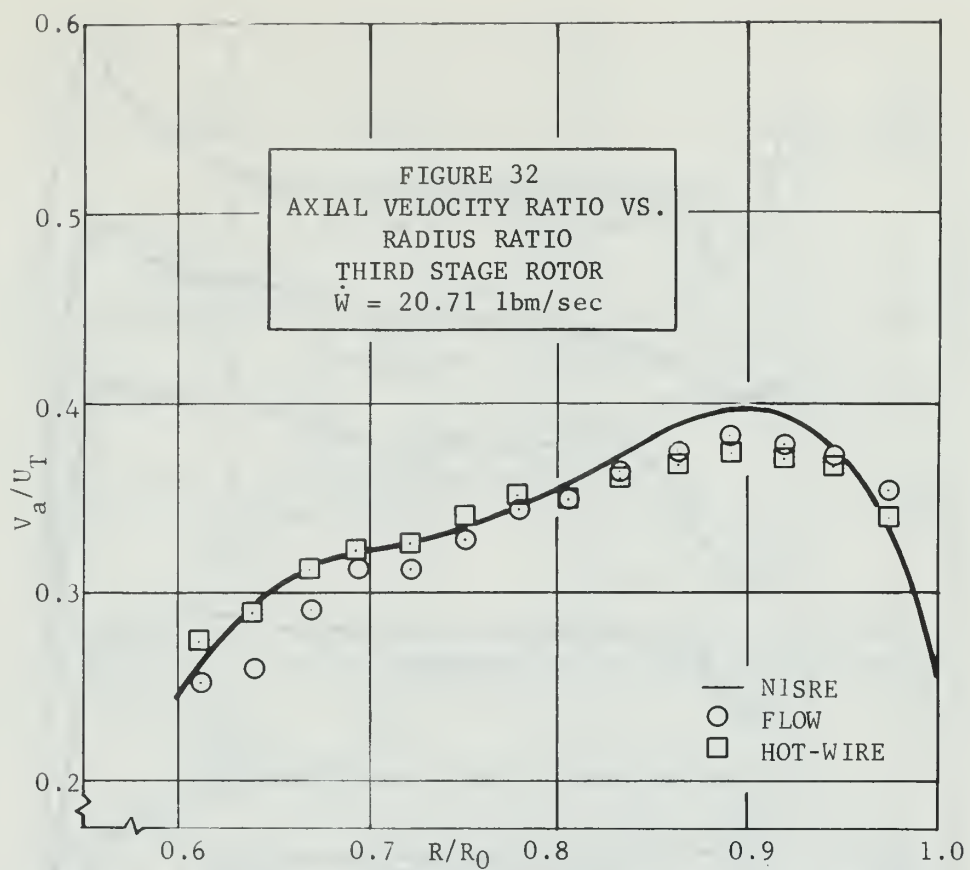












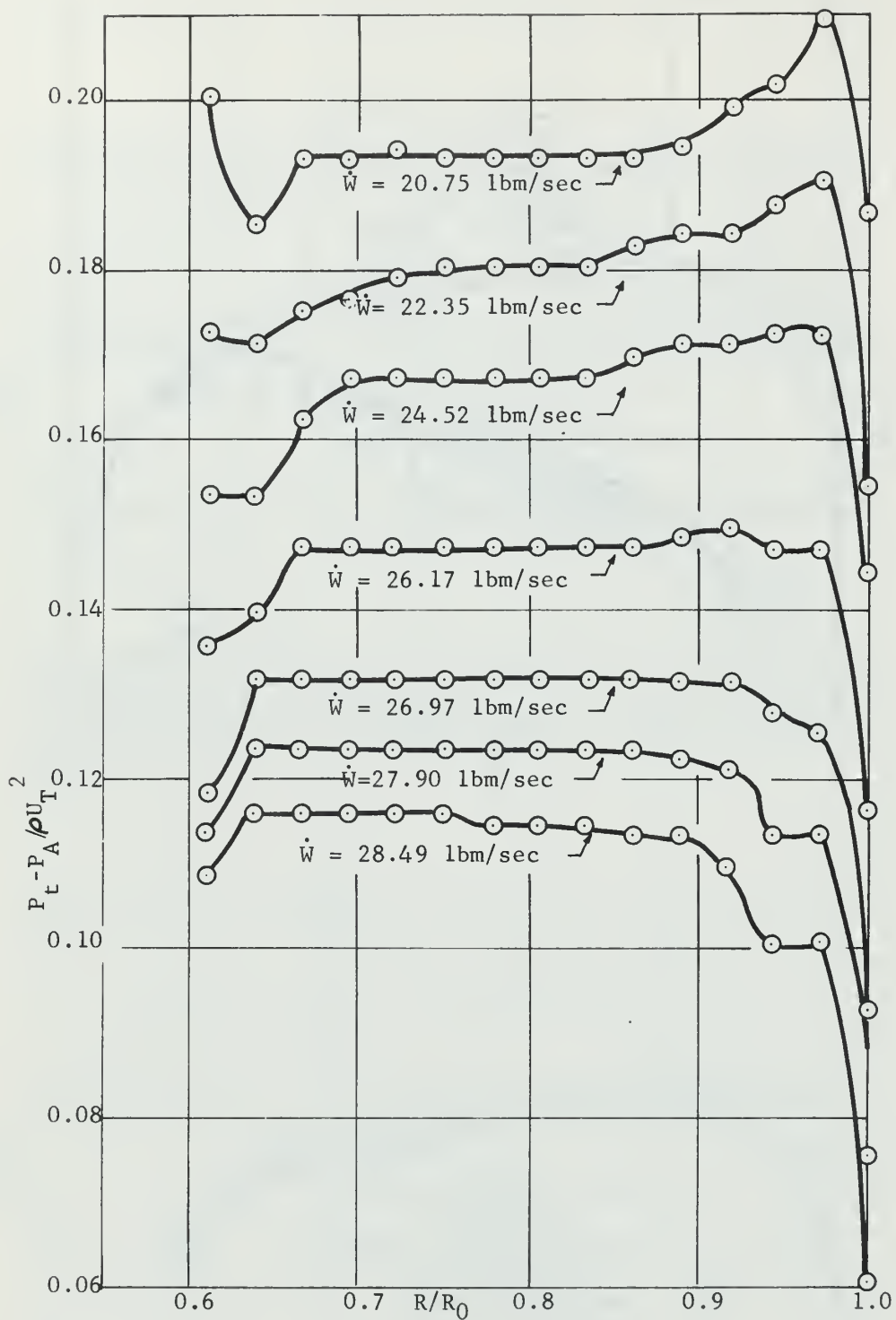


FIGURE 33
TOTAL PRESSURE COEFFICIENT VS. RADIUS RATIO
FIRST STAGE ROTOR

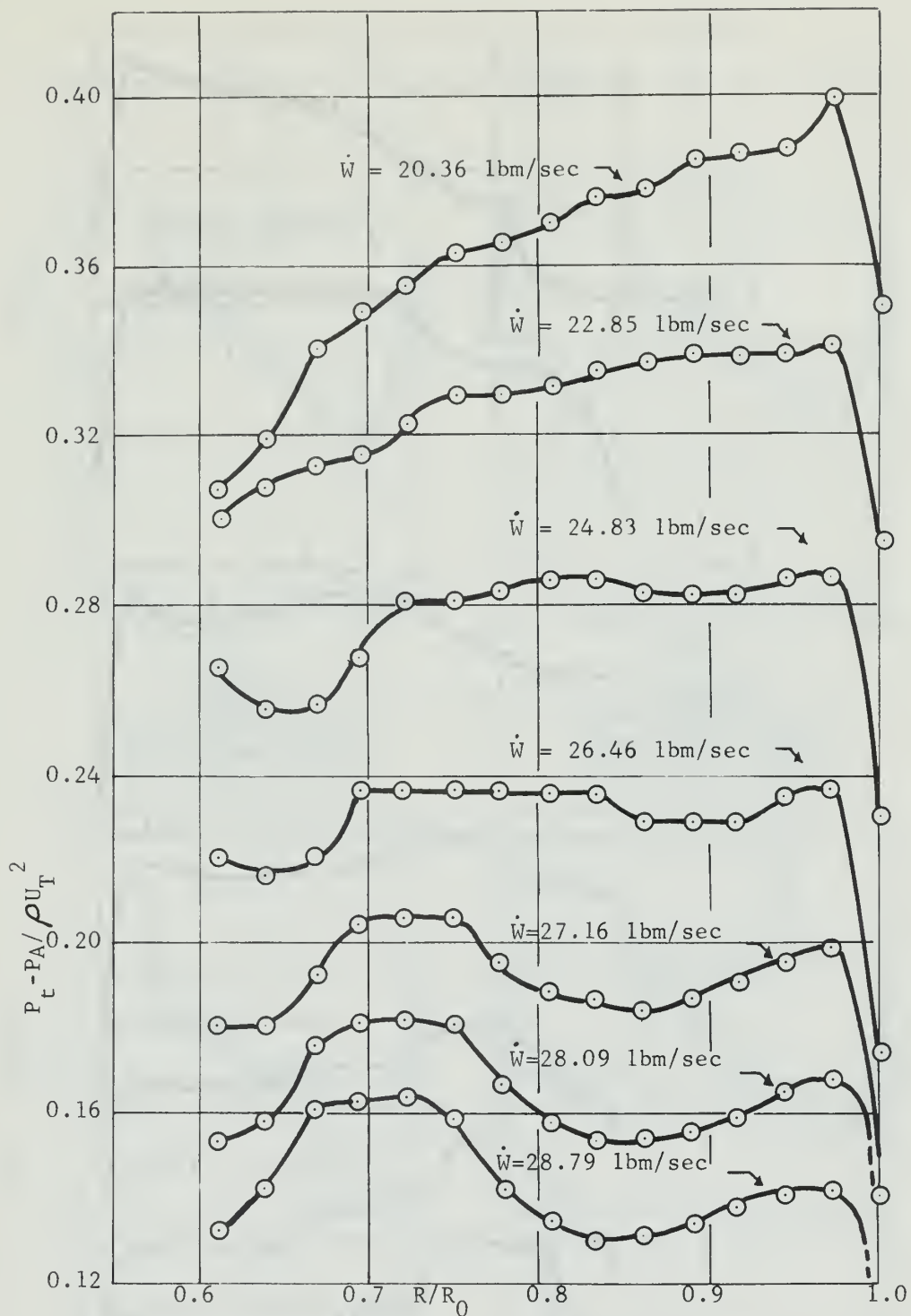


FIGURE 34
TOTAL PRESSURE COEFFICIENT VS. RADIUS RATIO
SECOND STAGE ROTOR

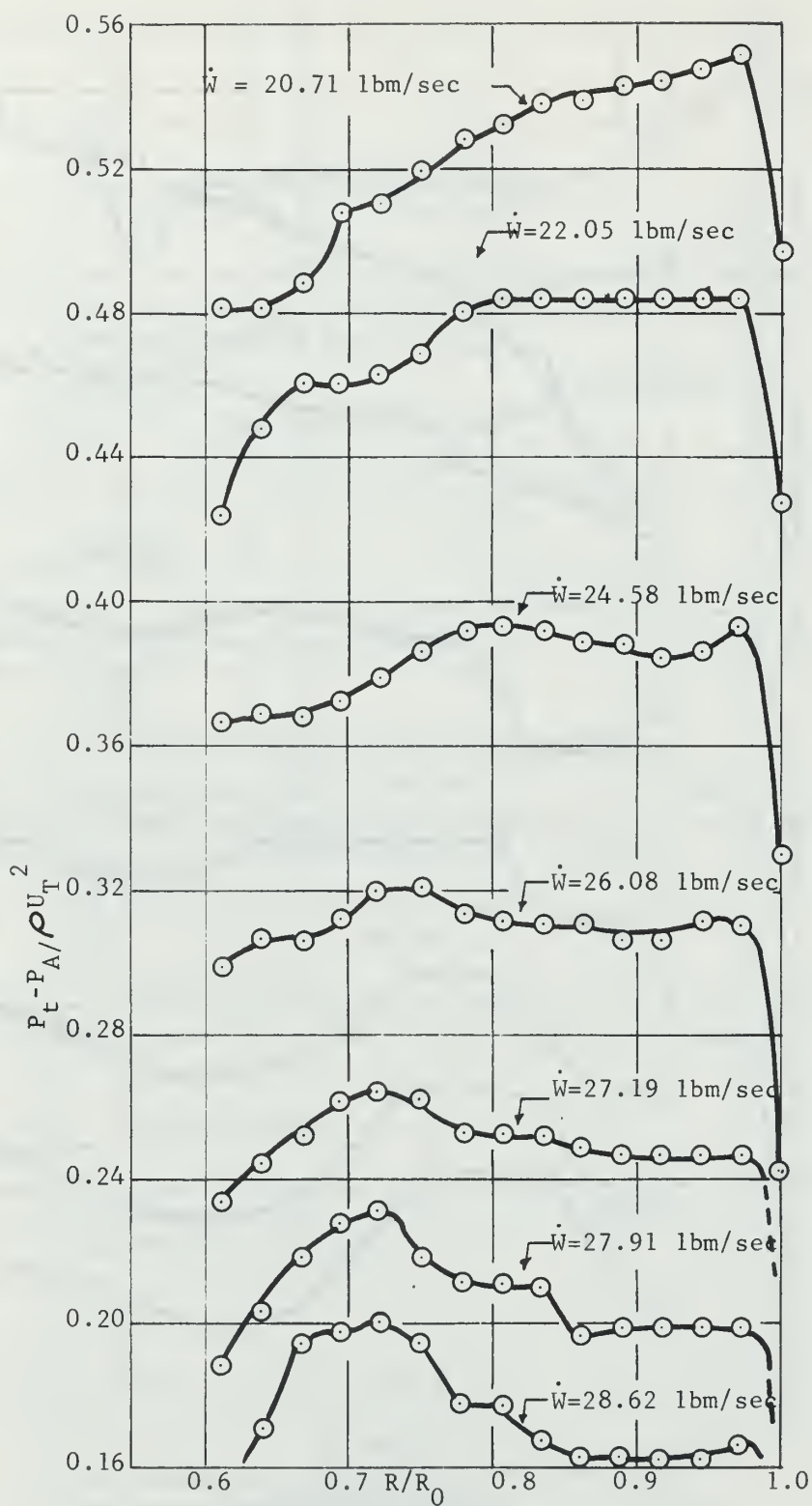


FIGURE 35
TOTAL PRESSURE COEFFICIENT VS. RADIUS RATIO
THIRD STAGE ROTOR

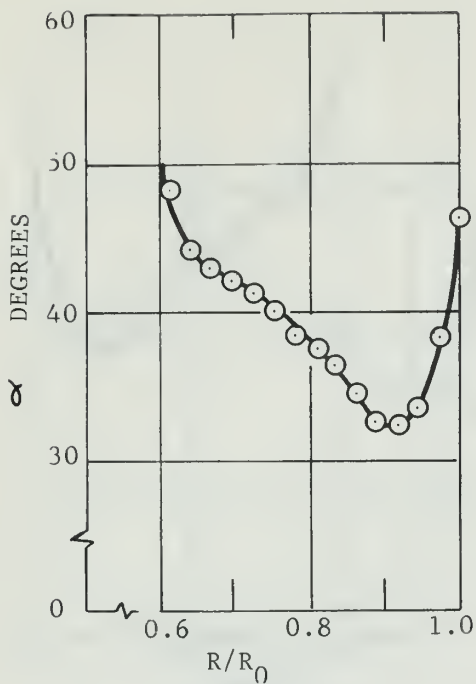


FIGURE 36
 α VS. RADIUS RATIO
 FIRST STAGE ROTOR
 $\dot{W} = 28.49$ lbm/sec

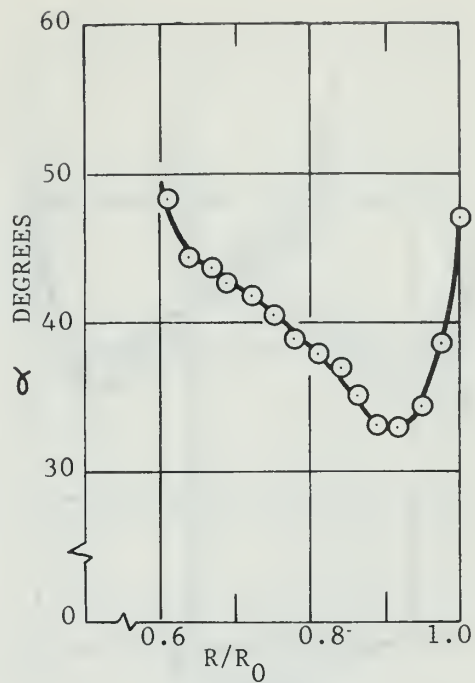


FIGURE 37
 α VS. RADIUS RATIO
 FIRST STAGE ROTOR
 $\dot{W} = 27.90$ lbm/sec

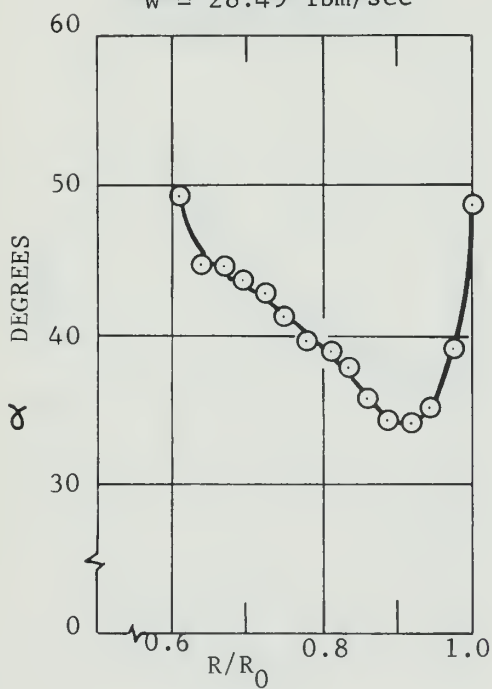


FIGURE 38
 α VS. RADIUS RATIO
 FIRST STAGE ROTOR
 $\dot{W} = 26.97$ lbm/sec

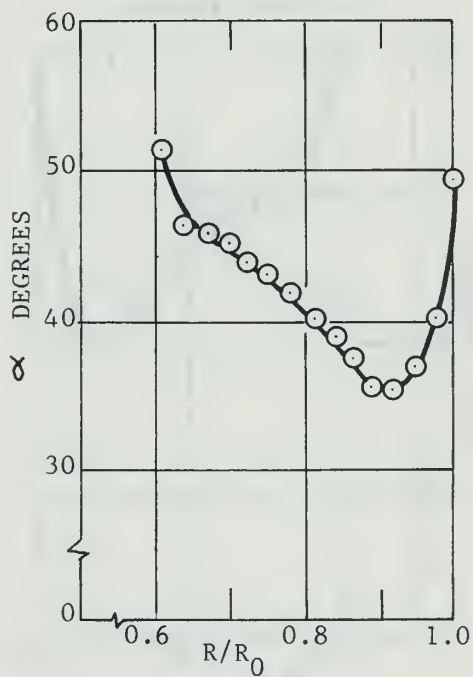


FIGURE 39
 α VS. RADIUS RATIO
 FIRST STAGE ROTOR
 $\dot{W} = 26.17$ lbm/sec

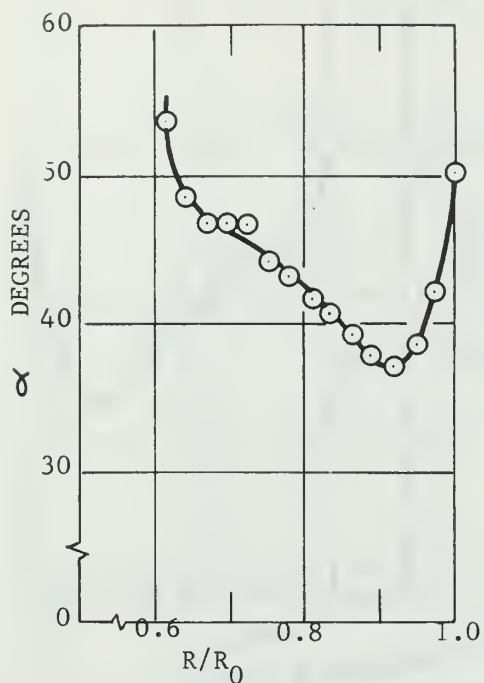


FIGURE 40
 α VS. RADIUS RATIO
 FIRST STAGE ROTOR
 $\dot{W} = 24.52$ lbm/sec

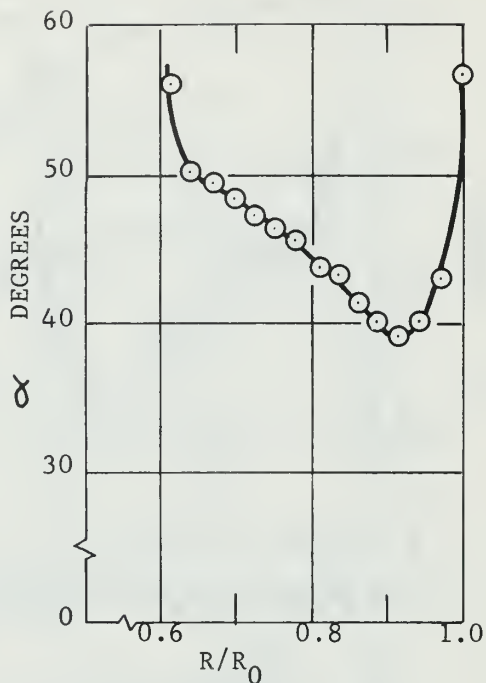


FIGURE 41
 α VS. RADIUS RATIO
 FIRST STAGE ROTOR
 $\dot{W} = 22.35$ lbm/sec

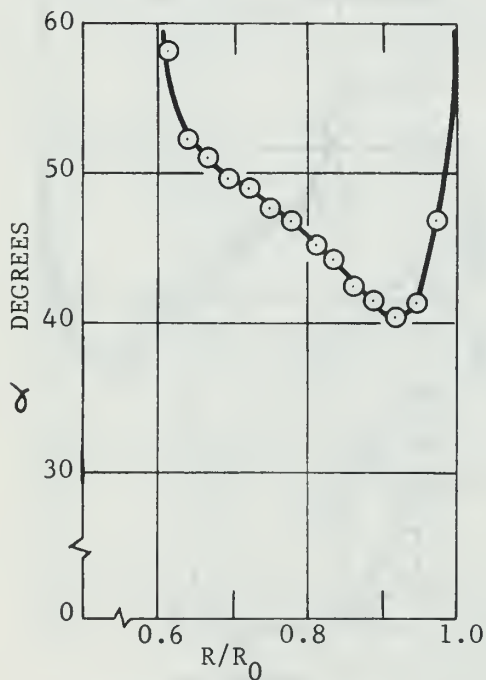


FIGURE 42
 α VS. RADIUS RATIO
 FIRST STAGE ROTOR
 $\dot{W} = 20.75$ lbm/sec

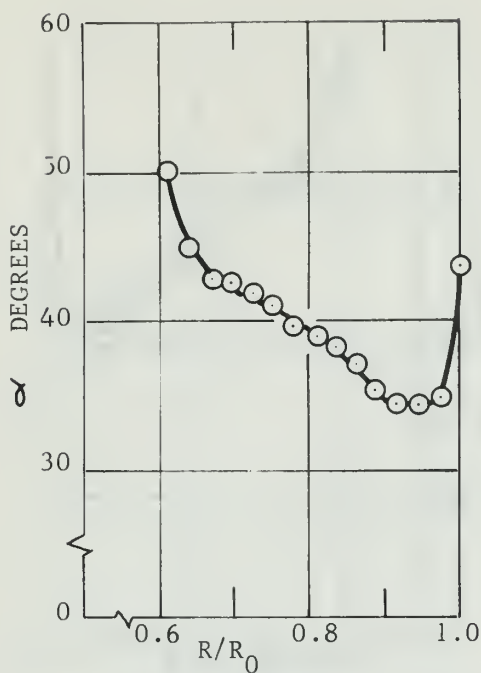


FIGURE 43
 α VS. RADIUS RATIO
 SECOND STAGE ROTOR
 $\dot{W} = 28.79$ lbm/sec

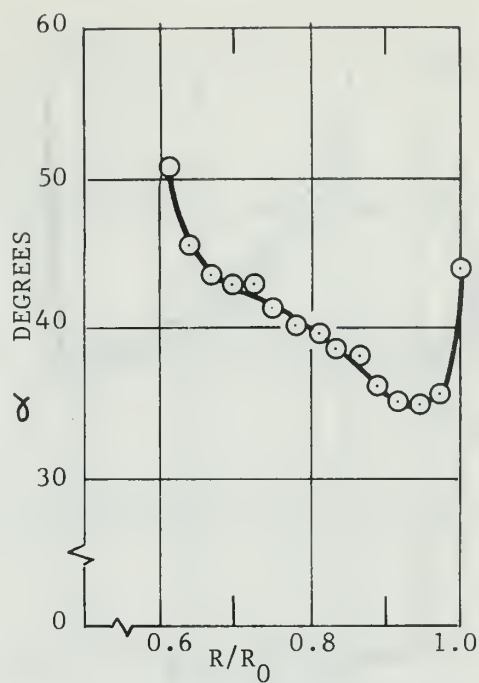


FIGURE 44
 α VS. RADIUS RATIO
 SECOND STAGE ROTOR
 $\dot{W} = 28.09$ lbm/sec

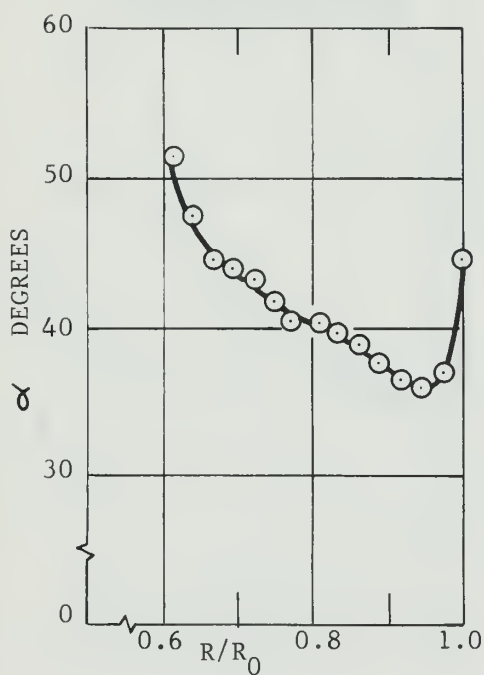


FIGURE 45
 α VS. RADIUS RATIO
 SECOND STAGE ROTOR
 $\dot{W} = 27.16$ lbm/sec

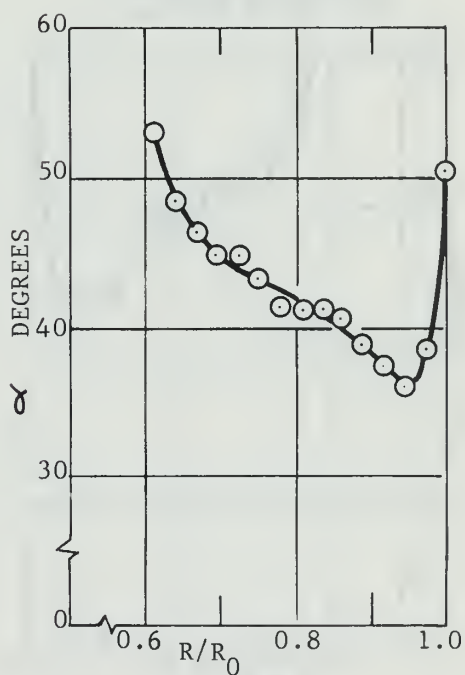


FIGURE 46
 α VS. RADIUS RATIO
 SECOND STAGE ROTOR
 $\dot{W} = 26.46$ lbm/sec

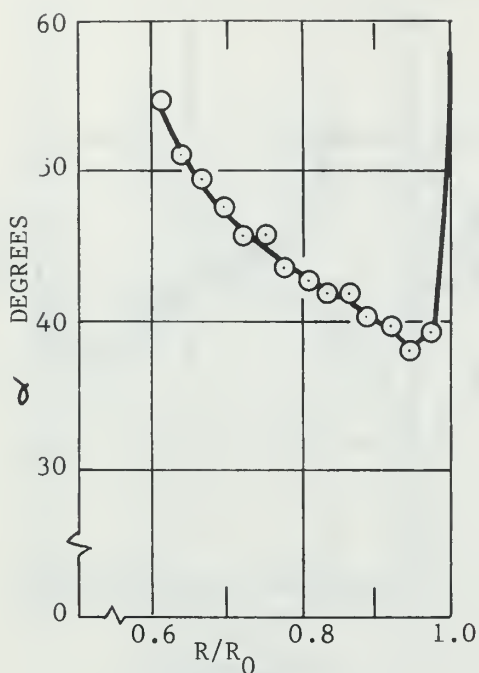


FIGURE 47
 α VS. RADIUS RATIO
 SECOND STAGE ROTOR
 $\dot{W} = 24.83$ lbm/sec

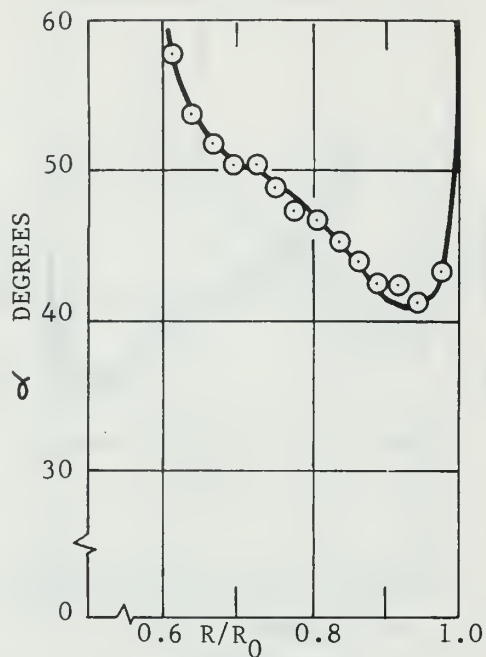


FIGURE 48
 α VS. RADIUS RATIO
 SECOND STAGE ROTOR
 $\dot{W} = 22.85$ lbm/sec

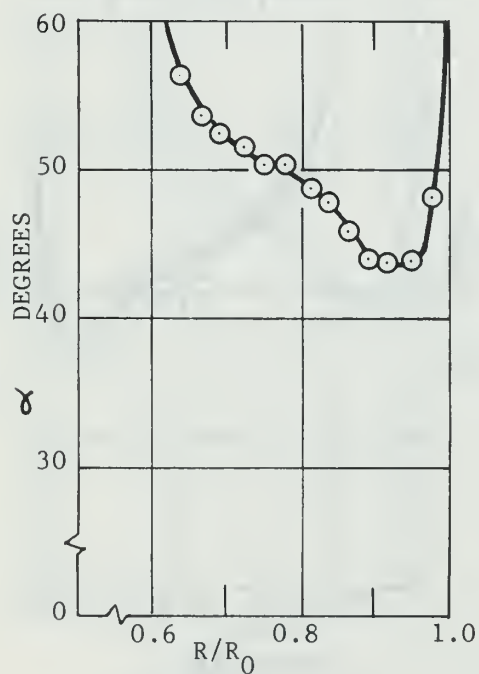


FIGURE 49
 α VS. RADIUS RATIO
 SECOND STAGE ROTOR
 $\dot{W} = 20.36$ lbm/sec

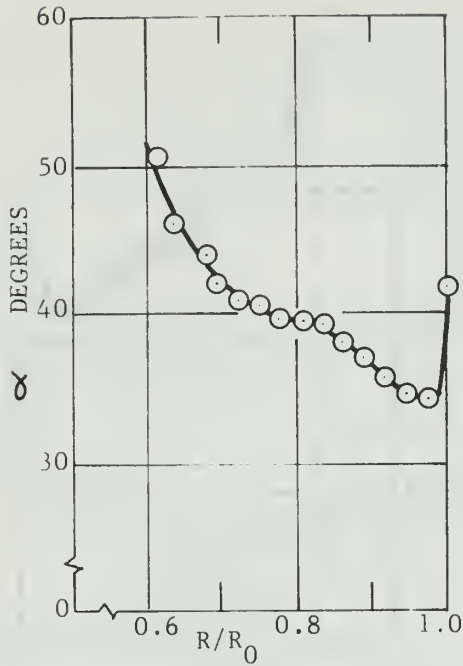


FIGURE 50
 α VS. RADIUS RATIO
 THIRD STAGE ROTOR
 $\dot{W} = 28.62$ lbm/sec

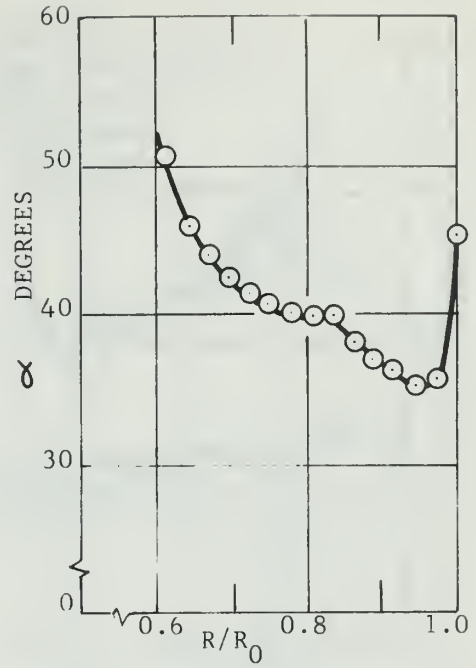


FIGURE 51
 α VS. RADIUS RATIO
 THIRD STAGE ROTOR
 $\dot{W} = 27.91$ lbm/sec

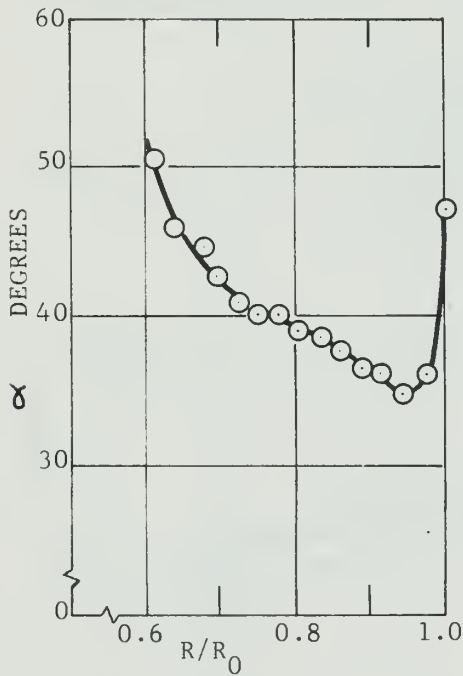


FIGURE 52
 α VS. RADIUS RATIO
 THIRD STAGE ROTOR
 $\dot{W} = 27.19$ lbm/sec

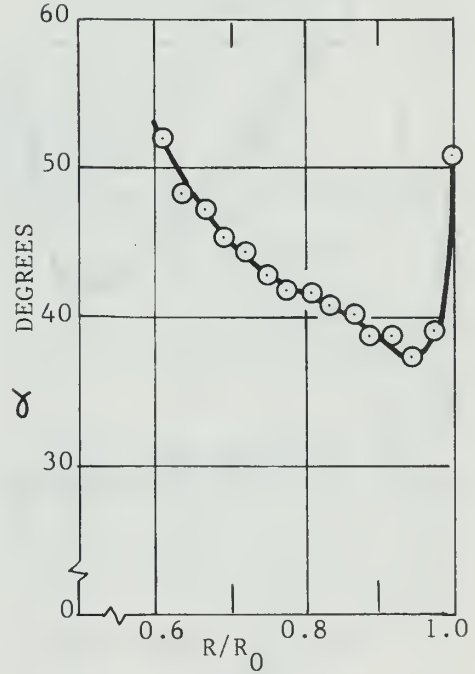


FIGURE 53
 α VS. RADIUS RATIO
 THIRD STAGE ROTOR
 $\dot{W} = 26.08$ lbm/sec

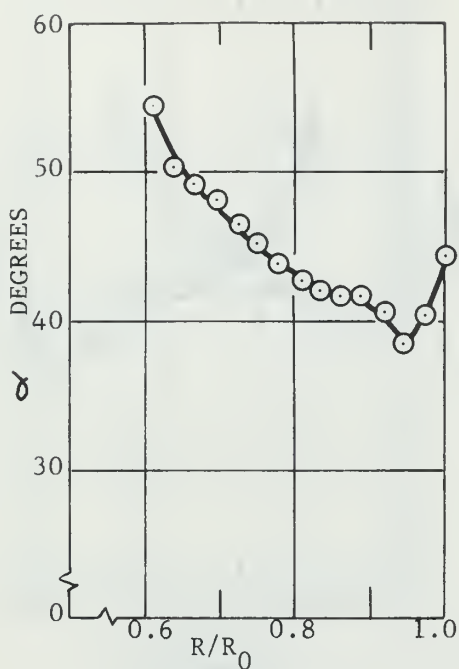


FIGURE 54
 α VS. RADIUS RATIO
 THIRD STAGE ROTOR
 $\dot{W} = 24.58$ lbm/sec

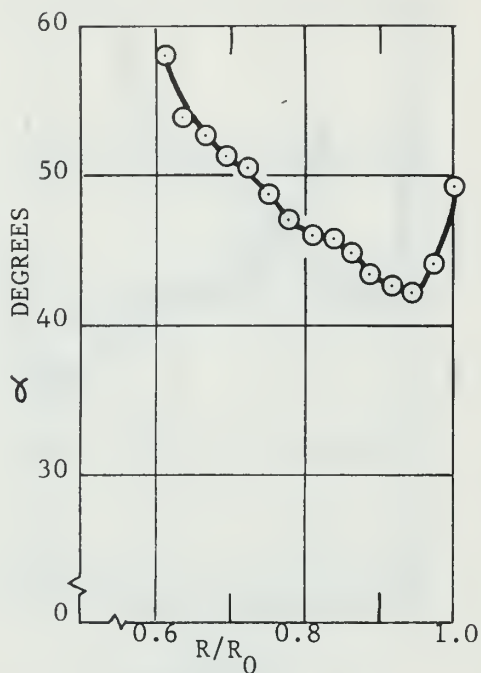


FIGURE 55
 α VS. RADIUS RATIO
 THIRD STAGE ROTOR
 $\dot{W} = 22.05$ lbm/sec

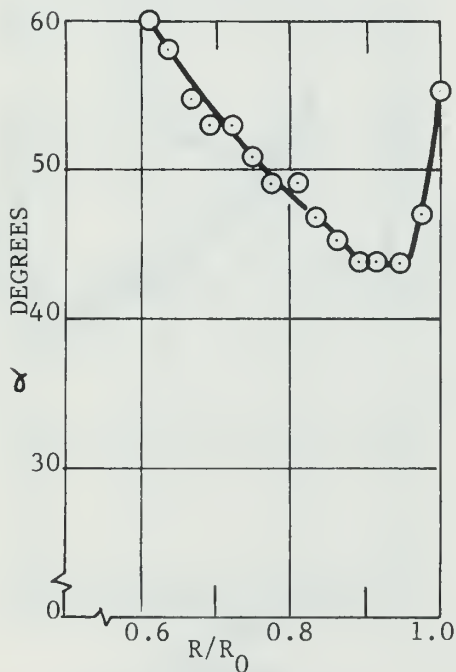
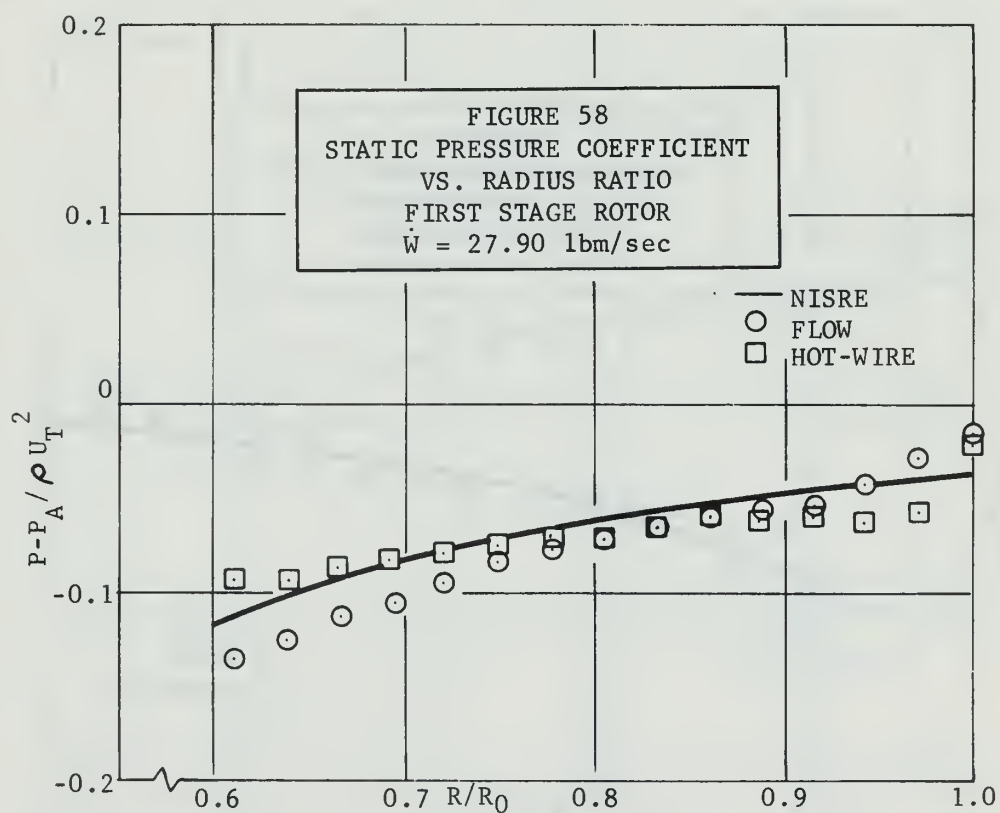
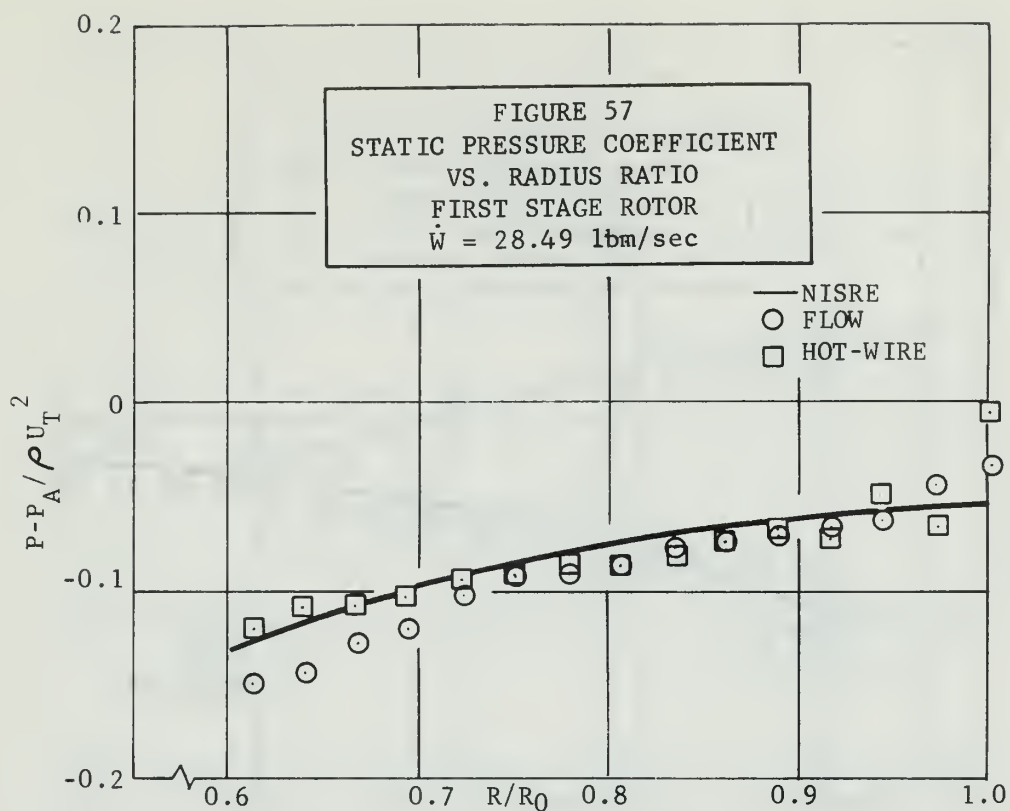
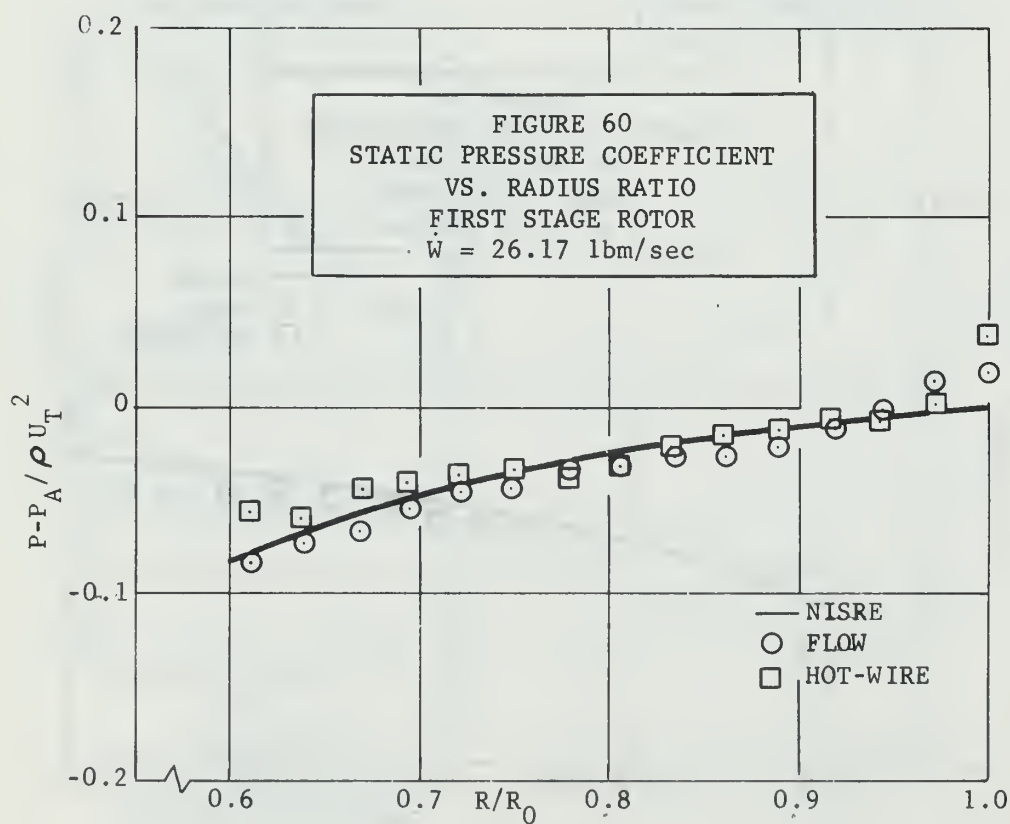
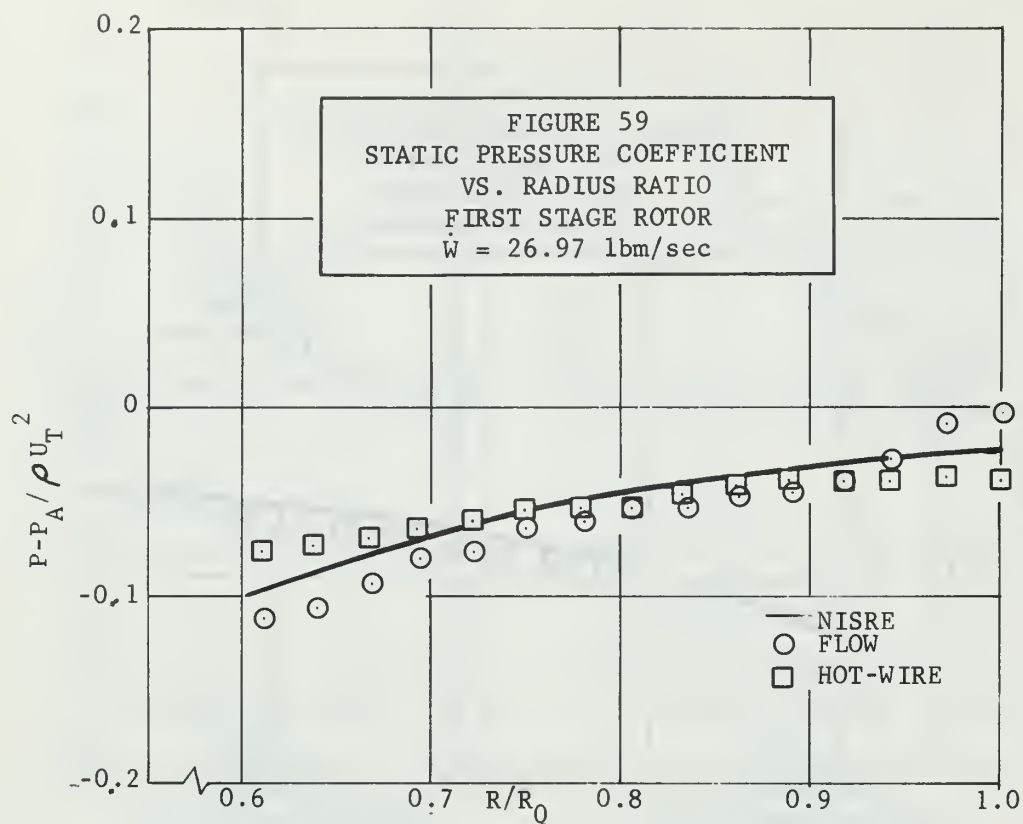
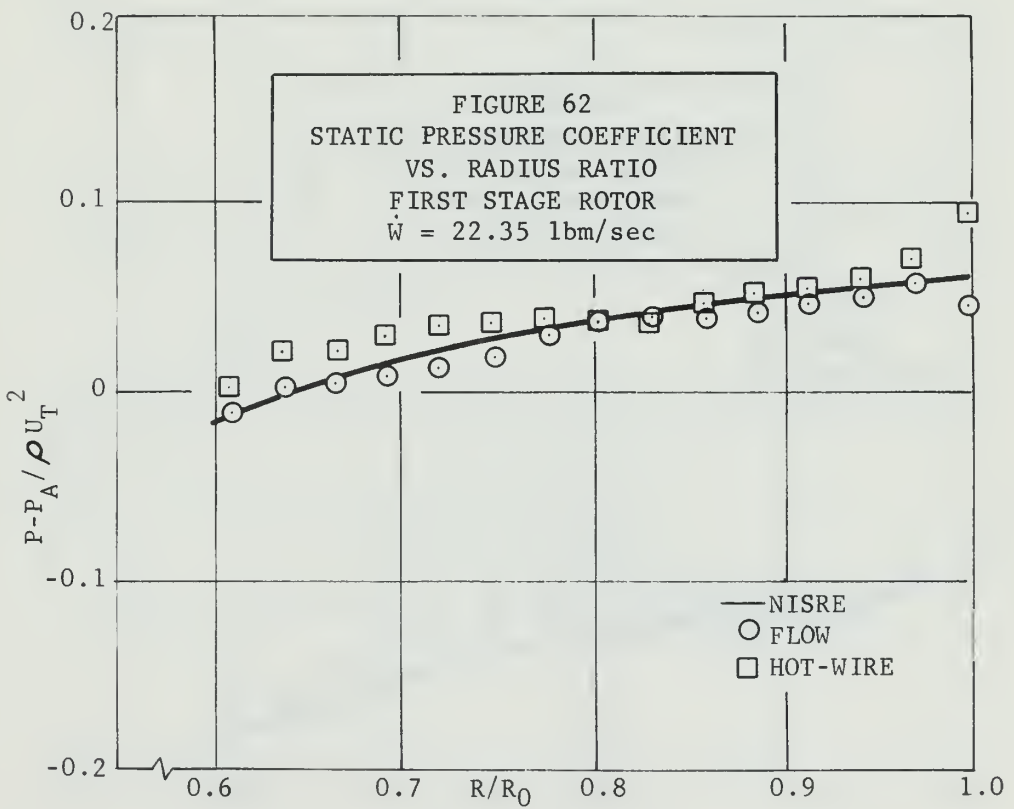
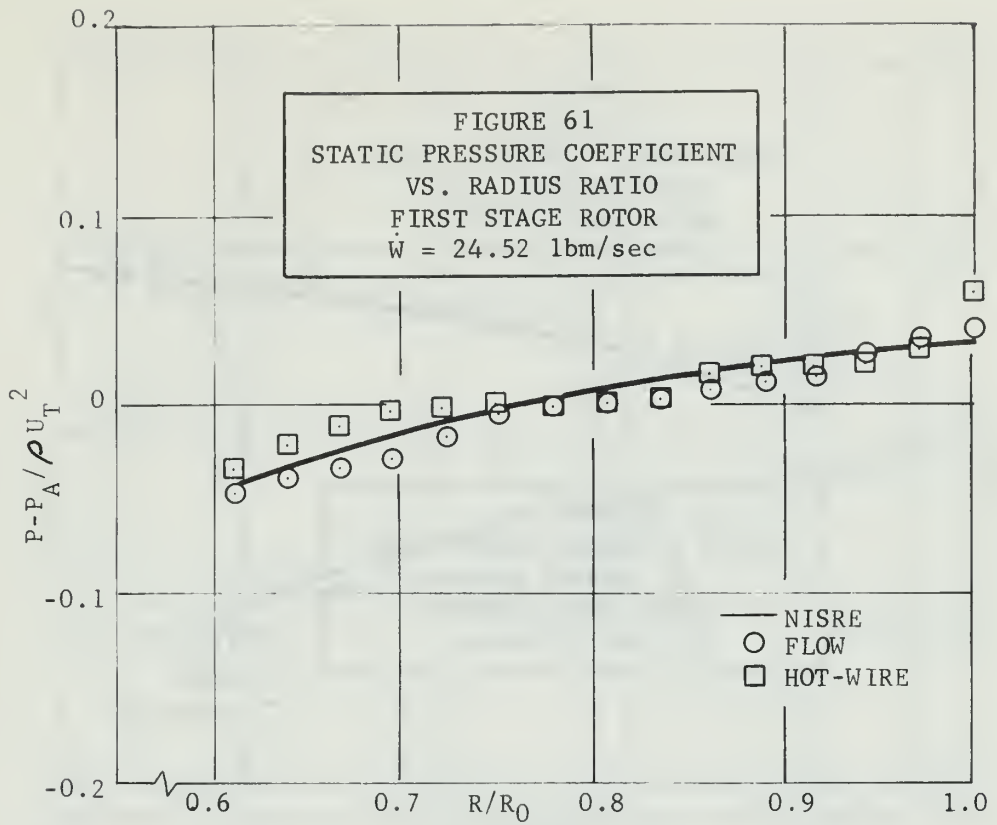
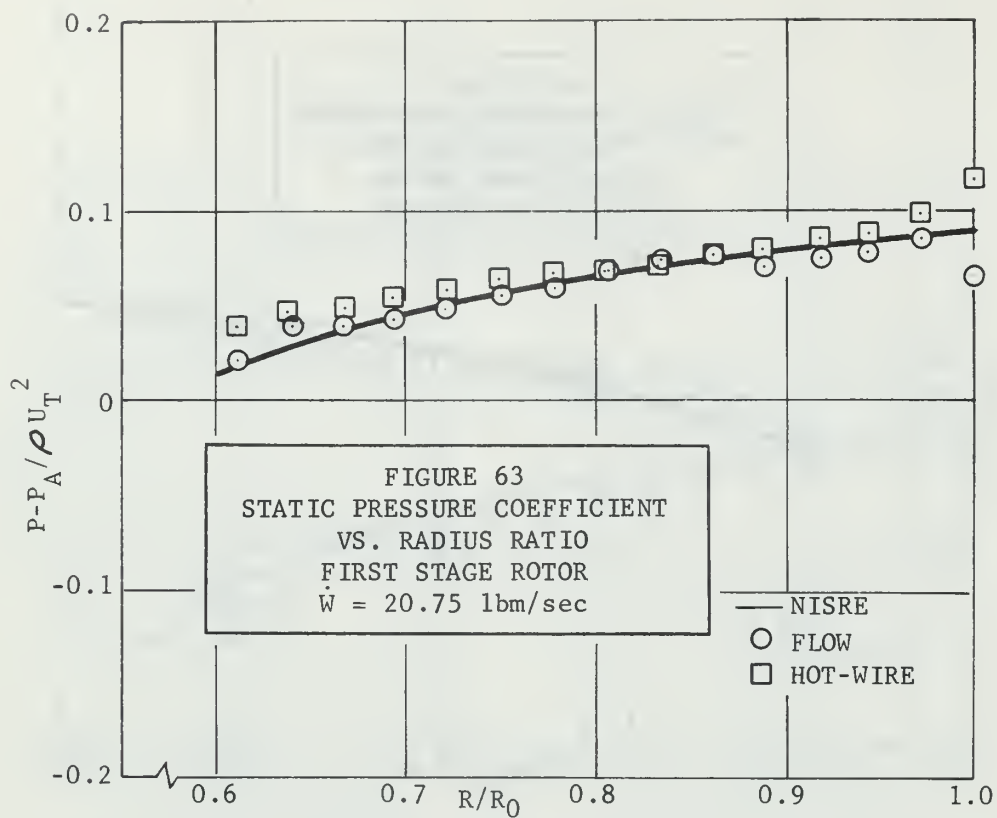


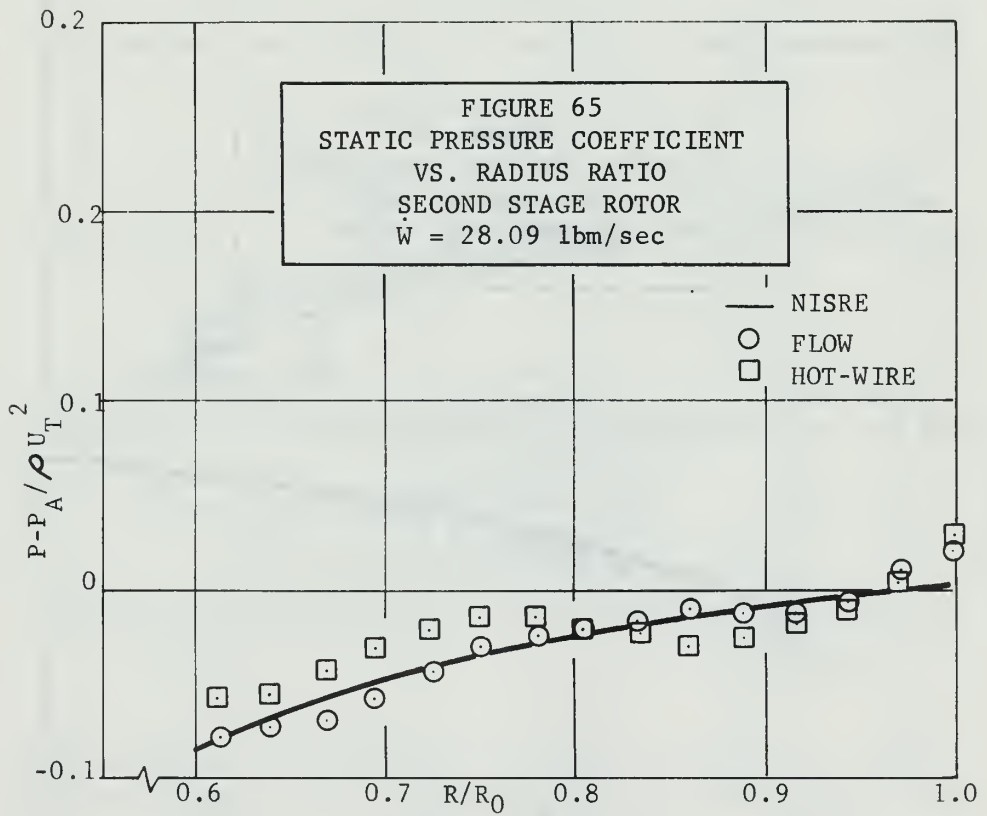
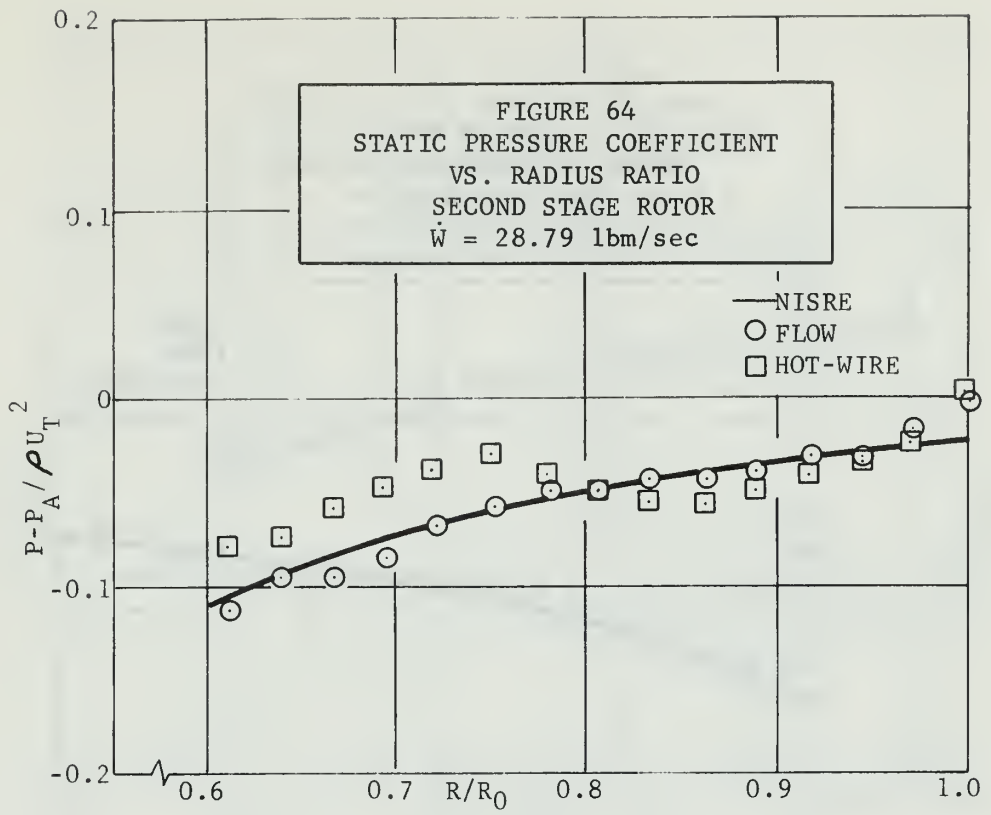
FIGURE 56
 α VS. RADIUS RATIO
 THIRD STAGE ROTOR
 $\dot{W} = 20.71$ lbm/sec

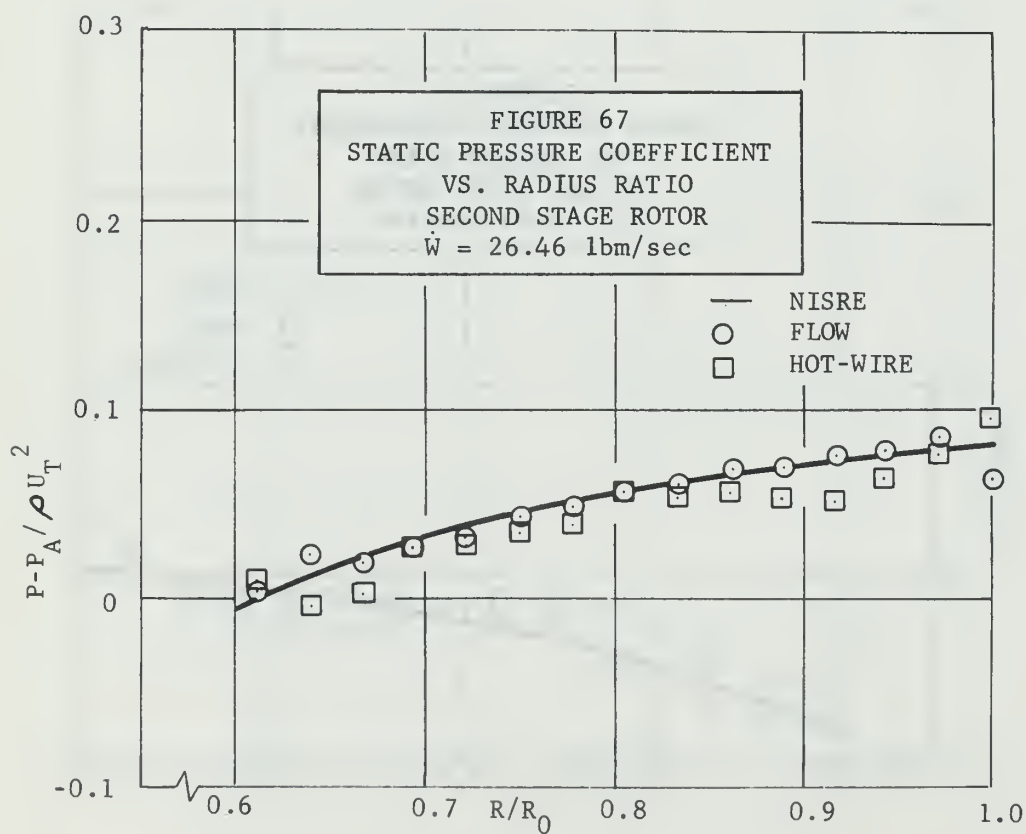
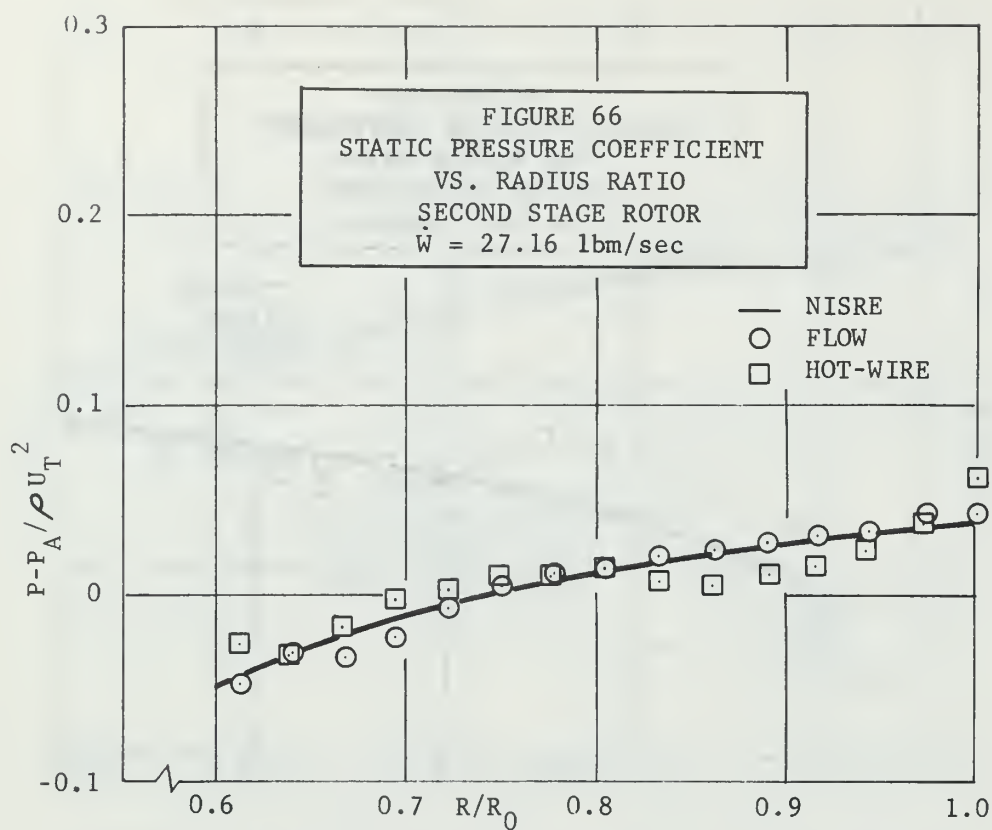


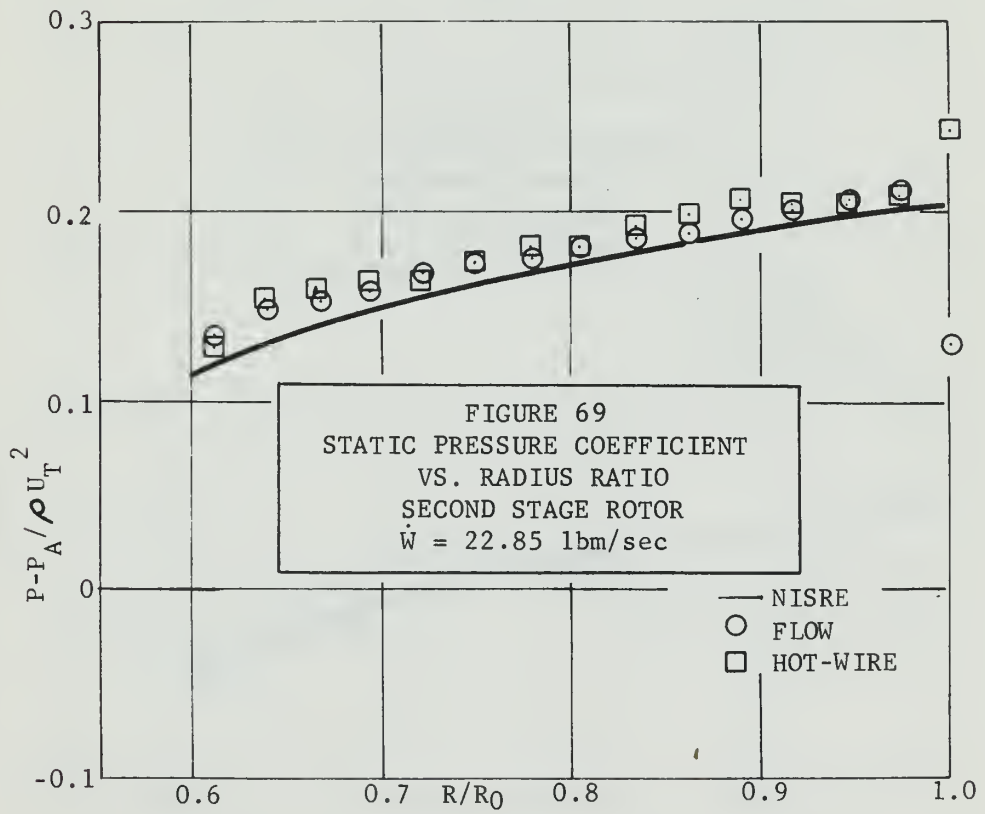
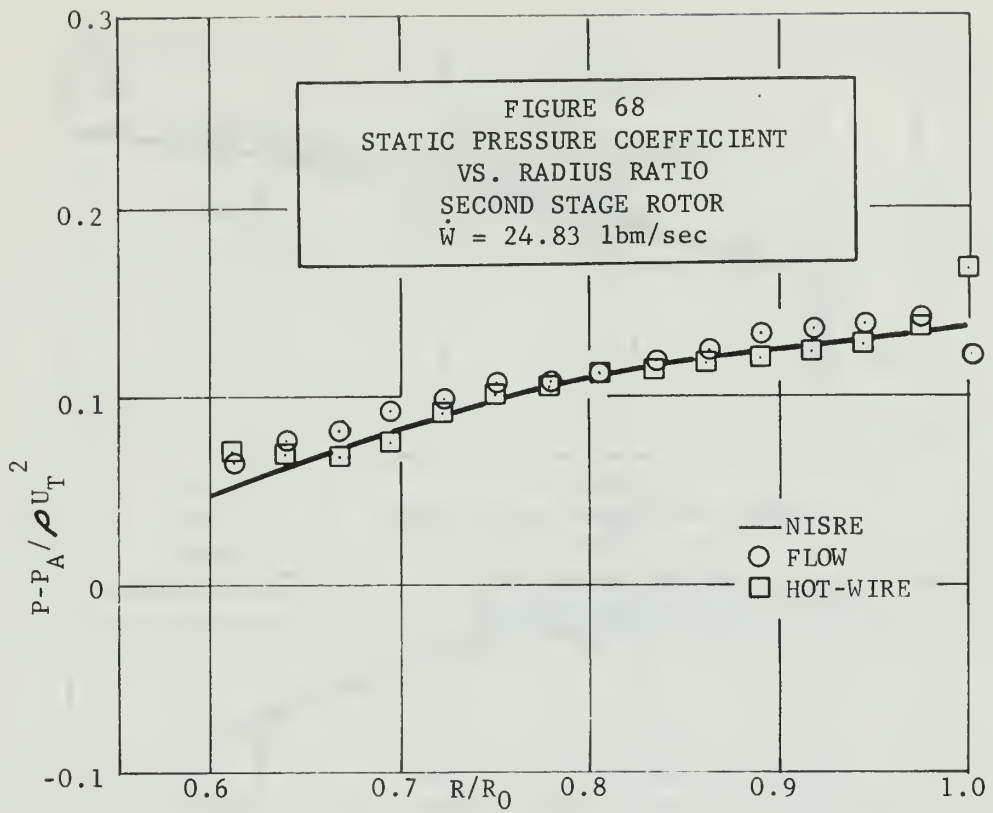


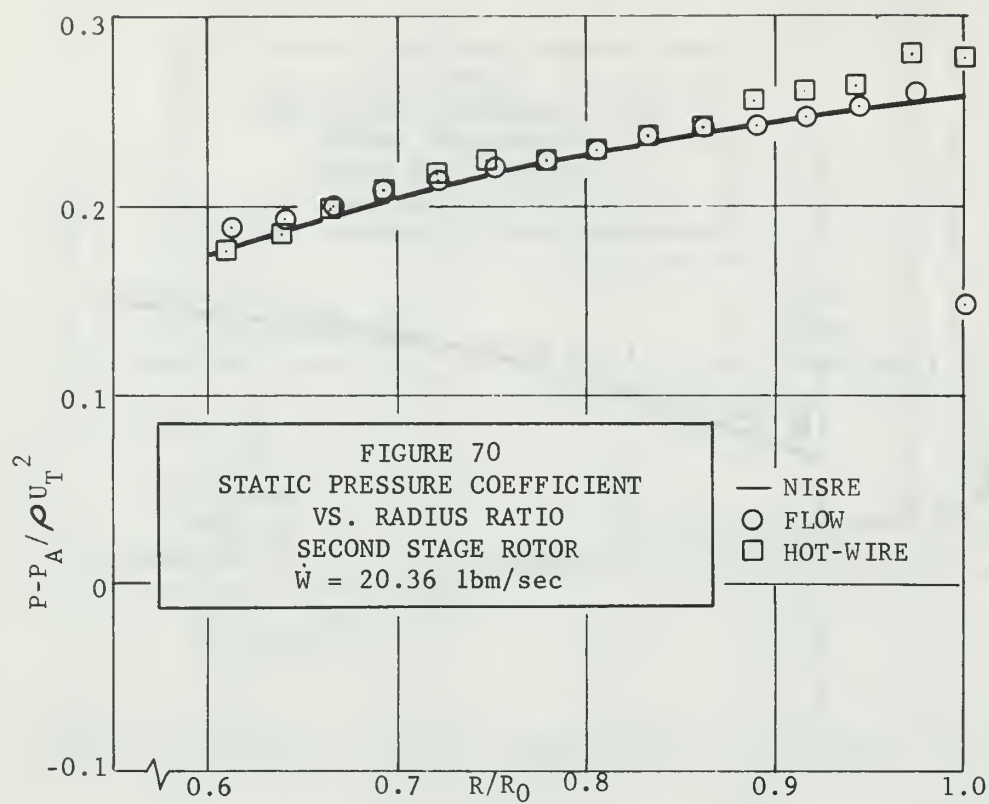


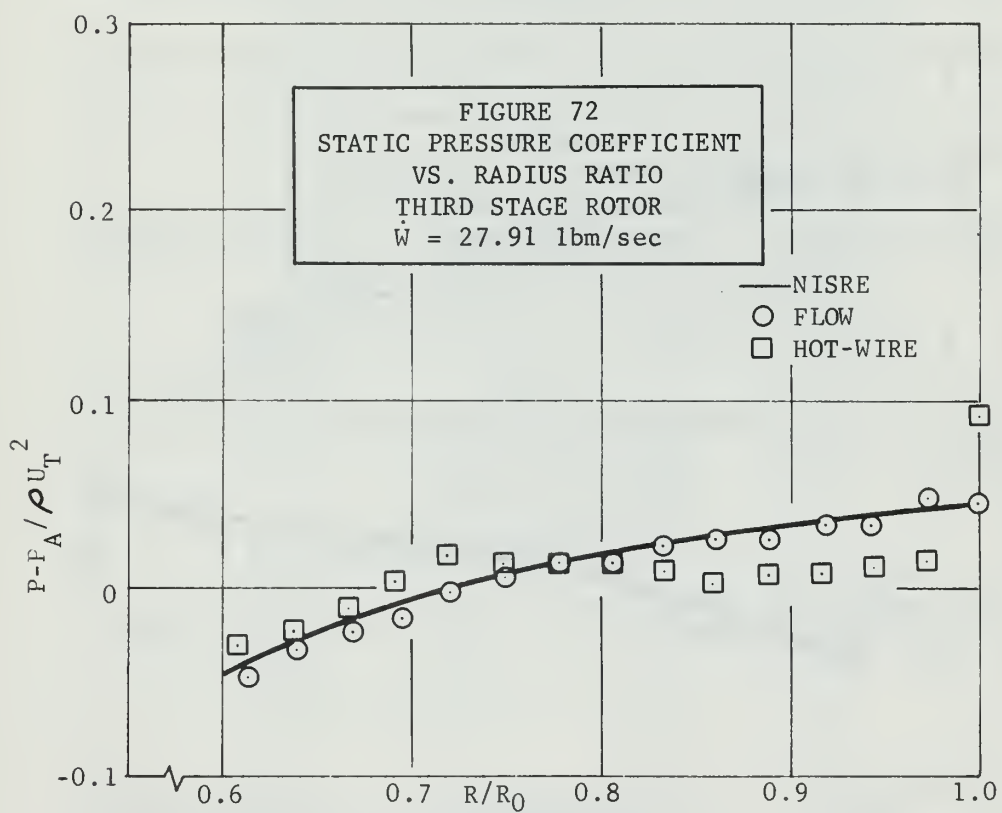
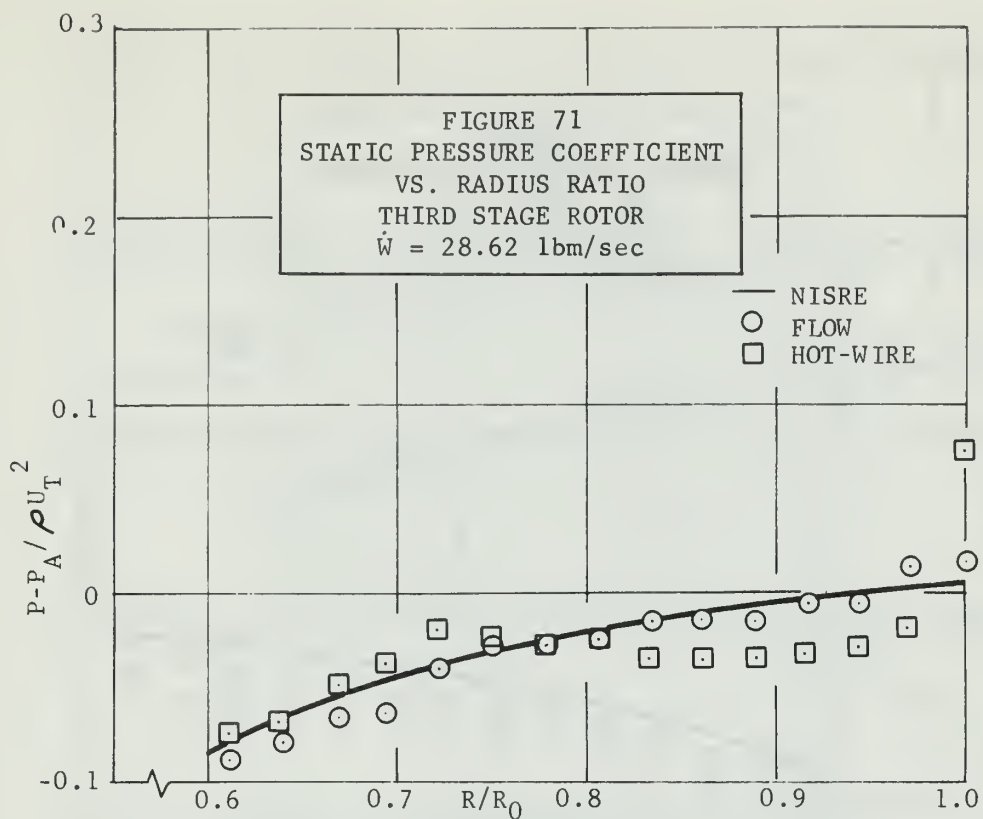


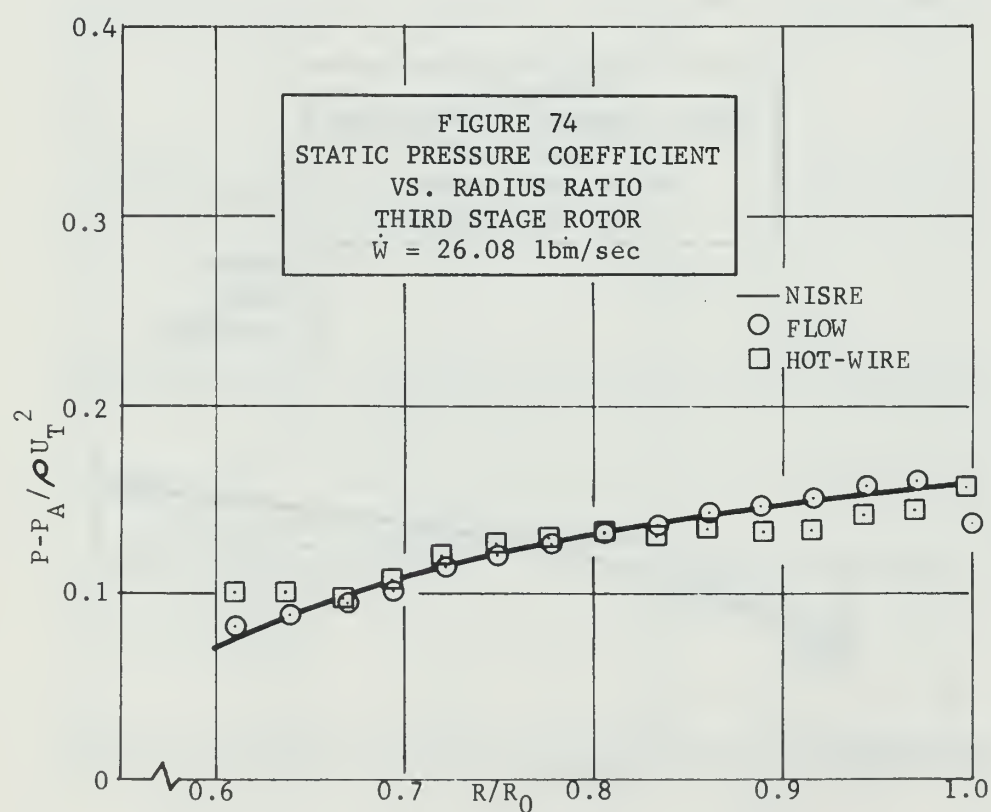
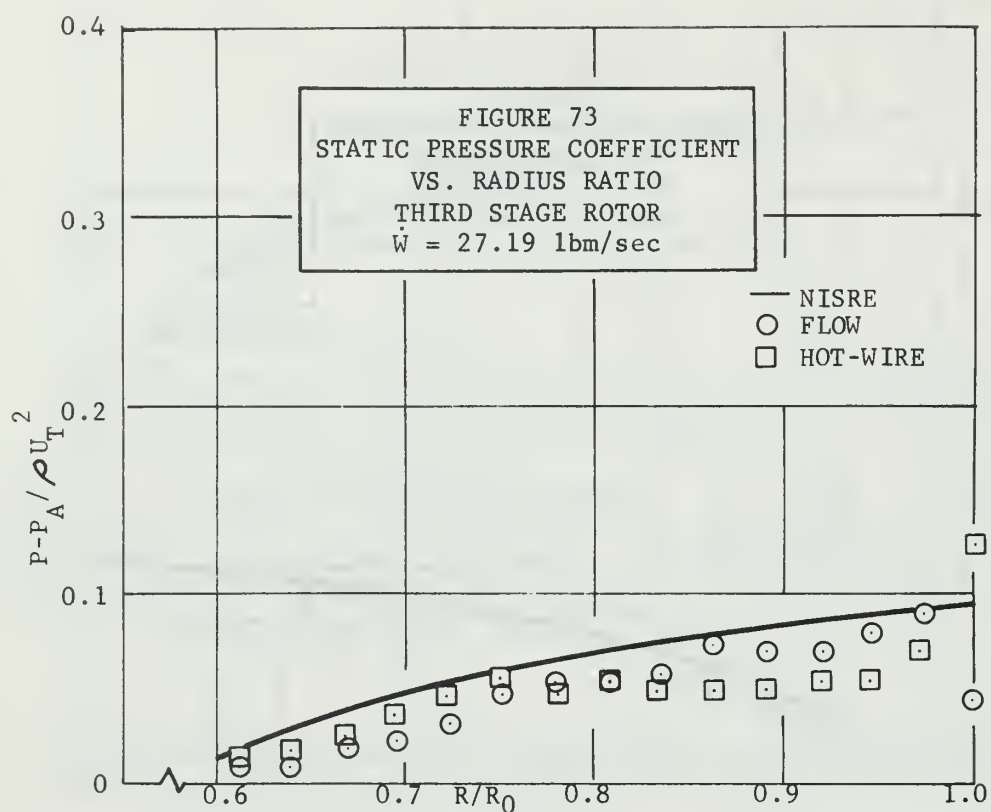


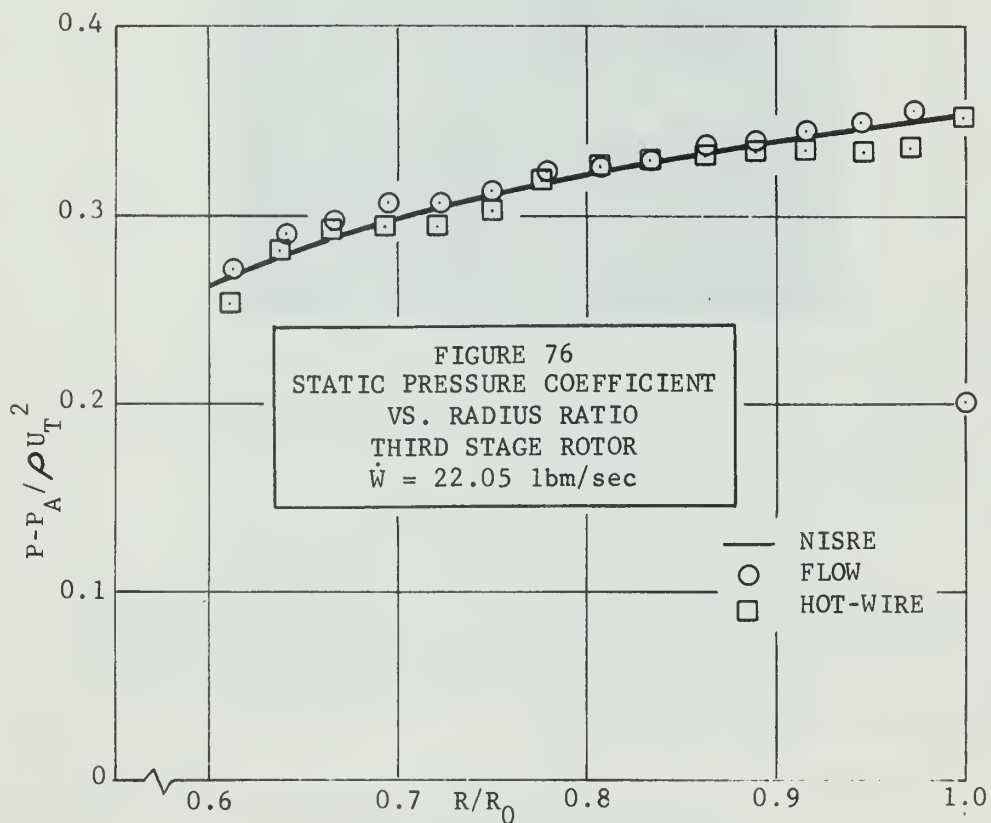
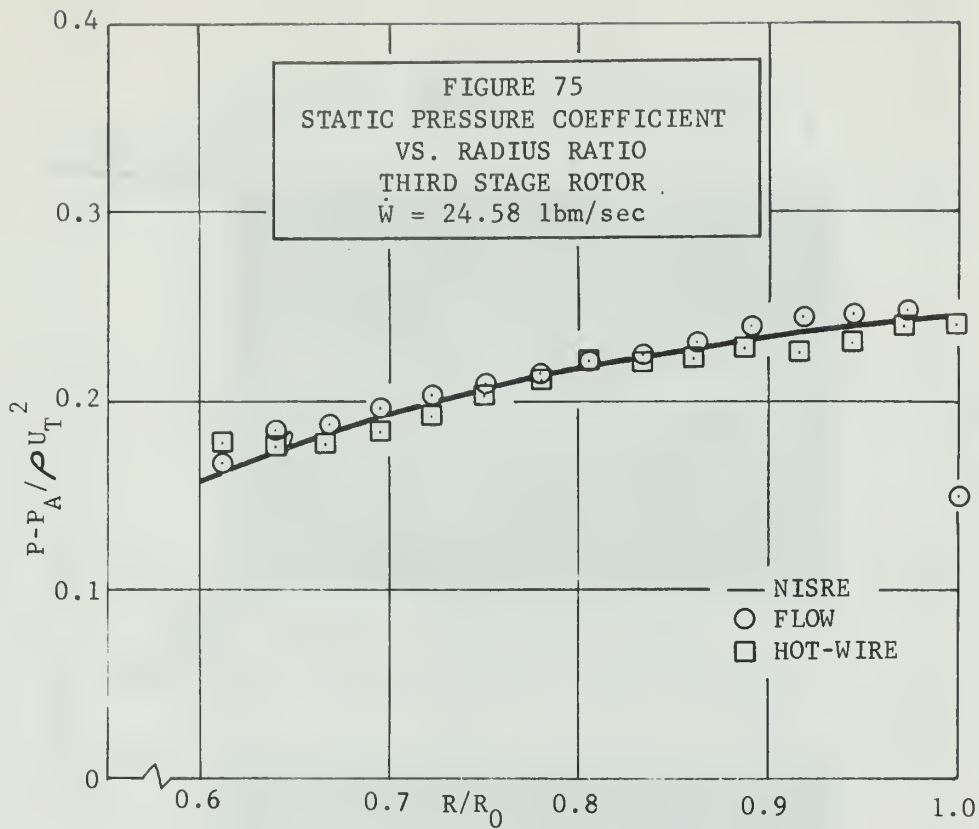


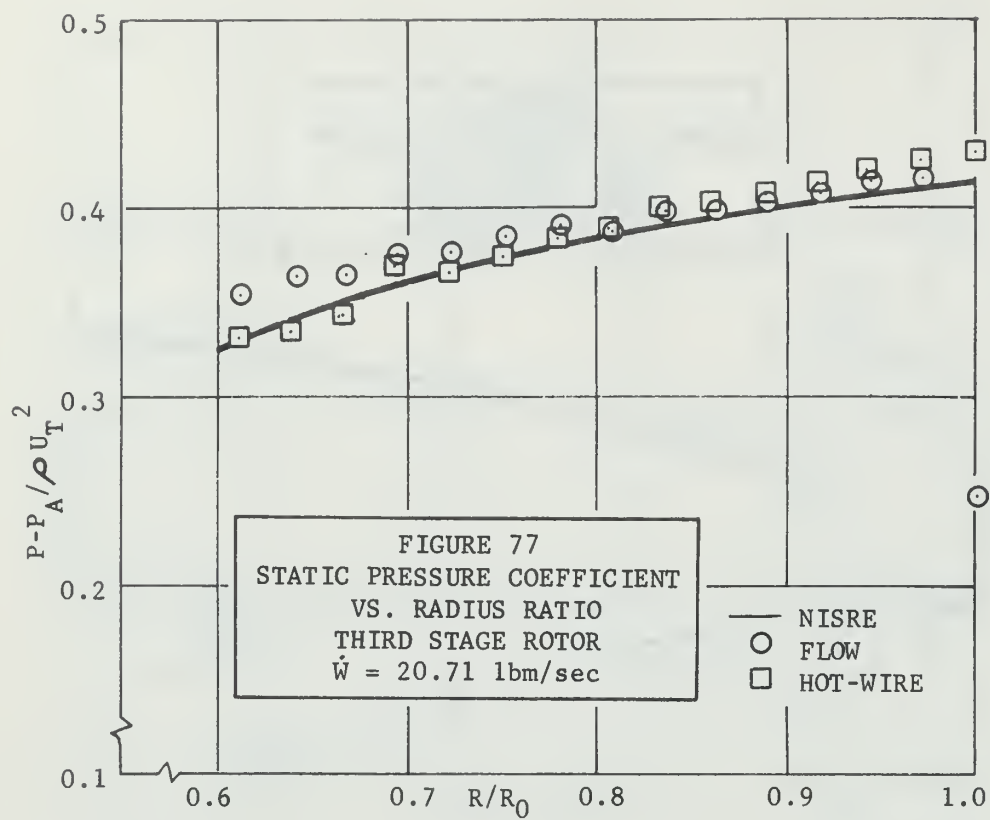


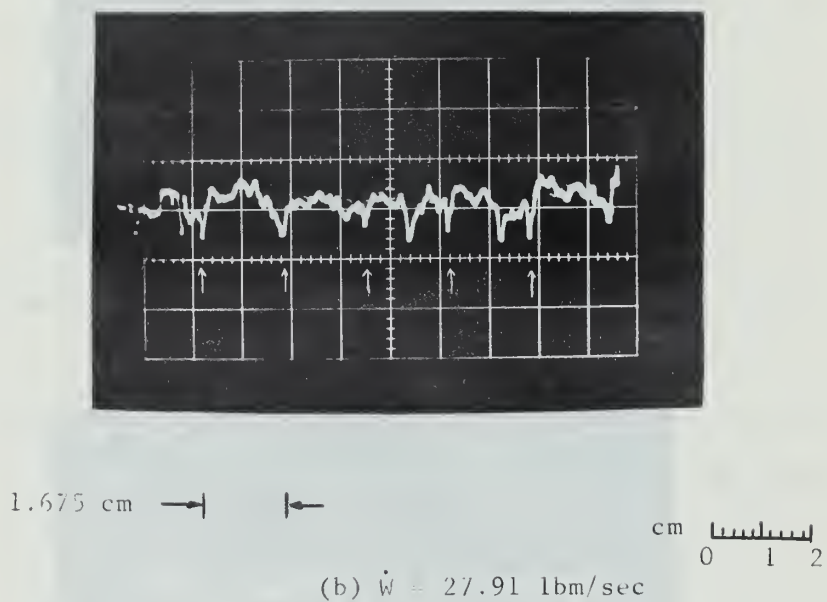
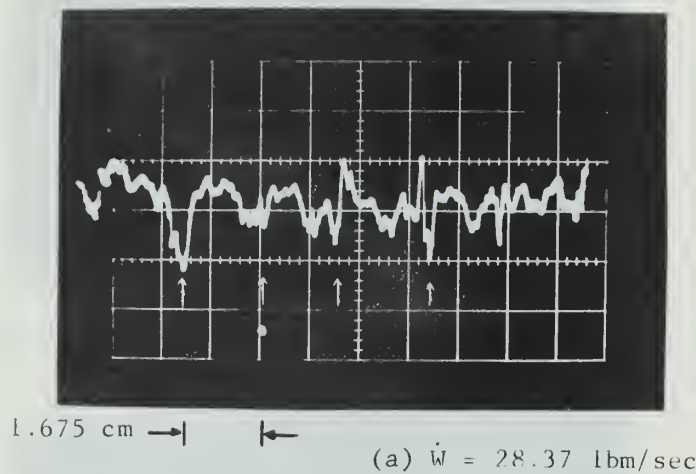








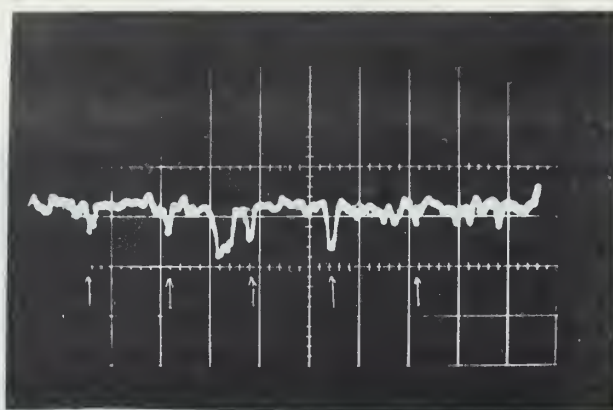




PROBE POSITION
DOWNSTREAM OF
SECOND STAGE ROTOR
RADIUS = 13 inches

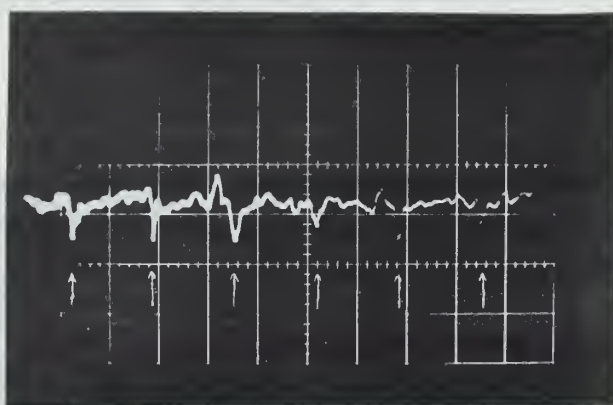
OSCILLOSCOPE SETTINGS
TIME SCALE 1 millisecc/cm
AMPLITUDE 10 millivolt/cm
HOT-WIRE CURRENT 25 milliamps

FIGURE 76
HOT-WIRE ANEMOMETER OSCILLOGRAMS
SECOND STAGE ROTOR



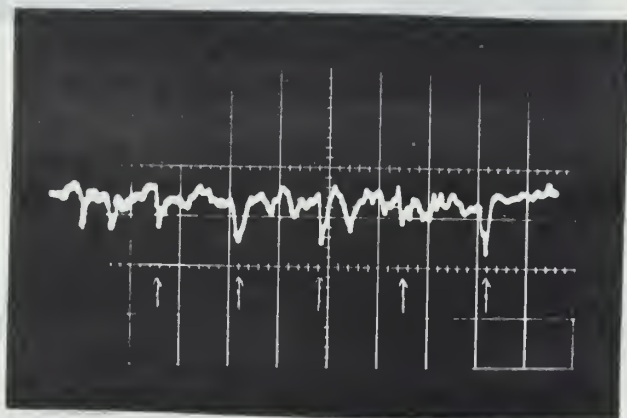
1.675 cm → | ←

(c) $\dot{W} = 27.12 \text{ lbm/sec}$



1.675 cm → | ←

(d) $\dot{W} = 25.93 \text{ lbm/sec}$

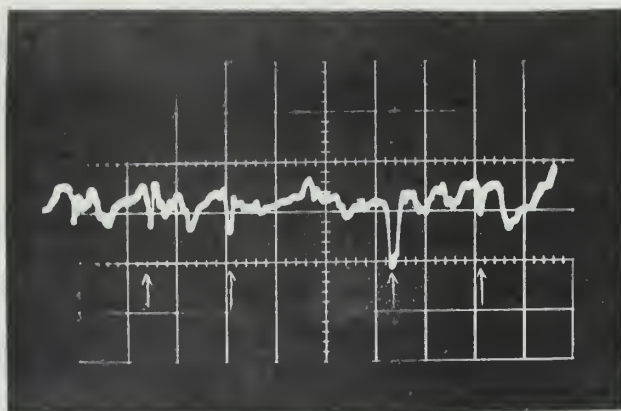


1.675 cm → | ←

(e) $\dot{W} = 24.80 \text{ lbm/sec}$

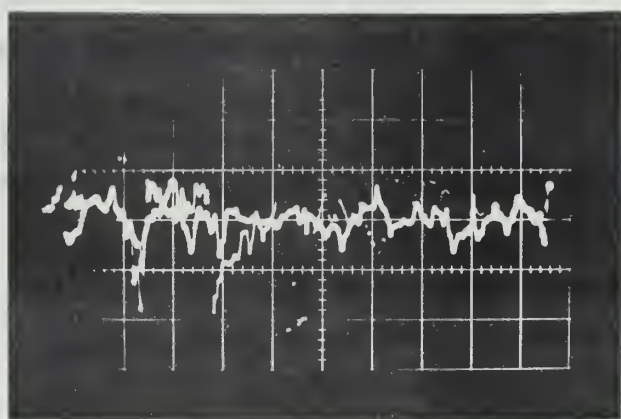
cm 0 1 2

FIGURE 78 (continued)



1.675 cm \rightarrow | \leftarrow

(f) $\dot{W} = 22.52 \text{ lbm/sec}$



(g) $\dot{W} = 19.26 \text{ lbm/sec}$

cm $\overline{\text{0 1 2}}$

FIGURE 78 (continued)

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3. Giamati, Charles C. Jr. and Finger, Harold B., "Design Velocity Distribution in Meridional Plane," Chapter VIII of NASA SP-36, Washington, D. C., 1965.
4. Bowen, John T., Sabersky, Rolf H. and Rannie, Duncan W., "Theoretical and Experimental Investigations of Axial Flow Compressors (Summary Report)," California Institute of Technology, January 1949.
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7. Iura, T. and Rannie, W. D., "Observations of Propagating Stall in Axial-Flow Compressors," California Institute of Technology, April 1953.

APPENDIX A

DETAILS OF FLOW RATE CALIBRATION COMPUTER PROGRAM

This program uses the data obtained from the hot-wire anemometer surveys of the inlet to calculate volume flow rate. Reference velocity for the hot-wire reference setting is obtained from the inlet survey Pitot-static probe mounted at the inlet centerline. Inlet guide vane velocity is obtained from the permanently mounted Pitot-static probe ahead of the inlet guide vanes.

This program assumes that the hot-wire instrument is set to 90 per cent of full scale for the reference velocity at the inlet centerline and that the hot-wire instrument is linear.

Input

Card No.	Format	Fortran	Description
1	12	KKK	Number of runs to be considered.
2	3I3,2I10	M	Number of radial data points - symmetric on either side of centerline (maximum 99)
		MM	Number of readings of total pressure and velocity head taken at the inlet centerline (maximum 99)
		MMM	Number of readings of total pressure and velocity head taken ahead of the inlet guide vanes (maximum 99)

		IRUN	Run number
		ISPEED	Rotor speed (rpm)
3	4F10.4	TI	Temperature in the inlet (°F)
		TW	Temperature in test cell (°F)
		BAR	Barometric pressure (inches Hg.)
		TBAR	Temperature of mercury column of barometer (°F)
4	8F10.4	PT1R	Total pressure at the inlet centerline (inches H ₂ O)
		Q1R	Velocity head at the inlet centerline (inches H ₂ O)
5	8F10.4	PT2R	Total pressure ahead of the inlet guide vanes (inches H ₂ O)
6	8F10.4	Q2R	Velocity head ahead of the inlet guide vanes (inches H ₂ O)
7	8F10.4	R	Radii at which data are taken from the centerline outward - data points must be symmetric on either side of centerline (inches)
8	8F10.4	VRL	Values of velocity ratio of hot-wire anemometer to the left side of centerline looking downstream (dimensionless)

Values of velocity ratio of
hot-wire anemometer to the
right side of centerline
looking downstream
(dimensionless)

Output

The computer program output prints the input data in the same format as they are read in.

The calculated information is presented as follows:

<u>Description</u>	<u>Units</u>
Barometric pressure	(lb/ft ²)
Inlet temperature	(°R)
Volume flow rate	(ft ³ /sec)
Mass flow rate	(lbm/sec)
Velocity at inlet centerline	(ft/sec)
Velocity ahead of inlet guide vanes	(ft/sec)
Mass density at inlet centerline	(lbm/ft ³)
CCC = $\frac{(\text{volume flow rate})}{(\text{velocity ahead of inlet guide vanes})}$	$\frac{(\text{ft}^3/\text{sec})}{(\text{ft/sec})}$

TABLE A-1 LISTING OF PROGRAM FLORAT

```

DIMENSION PT1R(99),Q1R(99),PT2R(99),Q2R(99),R(99),VRL(99),VRR(99),
1 PT1(99),Q1(99),P1(99),RH01(99),V(99),PT2(99),Q2(99),P2(99),RH02(99)
2)
G=32.16
RGAS=53.35
READ(5,1)KKK
1 FORMAT(I2)
1 DO 2 I=1,KKK
3 READ(5,3)M,MM,MMM,IRUN,ISPEED
3 FORMAT(3I3,2I10)
4 READ(5,4)TI,TW,BAR,TBAR
4 FORMAT(4F10.4)
5 READ(5,5)(PT1R(I),Q1R(I),I=1,MM)
5 FORMAT(8F10.4)
6 READ(5,5)(PT2R(I),I=1,MMM)
6 READ(5,5)(Q2R(I),I=1,MMM)
6 READ(5,5)(R(I),I=1,M)
6 READ(5,5)(VRL(I),I=1,M)
6 READ(5,5)(VRR(I),I=1,M)
WRITE(6,14)
14 FORMAT(1H1)
WRITE(6,3)M,MM,MMM,IRUN,ISPEED
WRITE(6,4)TI,TW,BAR,TBAR
WRITE(6,5)(PT1R(I),Q1R(I),I=1,MM)
WRITE(6,5)(PT2R(I),I=1,MMM)
WRITE(6,5)(Q2R(I),I=1,MMM)
WRITE(6,5)(R(I),I=1,M)
WRITE(6,5)(VRL(I),I=1,M)
WRITE(6,5)(VRR(I),I=1,M)
GWRM=.99837633+1.0605756*TW/10000.-1.593186*TW**2/1000000.
GHGRM=13.63905-.0013630303*TBAR
CHGC=.4891585*GHGRM/13.54*144.
PAMB=BAR*CHGC
TI=TI+459.7
TOTAL=0.
DO 6 I=1,MM
PT1(I)=PT1R(I)*GWRM/12.*62.42732+PAMB
Q1(I)=Q1R(I)*GWRM/12.*62.42732
P1(I)=PT1(I)-Q1(I)
RH01(I)=P1(I)/(RGAS*TI*G)
V1=SQRT(2.*Q1(I)/RH01(I))
TOTAL=TOTAL+V1
6 CONTINUE
RMM=MM
V1=TOTAL/RMM

```

TABLE A-1 (continued)

```

DO 7 I=1,M
V(I)=(VRL(I)+VRR(I))/2.*V1/.9
7 CONTINUE
R(M+1)=18.
TOTAR=V(I)*3.1416*(R(2)/2.)**2/144.
K=M-1
DO 8 I=2,K
SEGAR=V(I)*3.1416*((R(I)+R(I+1))/2.)**2-((R(I)+R(I-1))/2.)**2)/144.
14. TOTAR=TOTAR+SEGAR
CONTINUE
8 SEGAR=V(M)*3.1416*(R(M+1)**2-((R(M)+R(M-1))/2.)**2)/144.
TOTAR=TOTAR+SEGAR
VOLFL=TOTAR
TOTAR=0.
DO 9 I=1,MMM
PT2(I)=PT2R(I)*GWRM/12.*62.42732+PAMB
Q2(I)=Q2R(I)*GWRM/12.*62.42732
P2(I)=PT2(I)-Q2(I)
RHO2(I)=P2(I)/(RGAS*TI*G)
V2=SQRT(2.*Q2(I)/RHO2(I))
TOTAR=TOTAR+V2
9 CONTINUE
RMMM=MMM
V2=TOTAR/RMMM
CCC=VOLFL/V2
TOTAR=0.
DO 10 I=1,MM
TOTAR=TOTAR+RH01(I)
10 CONTINUE
WDOT=VOLFL*TOTAR/RMM*G
GRH01=TOTAR/RMM*G
WRITE(6,11)
11 FORMAT(' NAVAL POSTGRADUATE SCHOOL',' TURBO-PROPULSION LABORATORY',
1/5X,' CNR COMPRESSOR',' 5X,' FLOW CALIBRATION',' )
WRITE(6,12) IRUN, ISPEED, PAMB, TI
12 FORMAT(' RUN NUMBER',' I3, I10,' RPM',' BAROMETRIC PRESSURE='F10.4,'
1PSFA INLET TEMPERATURE='F10.4,' DEG-R')
WRITE(6,13) VOLFL, WDOT, CCC
13 FORMAT(' VOLUME FLOW RATE='F10.4,' FT3/SEC MASS FLOW RATE='F10.4
1,' LBM/SEC CCC='F10.4,' FT3/SEC PER FT/SEC')
WRITE(6,16) V1, V2, GRH01
16 FORMAT(' VELOCITY AT INLET CENTERLINE='F10.4,' FT/SEC',' VELOCITY
1AHEAD OF INLET GUIDE VANES='F10.4,' FT/SEC',' MASS DENSITY IN INLET
2='F10.4,' LBM/FT3')

```


TABLE A-1 (continued)

```
15 WRITE(6,15)  
    FORMAT(1H1)  
    2 CONTINUE  
    STOP  
    END
```


APPENDIX B

DETAILS OF FLOW PROPERTIES COMPUTER PROGRAM

This program uses the total pressure, total temperature, velocity head, velocity ratio from the hot-wire anemometer, and absolute flow angle data obtained from the radial surveys downstream of rotor blade rows and calculates flow properties based on the NISRE solution, flow probe velocity and hot-wire anemometer velocity. The NISRE solution also requires total pressure and velocity head data from the permanent Pitot-static probe ahead of the inlet guide vanes in order to calculate mass flow rate.

Input

Card No.	Format	Fortran	Description
1	I2	KKK	Number of sets of data to be read.
2	3I3,7F10.3	IRUN	Run number
		MD	Number of radial data points (maximum 50)
		N	Number of radial points required from NISRE solution (maximum 100)
		BAR	Barometric pressure (inches Hg.)
		TBAR	Temperature of mercury column of barometer (°F)
		RPM	Rotor speed (rpm)
		BKG	Assumed gross weight flow blockage factor ($BKG \leq 1$)

		GAM	Specific heat ratio (dimensionless)
		RGAS	Gas constant (ft-lb)/lbm-°R)
		FARB	Arbitrary multiplication factor for reference axial velocity in NISRE solution, required to start Newton Raphson iteration $(1 < \text{FARB} \leq 1.2)$
3	6F10.3,3I3	VA1	Reference axial velocity at root mean square radius for NISRE solution, which must be estimated within 50 per cent of true value (ft/sec)
		ACC	Accuracy to which the NISRE solution is to match the actual flow rate. $(\text{ACC} \quad \left 1 - \frac{\text{Flow rate calculated}}{\text{Actual flow rate}} \right ,$ $0 < \text{ACC} \leq .00001)$
		TW	Temperature in the test cell (°F)
		TI	Inlet air temperature (°F)
		RO	Outer radius of the annulus (inches)
		RI	Inner radius of the annulus (inches)

		MMM	Number of readings of total pressure and velocity head taken ahead of the in- let guide vanes (maximum 50)
		NREF	The number of the data point at which the hot wire anemome- ter was set to 90 per cent, counting from the hub outward.
		NS	Stage number
4	8F10.3	PTIR	Total pressure ahead of the inlet guide vanes (inches (H ₂ O)
		QIR	Velocity head ahead of the inlet guide vanes (inches H ₂ O)

The remaining input data are from the radial surveys downstream of a particular rotor. Data must be entered into the program from the hub outward, one card per radial station.

5	6F10.4	PTR	Total pressure (inches H ₂ O)
		QR	Velocity head (inches H ₂ O)
		TTR	Total temperature (milli- volts determined from an iron-constantan thermocouple with a 32°F reference junc- tion)

ALPHA	Absolute flow angle, taken positive from the axial direction to the direction of rotation (degrees)
VR	Velocity ratio from hot-wire anemometer (dimensionless)
R	Radius (inches)

Output

The computer program output gives the input data in the same format as read in for the purpose of checking input data for errors.

The major part of the output is divided into three sections, the NISRE, flow probe, and hot-wire calculations respectively. The calculated data for each of the three methods are presented in dimensional and in dimensionless form. The method used to obtain the dimensionless quantities is described in Section 8.

Dimensional Form

Name	Description
RADIUS	(inches)
PT	Total pressure (psfa)
P	Static pressure (psfa)
TT	Total temperature ($^{\circ}$ R)
T	Static temperature ($^{\circ}$ R)
V	Absolute velocity (ft/sec)
VA	Axial component of absolute velocity (ft/sec)
VU	Peripheral component of absolute velocity (ft/sec)
VMACH	Mach number of absolute velocity based on calculated static temperature (dimensionless)

W	Relative velocity (ft/sec)
WA	Axial component of relative velocity (ft/sec)
WU	Peripheral component of relative velocity (ft/sec)
WMACH	Mach number of relative velocity based on calculated static temperature (dimensionless)
U	Peripheral velocity (ft/sec)
ALPHA	Angle of absolute velocity - positive from the axial direction to the direction of rotation (degrees)
BETA	Angle of relative velocity - positive from the axial direction to the direction of rotation (degrees)

Dimensionless Form

All velocities are made dimensionless by dividing by the peripheral tip velocity (U_T). All temperatures are made dimensionless by dividing by the compressor inlet temperature.

R/RO	Radius ratio - Radius divided by tip radius
DPT/RHO*UT **2	$(P_t - P_a) / (\frac{1}{2} \rho U_T^2)$
DP/RHO*UT **2	$(P - P_a) / (\frac{1}{2} \rho U_T^2)$
PHIAV	Numerical average of the dimensionless axial velocity components.

TABLE B-1 LISTING OF PROGRAM FLOW

```

REAL*8 RD,TTD,PTD,ALPHD,BT,BP,BA,TL,CL,AL,YL,RDN
DIMENSION DELY(99),SB(6),TL(6),ST(6),CL(6),SC(6),AL(30,30),WL(99),
1YL(99),RD(99),TTD(99),PTD(99),ALPHD(99),BT(6),BA(6),RDN(100),
2PT(50),TT(50),ALPH(100),RN(100),V(100),VA(100),VU(100),W(100),WA(
3100),WU(100),BETA(100),VMACH(100),WMACH(100),U(100),T(100),P(100),
4PTIR(50),QIR(50),PTR(50),QR(50),TTR(50),ALPHA(50),VR(50),R(50),TTN
5(100),PTN(100),QM(50),PM(50)
READ(5,6)KKK
6FORMAT(12)
DO 100 KI=1,KKK
READ(5,1)IRUN,MD,N,BAR,TBAR,RPM,BKG,GAM,RGAS,FARB
1FORMAT(3I3,7F10.3)
READ(5,2)VAL,ACC,TW,TI,RO,RI,MMM,NREF,NS
2FORMAT(6F10.3,3I3)
READ(5,9)(PTIR(I),QIR(I),I=1,MMM)
9FORMAT(8F10.3)
READ(5,3)(PTR(I),QR(I),TTR(I),ALPHA(I),VR(I),R(I),I=1,MD)
3FORMAT(6F10.4)
WRITE(6,1)IRUN,MD,N,BAR,TBAR,RPM,BKG,GAM,RGAS,FARB
WRITE(6,2)VAL,ACC,TW,TI,RO,RI,MMM,NREF,NS
WRITE(6,3)(PTR(I),QR(I),TTR(I),ALPHA(I),VR(I),R(I),I=1,MD)
WRITE(6,9)(PTIR(I),QIR(I),I=1,MMM)
CALL CONVER(PTR,QIR,PTI,QI,PI,TTR,TT,PTR,QR,PT,QM,PM,BAR,TBAR,MD,
1TW,MMM,PAMB)
WRITE(6,4)PTI,QI,PI
4FORMAT(3F10.3)
WRITE(6,5)(TT(I),PT(I),QM(I),PM(I),I=1,MD)
5FORMAT(4F10.3)
CALL FLOW(TI,PI,QI,WDES,RGAS)
WRITE(6,7)WDES
7FORMAT(1WDES=F10.4'LBM/SEC'//)
DO 8 I=1,MD
PTD(I)=PT(I)
TTD(I)=TT(I)
ALPHD(I)=ALPHA(I)
RD(I)=R(I)
8CONTINUE
IW=0
ISW=1
LP=0
KM=4
CALL LSQPOL(MD,KM,IW,ISW,LP,SIGMA,RD,PTD,WL,YL,DELY,BP,SB,TL,ST,C,
1SC,AL)
CALL LSQPOL(MD,KM,IW,ISW,LP,SIGMA,RD,TTD,WL,YL,DELY,BT,SB,TL,ST,C,
1SC,AL)

```

TABLE B-1 (continued)

```

CALL LSQPOL(MD,KM,IW,ISW,LP,SIGMA,RD,ALPHD,WL,YL,DELY,BA,SB,TL,ST,
1C,SC,AL)
CALL RADDET(RO,RI,N,M,RDN,RN)
WRITE(6,200)(RN(I),I=1,N)
FORMAT(12F10.5)
200 WRITE(6,201)M
201 FORMAT(14)
CALL POLRET(N,BP,RDN,PTN)
CALL POLRET(N,BT,RDN,TTN)
CALL POLRET(N,BA,RDN,ALPH)
1ETA,WCALC,BKG,VMACH,WMACH,U,T,P,IN,M,RGAS,GAM,N)
IF(IN.EQ.1)STOP
JJ=1
CALL OUTPUT(PTN,P,TTN,T,V,VA,VU,VMACH,W,WA,WU,WMACH,RN,U,ALPH,BETA
1,WDES,BKG,RPM,IRUN,PAMB,TI,JJ,N,NS)
CALL NONDIM(PTN,P,TTN,T,V,VA,VU,VMACH,W,WA,WU,WMACH,RN,U,ALPH,BETA
1,PAMB,TI,N,IRUN)
CALL PITOT(PM,QM,RGAS,GAM,ALPHA,BETA,TT,T,V,VA,VU,W,WA,WU,VMACH,WM
1ACH,U,MD,RPM,R)
JJ=3
CALL OUTPUT(PT,PM,TT,T,V,VA,VU,VMACH,W,WA,WU,WMACH,R,U,ALPHA,BETA,
1WDES,BKG,RPM,IRUN,PAMB,TI,JJ,MD,NS)
CALL NONDIM(PT,PM,TT,T,V,VA,VU,VMACH,W,WA,WU,WMACH,R,U,ALPHA,BETA,
1PAMB,TI,MD,IRUN)
CALL HOTWIR(NREF,VR,GAM,RGAS,RPM,ALPHA,V,VA,VU,T,VMACH,U,W,WA,WU,W
1MACH,BETA,MD,R,TT,P,PT)
JJ=2
CALL OUTPUT(PT,P,TT,T,V,VA,VU,VMACH,W,WA,WU,WMACH,R,U,ALPHA,BETA,
1WDES,BKG,RPM,IRUN,PAMB,TI,JJ,MD,NS)
CALL NONDIM(PT,P,TT,T,V,VA,VU,VMACH,W,WA,WU,WMACH,R,U,ALPHA,BETA,P
1AMB,TI,MD,IRUN)
100 CONTINUE
STOP
END

SUBROUTINE CONVER(PTIR,QIR,PTI,QI,PI,TTR,TT,PTR,QR,PT,QM,PM,8AR,TR
1AR,MD,TW,MMM,PAMB)
DIMENSION TT(1),PT(1),QM(1),PM(1),TTR(1),PTR(1),QR(1),PTIR(1),QIR(
11)
GWRM=.99837633+1.0605756*TW/10000.-1.5931861*TW**2/1000000.

```

TABLE B-1 (continued)

```

GHGRM=13.63905-.0013630303*TBAR
CHGC=.4891585*GHGRM/13.54*144.
FAMB=BAR*CHGC
DO 1 I=1,MD
TEMP=32.+39.98*TTR(I)-.435*TTR(I)**2
TI(I)=TEMP+459.7
PT(I)=PIR(I)*GWRM/12.*62.42732+PAMB
QM(I)=QR(I)*GWRM/12.*62.42732*1.09
PM(I)=PT(I)-QM(I)
1 CONTINUE
SUM1=0.
SUM2=0.
SUM3=0.
DO 2 I=1,MMM
PTI=PTIR(I)*GWRM/12.*62.42732+PAMB
QI=QIR(I)*GWRM/12.*62.42732
PI=PTI-QI
SUM1=SUM1+PTI
SUM2=SUM2+QI
SUM3=SUM3+PI
2 CONTINUE
RMMM=MMM
PTI=SUM1/RMMM
QI=SUM2/RMMM
PI=SUM3/RMMM
RETURN
END

```

```

SUBROUTINE FLOW(TI,PI,QI,WDES,RGAS)
TIA=TI+459.7
RHOI=PI/(RGAS*TIA*32.17)
CCC=4.405
VI=SQRT(2.*QI/RHOI)
VF=CCC*VI
WDES=RHOI*32.17*VF
RETURN
END

```


TABLE B-1 (continued)

```

SUBROUTINE RADDET(RO,RI,N,M,RDN,R)
REAL*8 RDN
DIMENSION RDN(1),R(1),A(100)
RMS=14.8432
RN=N-1
DR=(RO-RI)/RN
R(1)=RMS
I=2
1 R(I)=R(I-1)-DR
  IF(R(I).LT.RI)GO TO 2
  I=I+1
  GO TO 1
2 R(I)=RI
  M=I
  DO 3 I=1,M
    A(I)=R(M-I+1)
3 CONTINUE
  DO 4 I=1,M
    R(I)=A(I)
4 CONTINUE
  I=M+1
5 R(I)=R(I-1)+DR
  IF(R(I).GT.RO)GO TO 6
  I=I+1
  GO TO 5
6 R(I)=RO
  IF(I.GT.N)R(I-1)=RO
  DO 7 I=1,N
    RDN(I)=R(I)
7 CONTINUE
  RETURN
END

SUBROUTINE LSOPOL(M,KM,IW,ISW,LP,SIGMA,X,F2,W,Y,DELY,B,SB,T,ST,C,
1 SC,A)
REAL*8 X,F2,Y,B,T,C,A,F,P,BM,D,FBAR,XBAR,PXF,PXP,XPXP,XPXP,XP,
1 ALPHA,BETA,PPXF,PPXPP,PT,VARA,POLYE1
DIMENSION S(30),X(1),F2(1),ST(1),SB(1),F(100),PM(100),P(100),R(1),
1 DELY(1),W(1),A(30,30),T(1),Y(1),BM(11,11),D(11,11),C(1),SC(1)
DO 7 I=1,11

```

TABLE B-1 (continued)

```

00 4 J=1,11
D(I,J)=0.0D0
4 CONTINUE
7 CONTINUE
9 LL=0
FM=0.0
SUMEV2=0.0
A(1,1)=1.0
A(2,2)=1.0
FBAR=0.0
XBAR=0.0
DO10 I=1,M
IF(IW)1009,1010,1009
1010 W2=1.0
W(I)=1.0
GOTO1011
1009 W2=SQRT(W(I))
1011 FM=FM+W(I)
F(I)=W2*F2(I)
PM(I)=W2
FBAR=FBAR+F(I)*PM(I)
10 XBAR=XBAR+X(I)*PM(I)**2
XBAR=XBAR/FM
T(1)=FBAR/FM
A(2,1)=-XBAR
PXF=0.0
PXP=0.0
DO20 I=1,M
P(I)=(X(I)-XBAR)*PM(I)
PXF=PXF+P(I)*F(I)
PXP=PXP+P(I)*P(I)
20 T(2)=PXF/PXP
PMXPM=FM
S(1)=PMXPM
KM=KM+1
B(1)=T(1)*A(1,1)+T(2)*A(2,1)
B(2)=T(2)*A(2,2)
60 DO190K=2,KM
IF(K-2)40,165,65
40 WRITE(6,4000)
4000 FORMAT(7HSTOP 40)
65 STOP
XPXP=0.0
XPXPM=0.0
B(K)=0.0

```

TABLE B-1 (continued)

```

D070J=1,M
XP=X(J)*P(J)
70  XXP=XPXP+XP*P(J)
    ALPHAX=XPXP/PPX
    BETA=XPXPM/PMXPM
    PPXF=0.0
    PPXPP=0.0
D090I=1,M
PT=P(I)
80  P(I)=X(I)*PT-ALPHA*PT-BETA*PM(I)
81  PPXF=PPXF+P(I)*F(I)
82  PPXPP=PPXPP+P(I)*P(I)
83  PM(I)=PT
90  T(K)=PPXF/PPXPP
    PMXPM=PPX
    PXP=PPXPP
    A(K,1)=-ALPHA*A(K-1,1)-BETA*A(K-2,1)
    A(K,K-1)=A(K-1,K-2)-A(K-1,K-1)*ALPHA
    A(K,K)=1.0
    IF(K-3)150,150,110
110 K1=K-2
    D0120I=2,K1
120 A(K,I)=A(K-1,I-1)-ALPHA*A(K-1,I)-BETA*A(K-2,I)
150 D0160I=1,K
160 B(I)=B(I)+T(K)*A(K,I)
165 SIG3=0.0
    D0180I=1,M
    Y(I)=POLYE1(X(I),K,B)
175 DELY(I)=Y(I)-F2(I)
180 SIG3 = SIG3 + (DELY(I)**2)*W(I)
    SIG3=SIG3/FM
    SIG2=SIG3*FLOAT(M)/FLOAT(M-K)
    IF(K-2)40,1650,1651
1650 FLEV = 0.
    GO TO 1652
1651 FLEV=(SUMEV2-SIG3)/SIG2
1652 SUMEV2=SIG3
    SIGMA=SQRT (SIG2)
    S(K) = PXP
D0499I=1,K
499 ST(I)=SIGMA/SQRT(S(I))
D0501I=1,K
SB(I)=0.0
D0500J=1,K

```

TABLE B-1 (continued)

```

500 SB(I)=SB(I)+(A(J,I)*ST(J))**2
501 SB(I)=SQRT(SB(I))
658 IF(LP)658,183,658
651 IF(K-2)652,651,652
D(1,1)=1.000
D(2,2)=1.000
D(3,3)=1.500
D(3,2)=0.000
D(3,1)=-0.500
D(4,4)=3.500
D(4,3)=0.000
D(4,2)=-1.500
D(4,1)=0.000
D(5,5)=35.000/8.000
D(5,4)=0.000
D(5,3)=-30.000/8.000
D(5,2)=0.000
D(5,1)=3.000/8.000
D(6,6)=63.000/8.000
D(6,5)=0.000
D(6,4)=-70.000/8.000
D(6,3)=15.000/8.000
D(7,7)=231.000/16.000
D(7,5)=-315.000/16.000
D(7,3)=105.000/16.000
D(7,1)=-5.000/16.000
D(8,8)=429.000/16.000
D(8,6)=-693.000/16.000
D(8,4)=315.000/16.000
D(8,2)=-35.000/16.000
D(9,9)=6435.000/128.000
D(9,7)=-12012.000/128.000
D(9,5)=6930.000/128.000
D(9,3)=-1260.000/128.000
D(9,1)=35.000/128.000
D(10,10)=12155.000/128.000
D(10,8)=-25740.000/128.000
D(10,6)=18018.000/128.000
D(10,4)=-4620.000/128.000
D(10,2)=315.000/128.000
D(11,11)=46189.000/256.000
D(11,9)=-109395.000/256.000
D(11,7)=90090.000/256.000
D(11,5)=-30030.000/256.000

```

TABLE B-1 (continued)

```

D(11,3)=3465.000/256.000
D(11,1)=-63.000/256.000
652 D0700 I1=1,K
    J=K-I1+1
    VARA=0.0
    I1=K-J
    IF(I1) 702,701,702
702 D0703 JJ=1,I1
    JK=K-JJ+1
703 VARA=VARA+D(JK,J)*BM(K,JK)
701 BM(K,J)=(A(K,J)-VARA)/D(J,J)
    IF(K-2) 700,704,700
704 BM(1,1)=A(1,1)/D(1,1)
700 CONTINUE
705 D0708 I=1,K
    C(I)=0.0
    SC(I)=0.0
    D0707 J=1,K
    C(I)=C(I)+BM(J,I)*T(J)
707 SC(I)=SC(I)+(BM(J,I)*ST(J))**2
708 SC(I)=SC(I)+BM(J,I)*ST(J)**2
183 CONTINUE
192 WRITE(6,600) (I,B(I),SB(I),I=1,K)
185 WRITE(6,186) SIGMA,FLEV,SUMEV2
    WRITE(6,601) (I,T(I),ST(I),I=1,K)
    IF(LP) 187,670,187
187 WRITE(6,188)
    WRITE(6,602) (I,C(I),SC(I),I=1,K)
670 WRITE(6,2)
    WRITE(6,603) (I,X(I),F2(I),Y(I),DELY(I),W(I),I=1,M)
190 CONTINUE
211 IF(ISW) 210,220,210
210 D0215 I=2,KM
215 WRITE(6,5) I,(A(I,J),J=1,I)
220 KM=KM-1
    RETURN
1 FORMAT(3H B(OP12,2H)=1PE15.7,6H ERRB=E10.3,3H B(OP12,2H)=1PE15.7,
16H ERRB=E10.3,3H B(OP12,2H)=1PE15.7,6H ERRB=E10.3)
2 FORMAT(4H0 I,11X 4HX(I) 12X4HF(I) 12X7HDELY(I) 10X4HW(I) /)
5 FORMAT(36H0 ORTHOGONAL POLYNOMIAL COEFF FOR K=I5/(1P8E15.6))
186 FORMAT(7H0 SIGMA=1PE16.7,9H F LEVEL=1PE16.7,12H SUM SQ DEV=,1PF16.7
* // 45H COEFFICIENTS OF Y=T1*P1+T2*P2+ETC AND
1 ERRORS/)
188 FORMAT(23H0 LEGENDRE POLYNOMIALS/45H COEFFICIENTS OF Y=C1*L1+C2*L

```


TABLE B-1 (continued)

```

12+ETC AND ERRORS/)
600 FORMAT(41H1COEFFICIENTS OF Y=B1+B2*X+ETC AND ERRORS/)
601 FORMAT(3H T(12,2H)=1PE15.7,6H ERRT=E10.3,3H T(OPI2,2H)=1PE15.7,6H
1ERRT=E10.3,3H T(OPI2,2H)=1PE15.7,6H ERRT=E10.3)
602 FORMAT(3H C(12,2H)=1PE15.7,6H ERRC=E10.3,3H C(OPI2,2H)=1PE15.7,6H
1ERRC=E10.3,3H C(OPI2,2H)=1PE15.7,6H ERRC=E10.3)
603 FORMAT(16,1P5E16.7)
END

```

```

REAL FUNCTION POLYE1*8(X,K,B)

```

```

REAL*8 X,B,S
DIMENSION B(30)

```

```

10 S=B(K)

```

```

20 KK=K-1

```

```

30 DO 40 I=1,KK

```

```

40 IK=K-I

```

```

S=X*S+B(IK)

```

```

POLYE1=S

```

```

RETURN

```

```

END

```

```

SUBROUTINE POLRET(N,C,R,VAL)

```

```

REAL*8 C,R,V

```

```

DIMENSION C(1),R(1),V(100),VAL(1)

```

```

DO 1 I=1,N

```

```

V(I)=C(1)+C(2)*R(I)+C(3)*R(I)**2+C(4)*R(I)**3+C(5)*R(I)**4

```

```

VAL(I)=V(I)

```

```

1 CONTINUE

```

```

RETURN

```

```

END

```

```

SUBROUTINE NISRE(PT,TT,WDES,ALPH,R,VAL,FARB,ACC,SPEED,V,VA,VU,W,WA
1,WU,BETA,WCALC,BKG,ZACH,WMACH,U,T,P,IN,M,RGAS,GAM,N)

```

```

DIMENSION PT(1),TT(1),ALPH(1),R(1),V(1),VA(1),VU(1),WA(1),WU(
1),BETA(1),ZACH(1),WMACH(1),U(1),TANAL(100),EF(100),GRHD(100),P(1
2),T(1)

```

```

IN=0

```

```

IP=0

```

TABLE B-1 (continued)

```

G=32.16
GAM1=1./((GAM-1.))
GAM2=((GAM-1.)/(2.*GAM))
GAM3=GAM*GAM1
BKSF=BKG*2.*3.1416
DO 400 I=1,N
ALP=ALPH(I)/57.296
TANAL(I)=TAN(ALP)
U(I)=3.1416/360.*SPEED*R(I)
400 CONTINUE
MP1=M+1
DO 401 I=MP1,N
EF(I)=ALOG((TT(I)/TT(I-1))*GAM3/(PT(I)/PT(I-1)))
401 MM1=M-1
DO 430 I=1,MM1
EF(I)=ALOG((TT(I)/TT(I+1))*GAM3/(PT(I)/PT(I+1)))
430 EF(M)=0.
FIRST=0.
KOUNT=0
VA(M)=VA1
VU(M)=VA(M)*TANAL(M)
VF=VA(M)**2+VU(M)**2
V(M)=SQRT(VF)
GRHO(M)=(PT(M)/(RGAS*TT(M)))*(1.-GAM2*VF/(G*RGAS*TT(M)))*GAM1
ZACH(M)=SORT(VF/(GAM*G*RGAS*(TT(M)-(GAM2*VF/(G*RGAS))))))
RAKM=GRHO(M)*VA(M)*R(M)/12.
RAK1=RAKM
END OF MEAN LINE CALCULATIONS
TOTAR=0.
DO 403 I=MP1,N
F=EF(I)
TERM1=2.*G*RGAS*GAM3*(TT(I)-TT(I-1))
TERM2=F*G*RGAS*(TT(I)+TT(I-1))
TERM3=VA(I-1)**2*(F*GAM2+1.)
TERM4=VU(I-1)**2*(F*GAM2+2.-R(I)/R(I-1))
SUM1=TERM1-TERM2+TERM3+TERM4
TERM5=1.-F*GAM2
TERM6=TANAL(I)**2*(2.-R(I-1)/R(I)-F*GAM2)
SUM2=TERM5+TERM6
VASQ=SUM1/SUM2
VA(I)=SQRT(VASQ)
VFN=VA(I)**2*(1.+TANAL(I)**2)
VU(I)=VA(I)*TANAL(I)
V(I)=SQRT(VFN)
GRHO(I)=(PT(I)/(RGAS*TT(I)))*(1.-GAM2*VFN/(G*RGAS*TT(I)))*GAM1

```

C

TABLE B-1 (continued)

```

403 ZACH(I)=SQRT(VFN/(GAM*G*RGAS*(TT(I)-(GAM2*VFN/(G*RGAS))))
    DELTR=(R(I)-R(I-1))/12.
    RAK2=GRHO(I)*VA(I)*R(I)/12.
    SEGAR=(RAK1+RAK2)*DELTR*.5
    TOTAR=TOTAR+SEGAR
    RAK1=RAK2
    CONTINUE
    RAK1=RAKM
    I=M-1
431 F=EF(I)
    TERM1=2.*G*RGAS*GAM3*(TT(I)-TT(I+1))
    TERM2=F*G*RGAS*(TT(I)+TT(I+1))
    TERM3=VA(I+1)**2*(F*GAM2+1.)
    TERM4=VU(I+1)**2*(F*GAM2+2.-R(I)/R(I+1))
    SUM1=TERM1-TERM2+TERM3+TERM4
    TERM5=1.-F*GAM2
    TERM6=TANAL(I)**2*(2.-R(I+1)/R(I)-F*GAM2)
    SUM2=TERM5+TERM6
    VASQ=SUM1/SUM2
    VA(I)=SQRT(VASQ)
    VFN=VA(I)**2*(1.+TANAL(I)**2)
    VU(I)=VA(I)*TANAL(I)
    V(I)=SQRT(VFN)
    GRHO(I)=(PT(I)/(RGAS*TT(I)))/(RGAS*TT(I))*(1.-GAM2*VFN/(G*RGAS*TT(I)))*GAM1
    ZACH(I)=SQRT(VFN/(GAM*G*RGAS*(TT(I)-(GAM2*VFN/(G*RGAS))))
    DELTR=(R(I+1)-R(I))/12.
    RAK2=GRHO(I)*VA(I)*R(I)/12.
    SEGAR=(RAK1+RAK2)*DELTR*.5
    TOTAR=TOTAR+SEGAR
    RAK1=RAK2
    IF(I.EQ.1)GO TO 432
    I=I-1
    GO TO 431
432 WCALC=BKSF*TOTAR
    IF(IP)415,404,415
404 IF(FIRST)406,405,406
405 VZN1=VA(M)
    WN1=WCALC
    TOTAR=0.
    FIRST=1.
    VA(M)=VA(M)*FARB
    GO TO 402
406 VZN2=VA(M)
    DELVZ=VZN2-VZN1
    WN2=WCALC

```

TABLE B-1 (continued)

```

407 DELWC=WN2-WN1
    IF (DELWC) 409, 407, 409
408 IN=1
    WRITE(6, 408)
    FORMAT(' DESIRED FLOW RATE IS NOT HIGH ENOUGH FOR NISRE STATOR SO
    LUTION-PROGRAM STOPPED')
    GO TO 421
409 DELWD=WDES-WN2
    VA(M)=(DELWD*DELVZ/DELWC)+VZN2
    IF (VA(M)) 410, 411, 411
410 VA(M)=0.0
411 CONTINUE
    RATIO=(WCALC/WDES)-1.
    RATIO=ABS(RATIO)
    IF (ACC-RATIO) 412, 419, 419
412 VZN1=VZN2
    WN1=WN2
    TOTAR=0.
    KOUNT=KOUNT+1
    IF (20-KOUNT) 413, 402, 402
413 IN=1
    WRITE(6, 414)
414 FORMAT('NO SOLUTION TO NISRE STATOR FLOW RATE TO ACC. REQUIRED IN
    1 20 ITERATIONS-PROGRAM STOPPED')
    GO TO 421
415 K=1
420 DO 418 I=1, N
    WSQ=(VU(I)-U(I))**2+VA(I)**2
    W(I)=SQRT(WSQ)
    WA(I)=VA(I)
    WU(I)=VU(I)-U(I)
    BETA(I)=ARCSIN((VU(I)-U(I))/W(I))
    BETA(I)=BETA(I)*57.296
    IF (ABS(BETA(I))-180.) 417, 417, 416
416 BETA(I)=BETA(I)-360.
417 CONTINUE
    T(I)=TT(I)-V(I)**2/(2.*G*RGAS*GAM3)
    P(I)=GRHO(I)*RGAS*T(I)
    AS=SQRT(GAM*G*RGAS*T(I))
    WMACH(I)=W(I)/AS
418 CONTINUE
    GO TO (404, 421), K
419 K=2
    GO TO 420
421 CONTINUE

```

TABLE B-1 (continued)

RETURN
END

```

SUBROUTINE PITOT(PM,QM,RGAS,GAM,ALPHA,BETA,TT,T,V,VA,VU,W,WA,WU,VM
1ACH,WMACH,U,MD,SPEED,R)
  DIMENSION PM(1),QM(1),ALPHA(1),BETA(1),TT(1),T(1),V(1),VA(1),VU(1)
  1,W(1),WA(1),WU(1),WMACH(1),U(1),P(1)
  G=32.17
  DO 3 I=1,MD
    ALP=ALPHA(I)/57.296
    ALSIN=SIN(ALP)
    ALCOS=COS(ALP)
    VSQ=2.*G*RGAS*QM(I)*TT(I)/(PM(I)+(GAM-1.)/GAM*QM(I))
    V(I)=SQRT(VSQ)
    T(I)=TT(I)-VSQ/(2.*G*(GAM/(GAM-1.))*RGAS)
    VA(I)=V(I)*ALCOS
    VU(I)=V(I)*ALSIN
    AS=SQRT(GAM*G*RGAS*TT(I))
    VMACH(I)=V(I)/AS
    U(I)=3.1416/360.*SPEED*R(I)
    WSQ=(VU(I)-U(I))**2+VA(I)**2
    W(I)=SQRT(WSQ)
    BETA(I)=ARCSIN((VU(I)-U(I))/W(I))
    BETA(I)=BETA(I)*57.296
    IF(ABS(BETA(I))-180.)1,1,2
    BETA(I)=BETA(I)-360.
  2 CONTINUE
  1 WA(I)=VA(I)
  WU(I)=VU(I)-U(I)
  WMACH(I)=W(I)/AS
  3 CONTINUE
  RETURN
  END

```

```

SUBROUTINE HOTWIR(NREF,VR,GAM,RGAS,SPEED,ALPHA,V,VA,VU,T,VMACH,U,W
1,WA,WU,WMACH,BETA,MD,R,TT,P,PT)
  DIMENSION VR(1),ALPHA(1),V(1),VA(1),VU(1),T(1),VMACH(1),U(1),W(1),

```


TABLE B-1 (continued)

```

1 WA(1), WU(1), WMACH(1), BETA(1), R(1), TT(1), P(1), PT(1)
  GAM2=(GAM-1.)/(2.*GAM)
  VREF=V(NREF)
  G=32.17
  DO 3 I=1, MD
    ALP=ALPHA(I)/57.296
    ALSIN=SIN(ALP)
    ALCOS=COS(ALP)
    V(I)=VR(I)*VREF/.9
    VF=V(I)**2
    GRHO=(PT(I)/(RGAS*TT(I)))*(1.-GAM2*VF/(G*RGAS*TT(I)))*(1./(GAM-1.
1))
    VA(I)=V(I)*ALCOS
    VU(I)=V(I)*ALSIN
    T(I)=TT(I)-V(I)**2/(2.*G*(GAM/(GAM-1.))*RGAS)
    P(I)=GRHO*RGAS*T(I)
    AS=SQRT(GAM*G*RGAS*T(I))
    VMACH(I)=V(I)/AS
    U(I)=3.1416/360.*SPEED*R(I)
    WSQ=(VU(I)-U(I))**2+VA(I)**2
    W(I)=SQRT(WSQ)
    BETA(I)=ARSIN((VU(I)-U(I))/W(I))
    BETA(I)=BETA(I)*57.296
    IF(ABS(BETA(I))-180.)1,1,2
2  BETA(I)=BETA(I)-360.
1  CONTINUE
  WA(I)=VA(I)
  WU(I)=VU(I)-U(I)
  WMACH(I)=W(I)/AS
3  CONTINUE
  RETURN
  END

SUBROUTINE OUTPUT(PT,P,TT,T,V,VA,VU,VMACH,W,WA,WU,WMACH,R,U,ALPHA,
1 BETA,WDES,BKG,RPM,IRUN,PAMB,TT,MM,NP,NS)
  DIMENSION PT(1),P(1),TT(1),T(1),V(1),VA(1),VU(1),VMACH(1),W(1),WA(
1),WU(1),WMACH(1),R(1),U(1),ALPHA(1),BETA(1)
  WRITE(6,1)
1  FORMAT(1H1,50X, NAVAL POSTGRADUATE SCHOOL, /54X, MONTEREY, CALIFORN
1 1A,/)
  GO TO (2,3,4),MM

```

TABLE B-1 (continued)

```

2 WRITE(6,5)
5 FORMAT(28X,' RADIAL FLUID CONDITIONS BASED ON NON-ISENTROPIC RADIAL
1 EQUILIBRIUM EQUATION',/28X,' WITH INPUT OF TOTAL TEMPERATURE, TOTAL
1 PRESSURE, ALPHA AND MASS FLOW RATE'//)
6 WRITE(6,6)BKG
6 FORMAT(' ASSUMED BLOCKAGE FACTOR='F5.4//)
GO TO 9
3 WRITE(6,7)
7 FORMAT(39X,' RADIAL FLUID CONDITIONS BASED ON HOT WIRE INFORMATION'
1/37X,' WITH INPUT OF TOTAL TEMPERATURE, TOTAL PRESSURE AND ALPHA'//)
GO TO 9
4 WRITE(6,8)
8 FORMAT(37X,' RADIAL FLUID CONDITIONS BASED ON PITOT STATIC INFORMAT
1ION',/45X,' WITH INPUT OF TOTAL TEMPERATURE AND ALPHA'//)
9 WRITE(6,10)IRUN,RPM,WDES,PAMB,TI,NS MASS FLOW RATE='F10.4' LBM/SE
10 FORMAT(' RUN NUMBER',I3,F10.1,' RPM INLET TEMPERATURE='F10.4' DE
1C'/' BAROMETRIC PRESSURE='F10.4'PSFA DOWNSTREAM OF ROTOR NUMBER',I2//)
2G-F'/'
6 WRITE(6,11)
11 FORMAT(' RADIUS(IN) PT(PSFA) P(PSFA) W TT(DEG-R) T WU
1 VA VMACH W WA
2 WMACH'//)
WRITE(6,12)(R(I),PT(I),P(I),TT(I),V(I),VA(I),VU(I),VMACH(I),W
1(I),WA(I),WU(I),WMACH(I),I=1,NP)
12 FORMAT(F6.2,8X,F8.3,2X,F8.3,2X,F8.3,2X,F8.3,2X,F8.3,2X,F8.3,2X,F8.
13,2X,F8.3,2X,F8.3,2X,F8.3,2X,F8.3,2X,F8.3)
WRITE(6,13)
13 FORMAT(' RADIUS(IN) ALPHA BETA U'//)
WRITE(6,14)(R(I),ALPHA(I),BETA(I),U(I),I=1,NP)
14 FORMAT(F6.2,2X,F8.3,2X,F8.3,2X,F8.3)
WRITE(6,15)
15 FORMAT(IH1)
CONTINUE
RETURN
END

SUBROUTINE NONDIM(PT,P,TT,T,V,VA,VU,VMACH,W,WA,WU,WMACH,R,U,ALPHA,
1BETA,PBAR,TI,NP,IRUN)
1 DIMENSION PT(1),P(1),TT(1),V(1),VA(1),VU(1),VMACH(1),W(1),WA(
11),WU(1),WMACH(1),R(1),ALPHA(1),BETA(1),PTR(100),PR(100),PTR(
2100),TR(100),VR(100),VAR(100),VUR(100),WR(100),WAR(100),WUR(100),R

```

TABLE B-1 (continued)

[illegible]

TABLE B-2 SAMPLE OF ACCURACY OF POLYNOMIAL FIT OF MEASURED DATA

```

COEFFICIENTS OF Y=H1+H2*X+ETC. AND ERRORS
H( 1)= 1.1893155D 03 FRRH= 2.256E-02 H( 2)= 2.6811451D 02 FRRH= 6.383E-01 R( 3)= -2.960200D 01 FRRH= 6.712E-00
H( 4)= 1.3478942D 00 FRRH= 3.111E-01 H( 5)= -2.3671961D-02 FRRH= 5.361E-03 R(
SIGMA= 2.9211050E-01 F LEVEL= 1.2992601F 00 SUM SQ DEV= 5.6845738E-02
COEFFICIENTS OF Y=T1*P1+T2*P2+ETC AND ERRORS
T( 1)= 2.1260333D 03 ERRT= 7.542E-02 T( 2)= -4.2136928D-02 FRRT= 3.491E-02 T( 3)= -1.1081579D-01 FRRT= 1.819E-02
T( 4)= -2.5079506D-02 ERRT= 9.764E-03 T( 5)= -2.3671961D-02 FRRT= 5.361E-03 T(
I      X(I)      F(I)      Y(I)      DELY(I)      W(I)
1      1.1000000D 01      2.1253596D 03      2.1251750D 03      -1.8450393E-01      1.0000000E 00
2      1.1500000D 01      2.1256658D 03      2.1259460D 03      -2.8027272E-01      1.0000000E 00
3      1.2000000D 01      2.1262778D 03      2.126723D 03      -5.4926053E-03      1.0000000E 00
4      1.2500000D 01      2.1262778D 03      2.1263304D 03      -5.252789F-02      1.0000000E 00
5      1.3000000D 01      2.1262778D 03      2.1262612D 03      -1.6675498E-02      1.0000000E 00
6      1.3500000D 01      2.1262778D 03      2.1261701D 03      -1.0770929E-01      1.0000000E 00
7      1.4000000D 01      2.1262778D 03      2.1261272D 03      -1.5058839E-01      1.0000000E 00
8      1.4500000D 01      2.1262778D 03      2.1261670D 03      -1.1086053E-01      1.0000000E 00
9      1.5000000D 01      2.1262778D 03      2.1262883D 03      -1.04185546E-02      1.0000000E 00
10     1.5500000D 01      2.1262778D 03      2.126454D 03      1.7668557E-01      1.0000000E 00
11     1.6000000D 01      2.1263816D 03      2.1265937D 03      2.1210891E-01      1.0000000E 00
12     1.6500000D 01      2.1264851E 03      2.1265982D 03      1.1311305E-01      1.0000000E 00
13     1.7000000D 01      2.1262778D 03      2.1265250D 03      4.7137567E-02      1.0000000E 00
14     1.7500000D 01      2.1262778D 03      2.1255954D 03      -6.82431942E-01      1.0000000E 00
15     1.8000000D 01      2.1238293D 03      2.1241954D 03      3.6604041E-01      1.0000000E 00

ORTHOGONAL POLYNOMIAL COEFF FOR K= 2
-1.450000D 01 1.00000D 00

ORTHOGONAL POLYNOMIAL COEFF FOR K= 3
2.055833D 02 -2.90000D 01 1.00000D 00

ORTHOGONAL POLYNOMIAL COEFF FOR K= 4
-2.927550D 03 6.22400D 02 -4.35000D 01 1.00000D 00

ORTHOGONAL POLYNOMIAL COEFF FOR K= 5
4.17351D 04 -1.18516D 04 1.249679D 03 -5.80000D 01 1.00000D 00

```

TABLE B-3 SAMPLE OF DIMENSIONAL COMPUTER OUTPUT FOR NISRE PORTION OF PROGRAM FLOW

NAVAL POSTGRADUATE SCHOOL
MONTEREY, CALIFORNIA

RADIAL FLUID CONDITIONS BASED ON NON-ISENTROPIC RADIAL EQUILIBRIUM EQUATION WITH INPUT OF TOTAL TEMPERATURE, TOTAL PRESSURE, ALPHA AND MASS FLOW RATE

ASSUMED BLOCKAGE FACTOR = .96 CO

RUN NUMBER 35 1193.0 RPM MASS FLOW RATE= 26.1730 LHM/SEC
BAROMETRIC PRESSURE= 2114.4355 PSFA INLET TEMPERATURE= 77.9000 DEG-F
DOWNSTREAM OF ROTOR NUMBER 1

[illegible]

TABLE B-4 SAMPLE OF NON-DIMENSIONAL COMPUTER OUTPUT FOR NISRE PORTION OF PROGRAM FLOW

NON-DIMENSIONALIZED FLUID CONDITIONS FOR RUN NUMBER 15
 AVERAGE AXIAL VELOCITY COEFFICIENT VA/UT= 0.4389
 PRESSURES REFERRED TO PERIPHERAL TIP VELOCITY
 TEMPERATURES REFERRED TO INLET TEMPERATURE

R/R0	DPT/RHO*UT**2	OP/PHO*UT**2	TT/TT	T/TT	V/UT	VA/UT	WI/UT	W/UT	WA/UT	WI/UT	ALD+A	RFTA
0.6000	0.1275	-0.0829	1.0122	1.0101	0.5260	0.3017	0.5212	0.3905	0.3917	-0.0789	53.075	1.376
0.6177	0.1367	-0.0811	1.0114	1.0093	0.5264	0.3094	0.5168	0.4072	0.3994	-0.0977	52.272	-1.354
0.6315	0.1443	-0.0799	1.0104	1.0085	0.5273	0.4107	0.4938	0.4595	0.4210	-0.1141	49.889	-1.554
0.6591	0.1474	-0.0650	1.0101	1.0078	0.6452	0.4498	0.4732	0.4770	0.4449	-0.1721	46.765	-2.151
0.6729	0.1478	-0.0500	1.0098	1.0076	0.6400	0.4413	0.4635	0.4908	0.4516	-0.1965	45.117	-2.509
0.7005	0.1472	-0.0443	1.0098	1.0077	0.6319	0.4406	0.4554	0.5021	0.4516	-0.2104	44.519	-3.013
0.7218	0.1461	-0.0409	1.0099	1.0077	0.6266	0.4376	0.4537	0.5207	0.4471	-0.2324	43.561	-3.613
0.7457	0.1454	-0.0375	1.0100	1.0079	0.6081	0.4312	0.4515	0.5398	0.4432	-0.2554	43.585	-3.677
0.7694	0.1453	-0.0345	1.0100	1.0080	0.6022	0.4310	0.4515	0.5616	0.4417	-0.2854	42.789	-3.910
0.7920	0.1452	-0.0288	1.0100	1.0081	0.5968	0.4317	0.4514	0.5749	0.4417	-0.3681	42.265	-4.139
0.8108	0.1452	-0.0262	1.0100	1.0082	0.5978	0.4420	0.3820	0.6059	0.4424	-0.4449	41.642	-4.284
0.8318	0.1457	-0.0217	1.0100	1.0081	0.5971	0.4440	0.3671	0.6232	0.4505	-0.5249	40.919	-4.516
0.8522	0.1486	-0.0170	1.0099	1.0080	0.5922	0.4455	0.3551	0.6605	0.4545	-0.6093	39.518	-4.757
0.8660	0.1506	-0.0151	1.0097	1.0079	0.5774	0.4465	0.3508	0.6791	0.4586	-0.7014	37.412	-4.851
0.8936	0.1512	-0.0116	1.0095	1.0077	0.5758	0.4655	0.3431	0.7155	0.4655	-0.8229	35.846	-4.851
0.9074	0.1514	-0.0099	1.0093	1.0076	0.5722	0.4669	0.3398	0.7312	0.4669	-0.9627	35.223	-4.851
0.9212	0.1508	-0.0088	1.0092	1.0075	0.5693	0.4661	0.3383	0.7441	0.4661	-1.1049	35.082	-5.020
0.9488	0.1467	-0.0052	1.0092	1.0076	0.5688	0.4623	0.3360	0.7578	0.4623	-1.2571	35.316	-5.186
0.9723	0.1436	-0.0036	1.0096	1.0078	0.5682	0.4471	0.3342	0.7592	0.4471	-1.4213	37.791	-5.457
1.0000	0.1212	-0.0020	1.0104	1.0091	0.5590	0.3826	0.3555	0.7308	0.3826	-1.5929	49.179	-5.743
		0.0011	1.0104	1.0091	0.5520	0.3226	0.3555	0.7065	0.3226	-1.7919	49.179	-5.743

AVERAGE AXIAL VELOCITY COEFFICIENT VA/UT= 0.4389

TABLE B-5 SAMPLE OF DIMENSIONAL COMPUTER OUTPUT FOR FLOW PROBE PORTION OF PROGRAM FLOW

NAVAL POSTGRADUATE SCHOOL DUMPER, CALIFORNIA														
RADIAL FLUID CONDITIONS BASED ON PITOT STATIC INFORMATION WITH INPUT OF TOTAL TEMPERATURE AND ALPHA														
1193.0 RPM MASS FLOW RATE= 26.1730 LB/SEC PRESSURE= 29.92 IN Hg INLET TEMPERATURE= 77.9000 DEG-F DOWNSTREAM OF ROTOR NUMBER 1														
RADIUS (IN)	PT (PSFA)	P (PSFA)	TT (DEG-R)	T	V	VA	VU	VMACH	W	WA	WU	WMACH		
11.00	2125.360	2107.776	544.143	542.849	124.679	77.745	97.439	0.109	72.634	77.745	-17.091	0.070		
11.50	2125.360	2108.115	544.143	541.672	123.334	86.446	88.946	0.108	90.820	85.446	-30.780	0.080		
12.00	2125.360	2109.271	544.143	541.040	122.024	86.721	88.390	0.108	93.401	85.956	-36.541	0.082		
12.50	2125.360	2110.055	544.143	540.696	120.735	86.721	88.087	0.105	96.515	84.791	-45.060	0.084		
13.00	2125.360	2110.496	544.143	540.696	119.445	86.721	87.333	0.103	100.800	84.075	-54.267	0.087		
13.50	2125.360	2111.111	544.143	540.696	118.155	86.721	86.587	0.103	104.430	84.075	-64.267	0.092		
14.00	2125.360	2111.111	544.143	540.696	116.865	86.721	85.837	0.103	108.062	84.075	-74.267	0.097		
14.50	2125.360	2111.111	544.143	540.696	115.575	86.721	85.087	0.103	111.697	84.075	-84.267	0.102		
15.00	2125.360	2111.111	544.143	540.696	114.285	86.721	84.337	0.103	115.332	84.075	-94.267	0.107		
15.50	2125.360	2111.111	544.143	540.696	113.000	86.721	83.587	0.103	118.967	84.075	-104.267	0.108		
16.00	2125.360	2111.111	544.143	540.696	111.710	86.721	82.837	0.103	122.602	84.075	-114.267	0.110		
16.50	2125.360	2111.111	544.143	540.696	110.420	86.721	82.087	0.103	126.237	84.075	-124.267	0.113		
17.00	2125.360	2111.111	544.143	540.696	109.130	86.721	81.337	0.103	129.872	84.075	-134.267	0.115		
17.50	2125.360	2111.111	544.143	540.696	107.840	86.721	80.587	0.103	133.507	84.075	-144.267	0.118		
18.00	2125.360	2111.111	544.143	540.696	106.550	86.721	79.837	0.103	137.142	84.075	-154.267	0.120		
RAIUS (IN)	ALPHA	BETA	U											
11.00	51.400	12.385	119.520											
11.50	46.150	-19.810	119.931											
12.00	45.800	-23.031	120.136											
12.50	45.100	-27.082	120.542											
13.00	43.750	-32.077	120.955											
13.50	43.000	-37.072	121.368											
14.00	41.500	-42.067	121.782											
14.50	39.700	-47.063	122.196											
15.00	37.400	-49.020	122.610											
15.50	35.300	-51.340	123.024											
16.00	33.000	-54.497	123.438											
16.50	30.000	-58.231	123.852											
17.00	26.000	-62.615	124.266											
17.50	21.000	-67.615	124.680											
18.00	16.000	-72.615	125.094											

TABLE B-6 SAMPLE OF NON-DIMENSIONAL COMPUTER OUTPUT FOR FLOW PROBE PORTION OF PROGRAM FLOW

NON-DIMENSIONALIZED FLUID CONDITIONS FOR RUN NUMBER 35
 VELOCITY REFFERED TO PROBE TIP VELOCITY
 PRESSURES REFFERED TO RHO*UT**2
 TEMPERATURES REFFERED TO INLET TEMPERATURE

R/R0	DPT/RHO*UT**2	DP/RHO*UT**2	TT/TTI	T/TTI	V/UIT	VA/UIT	VII/UIT	W/UIT	WA/UT	WII/UIT	ALPHA	RETA
0.6111	0.1357	-0.0927	1.0122	1.0098	0.6653	0.4151	0.5200	0.4250	0.4151	-0.0011	51.400	-1.2.395
0.6389	0.1471	-0.0722	1.0095	1.0076	0.6578	0.4560	0.4744	0.4846	0.4587	-0.0162	44.950	-1.0.010
0.6667	0.1471	-0.0562	1.0105	1.0043	0.6510	0.4525	0.4717	0.4984	0.4587	-0.0160	45.100	-1.2.031
0.6944	0.1471	-0.0465	1.0103	1.0093	0.6424	0.4518	0.4540	0.5124	0.4525	-0.0204	45.150	-1.2.032
0.7222	0.1471	-0.0371	1.0097	1.0076	0.6297	0.4518	0.4325	0.5367	0.4518	-0.0289	43.750	-1.2.477
0.7500	0.1471	-0.0340	1.0097	1.0076	0.6207	0.4540	0.4233	0.5593	0.4540	-0.0326	43.000	-1.2.744
0.7778	0.1471	-0.0312	1.0105	1.0097	0.6067	0.4540	0.4007	0.5993	0.4540	-0.0407	41.000	-1.2.744
0.8056	0.1471	-0.0297	1.0095	1.0097	0.5902	0.4605	0.3850	0.6236	0.4505	-0.0420	39.900	-1.2.407
0.8333	0.1471	-0.0297	1.0095	1.0097	0.5805	0.4605	0.3557	0.6472	0.4505	-0.0420	39.000	-1.2.407
0.8611	0.1484	-0.0216	1.0095	1.0076	0.5695	0.4774	0.3393	0.6720	0.4774	-0.0420	37.000	-1.2.407
0.8889	0.1484	-0.0166	1.0094	1.0076	0.5587	0.4774	0.3315	0.6944	0.4774	-0.0420	35.000	-1.2.407
0.9167	0.1497	-0.0135	1.0094	1.0076	0.5486	0.4682	0.3294	0.7194	0.4682	-0.0420	33.000	-1.2.407
0.9444	0.1471	-0.0122	1.0092	1.0076	0.5436	0.4387	0.3294	0.7494	0.4387	-0.0420	31.000	-1.2.407
0.9722	0.1471	-0.0144	1.0099	1.0083	0.5172	0.3962	0.3324	0.7525	0.3962	-0.0420	29.000	-1.2.407
1.0000	0.1167	0.0172	1.0102	1.0091	0.4481	0.2916	0.3402	0.7213	0.2916	-0.0420	27.000	-1.2.407

AVERAGE AXIAL VELOCITY COEFFICIENT VA/UT= 0.4405

TABLE B-8 SAMPLE OF NON-DIMENSIONAL COMPUTER OUTPUT FOR HOT-WIRE PORTION OF PROGRAM FLOW

NON-DIMENSIONALIZED FLUID CONDITIONS FOR RUN NUMBER 35
 ALL VELOCITIES REFERRED TO PERIPHERAL TIP VELOCITY
 PRESSURES REFERRED TO $\rho H_0 U T^{*2}$
 TEMPERATURES REFERRED TO INLET TEMPERATURE

R/RD	DPT/RHO*UT**2	OP/RHO*UT**2	TY/II	TY/II	V/UT	VA/UT	VU/UT	W/UT	WA/UT	WU/UT	ALPHA	BETA
0.6111	0.1357	-0.0589	1.0122	1.0100	0.6269	0.3911	0.4899	0.4094	0.3911	-0.1212	51.400	-17.218
0.6389	0.1395	-0.0593	1.0099	1.0078	0.6329	0.4384	0.4564	0.4749	0.4384	-0.0795	46.150	-22.508
0.6667	0.1471	-0.0644	1.0095	1.0074	0.6422	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.6944	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.7222	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.7500	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.7778	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.8056	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.8333	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.8611	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.8889	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.9167	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.9444	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
0.9722	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508
1.0000	0.1471	-0.0649	1.0105	1.0084	0.6489	0.4352	0.4475	0.4749	0.4352	-0.0795	45.830	-22.508

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13. ABSTRACT

This work was undertaken to check the feasibility of obtaining the velocity profiles downstream of the rotors of turbomachines by measuring only the radial distributions of total temperature, total pressure, and absolute flow angle and using these data to calculate the flow velocities by the non-isentropic radial equilibrium equation such that the measured flow rate is matched. Curvature effects are ignored in this analysis.

The velocities calculated by this method are compared with those obtained by measurements with flow probes and hot-wire anemometers.

The tests were conducted on a 3-stage axial flow compressor of the Turbo-Propulsion Laboratory at the Naval Postgraduate School. Measurements were made over the entire operating range of the compressor at a fixed rotor speed of about 1200 rpm.

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Hot-Wire Anemometry

1

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